

The logo of The University of Texas at Dallas, featuring a circular seal with the letters 'UTD' in the center, the text 'THE UNIVERSITY OF TEXAS AT DALLAS' around the top, and 'EST. 1969' at the bottom. Two stars are positioned on either side of the 'EST. 1969' text.

Visual Rendering: Rasterization, Lighting and Shading, Fragment Processing

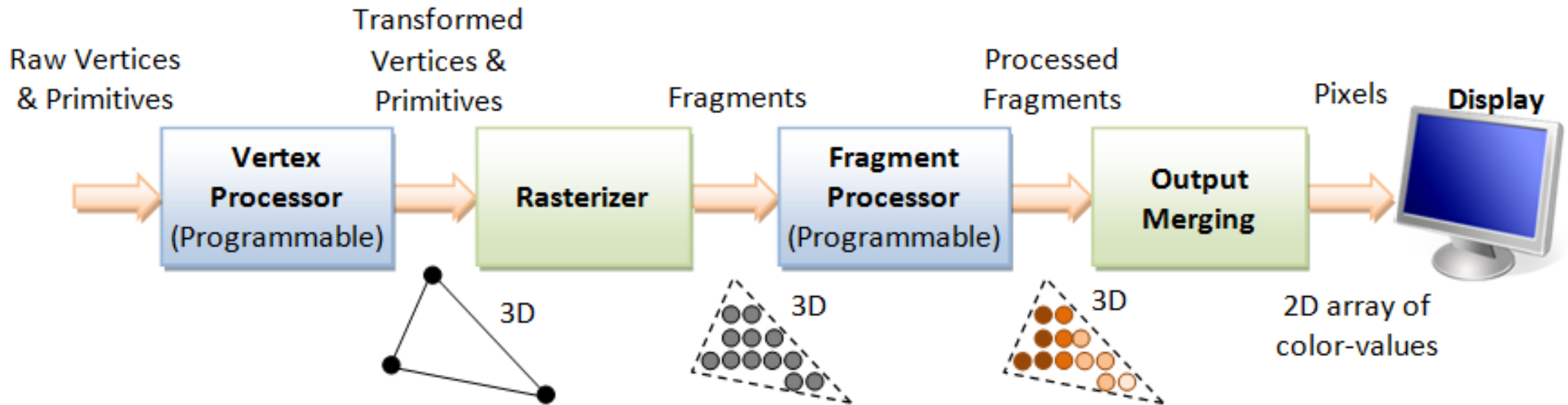
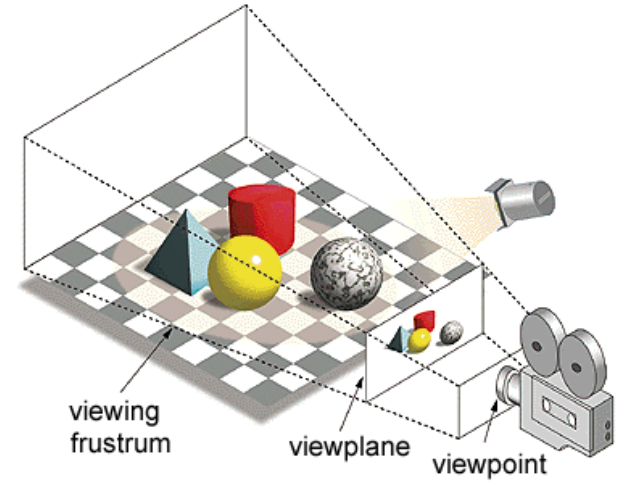
CS 6384 Computer Vision

Professor Yu Xiang

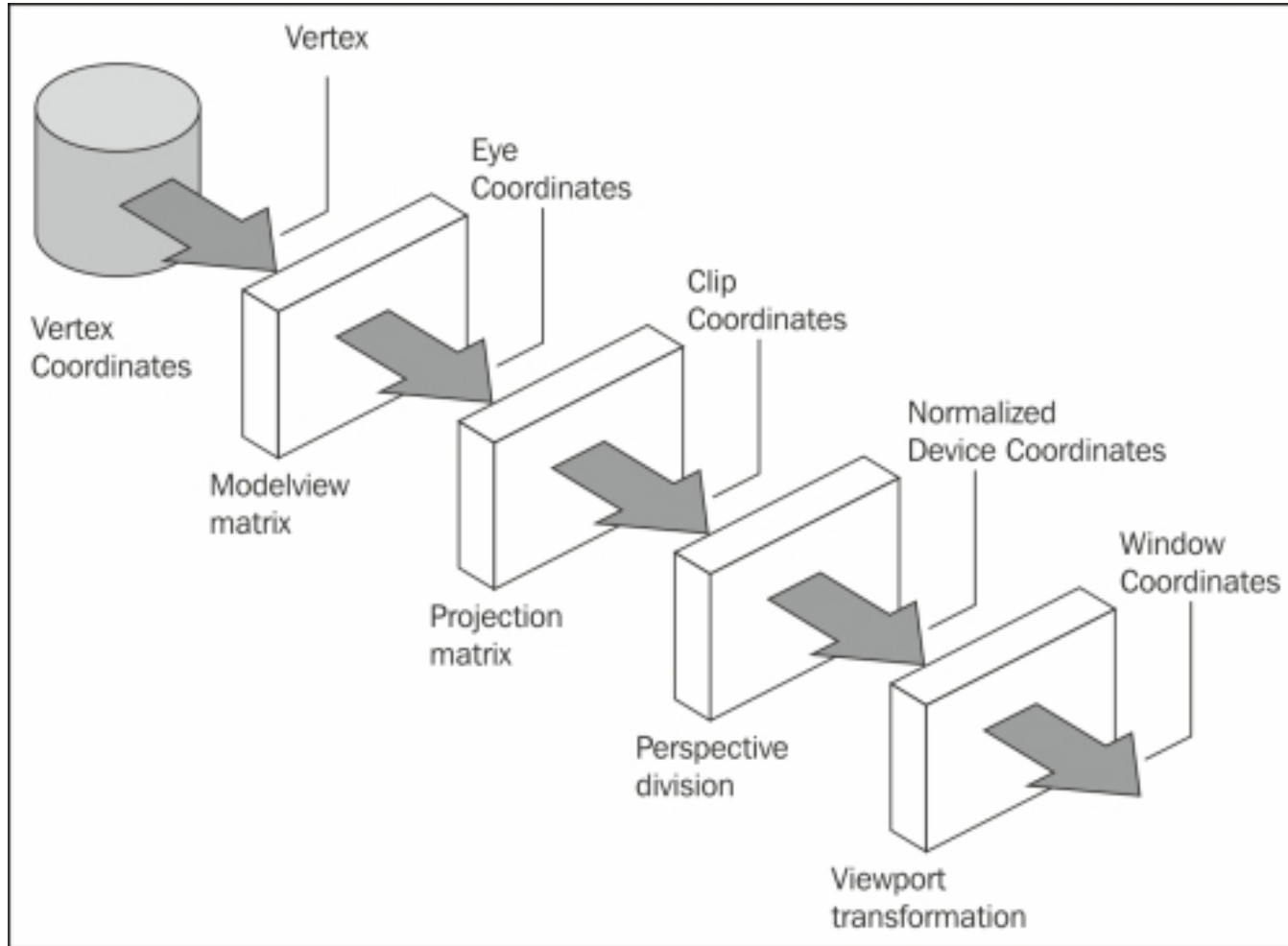
The University of Texas at Dallas

Visual Rendering

- Converting 3D scene descriptions into 2D images
- The graphics pipeline



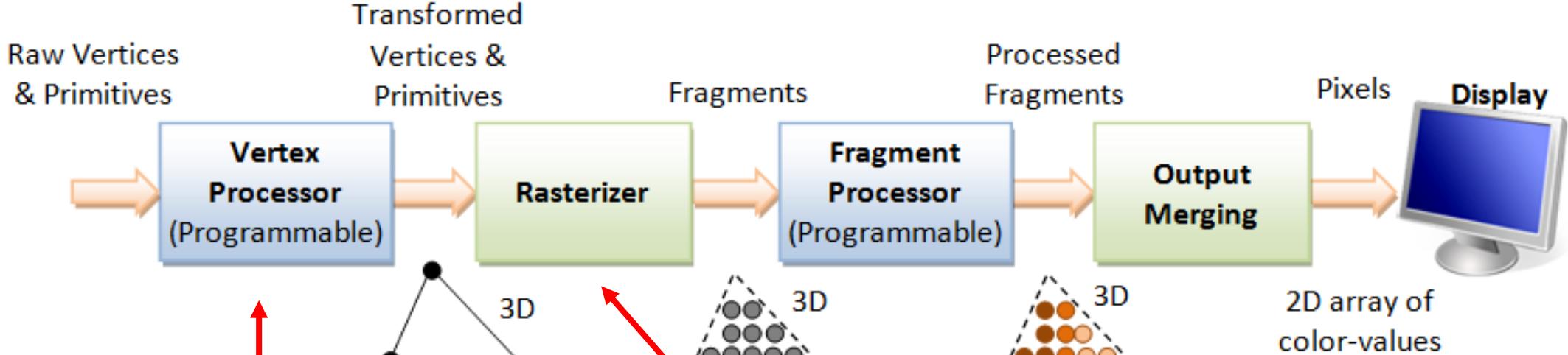
Vertex Transform



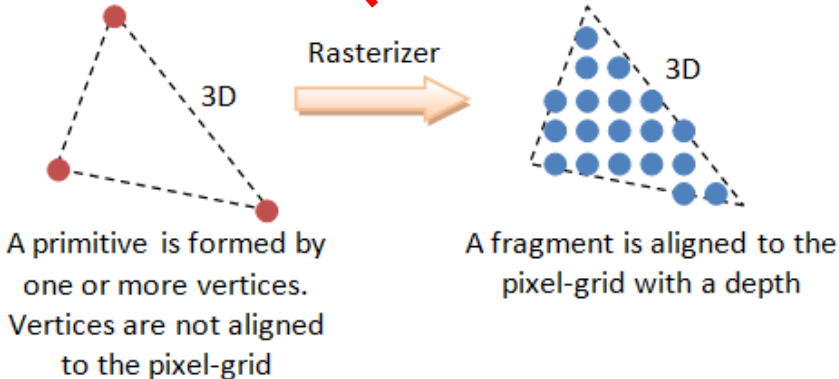
$$v_{window} = \begin{pmatrix} x_{window} \\ y_{window} \\ z_{window} \\ 1 \end{pmatrix} \begin{matrix} \in (0, width) \\ \in (0, height) \\ \in (0, 1) \end{matrix}$$

vertex in window coords

Rasterization



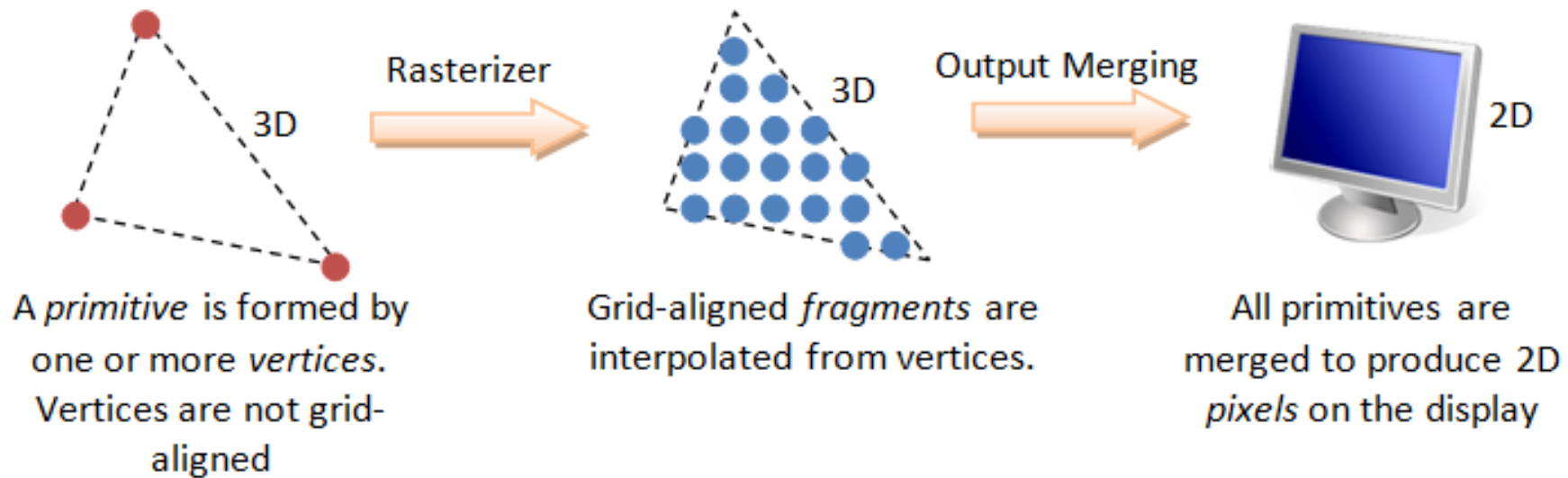
Vertex transforms



- Determine which pixels are inside the triangles
- Interpolate vertex attributes (e.g., color)

Pixels vs. Fragments

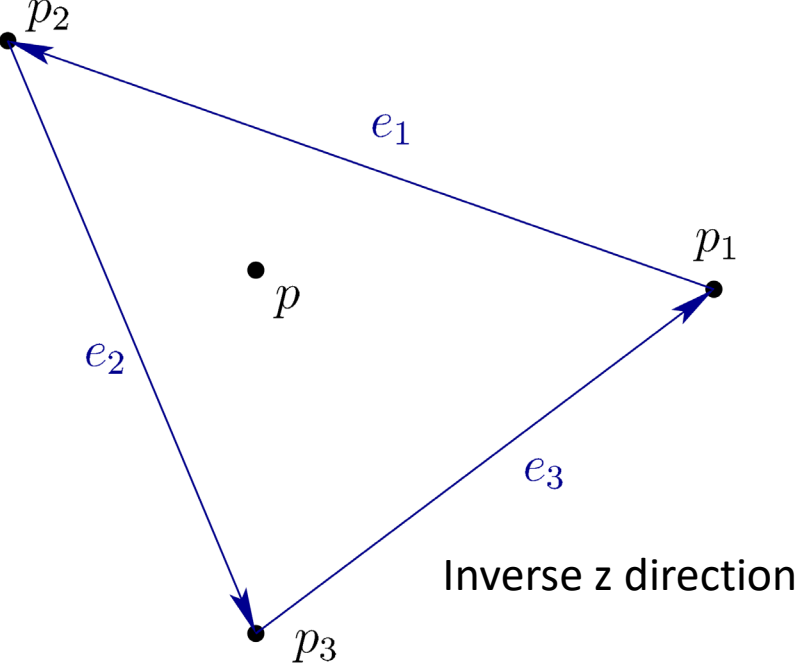
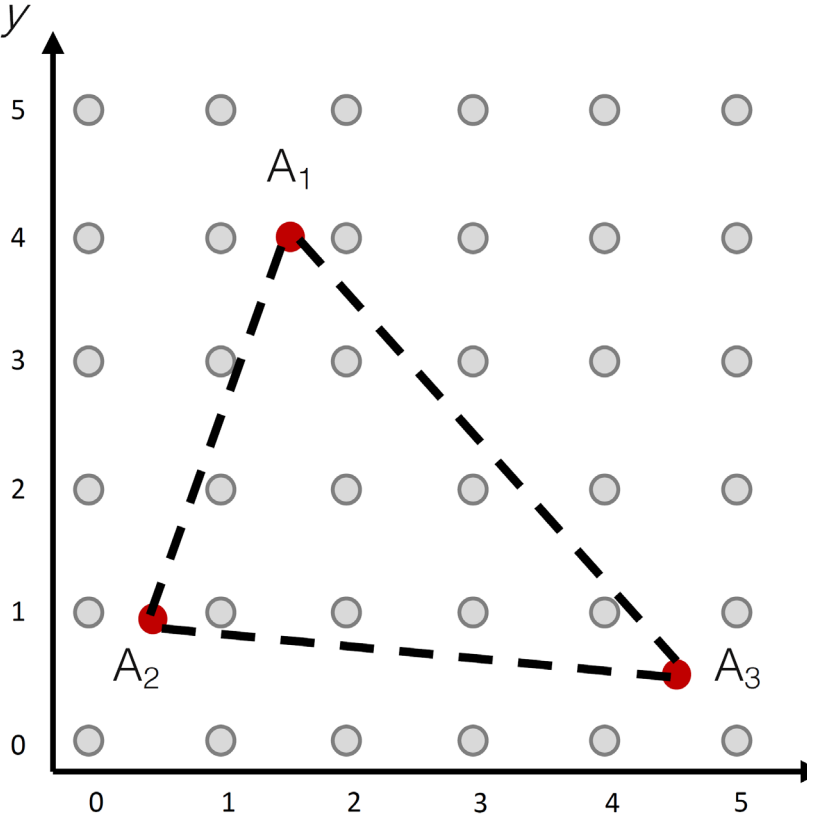
- Pixels are dots on the screen: (x, y) and RGB color
- Fragments: (x, y, z) , z is the depth and other attributes (color, normal, texture coordinates, alpha value, etc.)



Vertex, Primitives, Fragment and Pixel

Rasterization

- Determine which fragments are inside the triangle



$$e_1 = p_2 - p_1$$

$$e_2 = p_3 - p_2$$

$$e_3 = p_1 - p_3$$

p is inside if and only if

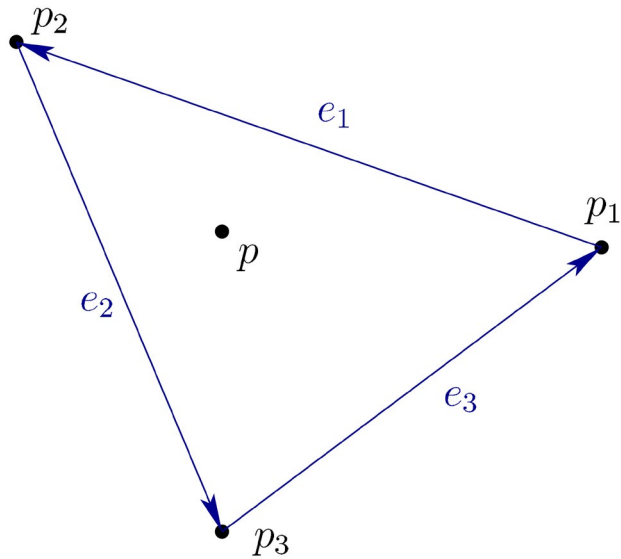
$$(p - p_1) \times e_1 < 0$$

$$(p - p_2) \times e_2 < 0$$

$$(p - p_3) \times e_3 < 0$$

magnitude of the cross products

Barycentric Coordinates



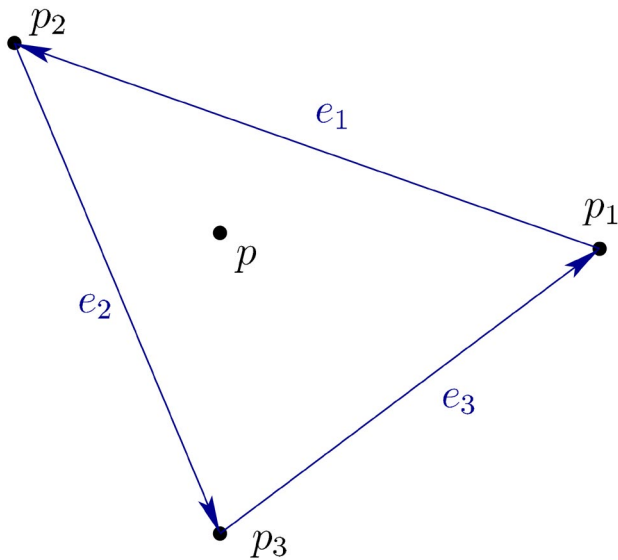
- Interpolate attributes of the vertices

$$p = \alpha_1 p_1 + \alpha_2 p_2 + \alpha_3 p_3$$

$$0 \leq \alpha_1, \alpha_2, \alpha_3 \leq 1$$

$$\alpha_1 + \alpha_2 + \alpha_3 = 1$$

Barycentric Coordinates



$$\mathbf{p}_1 = \begin{bmatrix} x_1 \\ y_1 \\ z_1 \end{bmatrix} \quad \mathbf{p}_2 = \begin{bmatrix} x_2 \\ y_2 \\ z_2 \end{bmatrix} \quad \mathbf{p}_3 = \begin{bmatrix} x_3 \\ y_3 \\ z_3 \end{bmatrix} \quad \mathbf{p} = \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$p = \alpha_1 p_1 + \alpha_2 p_2 + \alpha_3 p_3$$

$$0 \leq \alpha_1, \alpha_2, \alpha_3 \leq 1 \quad \alpha_1 + \alpha_2 + \alpha_3 = 1$$

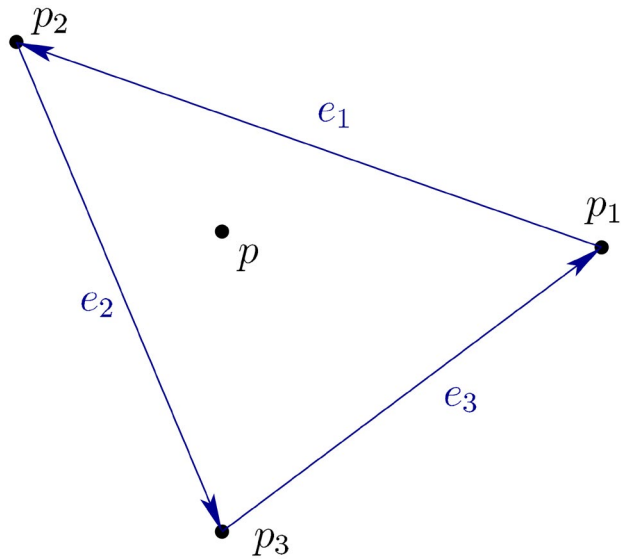
$$\alpha_1 = \frac{(y_2 - y_3)(x - x_3) + (x_3 - x_2)(y - y_3)}{(y_2 - y_3)(x_1 - x_3) + (x_3 - x_2)(y_1 - y_3)},$$

$$\alpha_2 = \frac{(y_3 - y_1)(x - x_3) + (x_1 - x_3)(y - y_3)}{(y_2 - y_3)(x_1 - x_3) + (x_3 - x_2)(y_1 - y_3)},$$

$$\alpha_3 = 1 - \alpha_1 - \alpha_2.$$

https://en.wikipedia.org/wiki/Barycentric_coordinate_system

Barycentric Coordinates



$$p = \alpha_1 p_1 + \alpha_2 p_2 + \alpha_3 p_3$$

Color

$$R = \alpha_1 R_1 + \alpha_2 R_2 + \alpha_3 R_3$$

$$G = \alpha_1 G_1 + \alpha_2 G_2 + \alpha_3 G_3$$

$$B = \alpha_1 B_1 + \alpha_2 B_2 + \alpha_3 B_3.$$

Apply to other attributes, e.g., depth, texture coordinates, alpha value, etc.

Depth Buffer for Visibility Testing

- When drawing multiple triangles, determine which one to draw and which one to discard
- If depth of fragment is **smaller than** the current value is the depth buffer, overwrite color and depth value using the current fragment



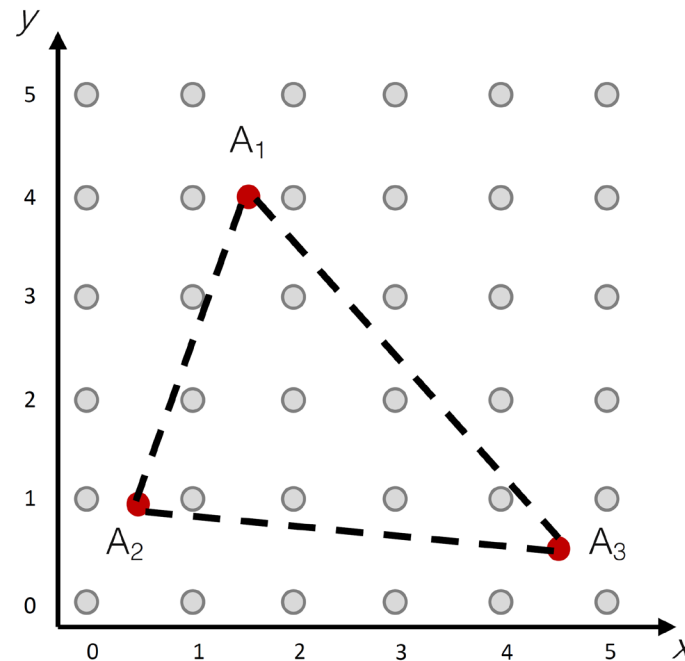
color buffer



depth buffer

Lighting and Shading

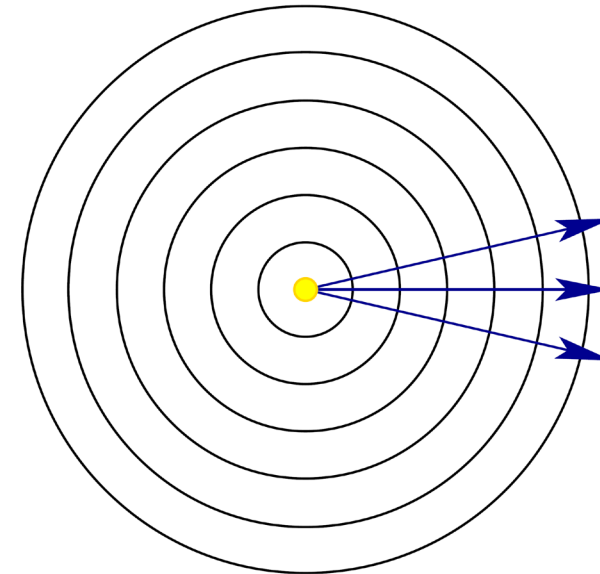
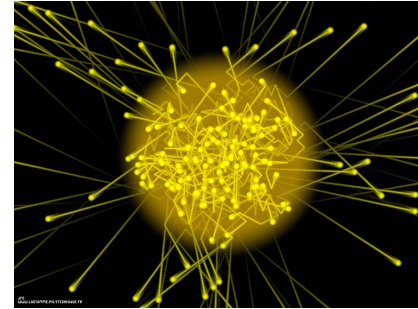
- How to determine color and what attributes to interpolate after rasterization



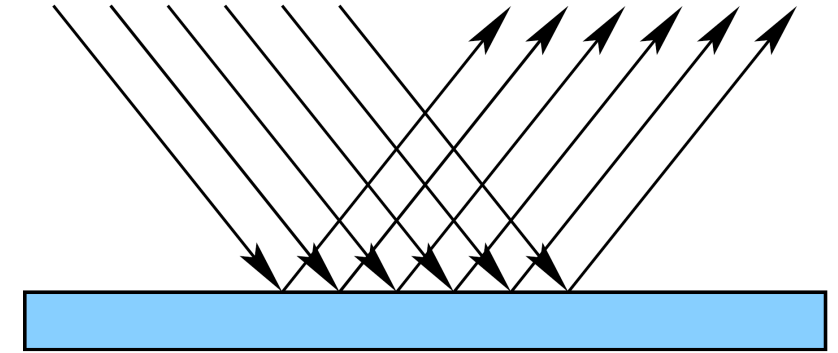
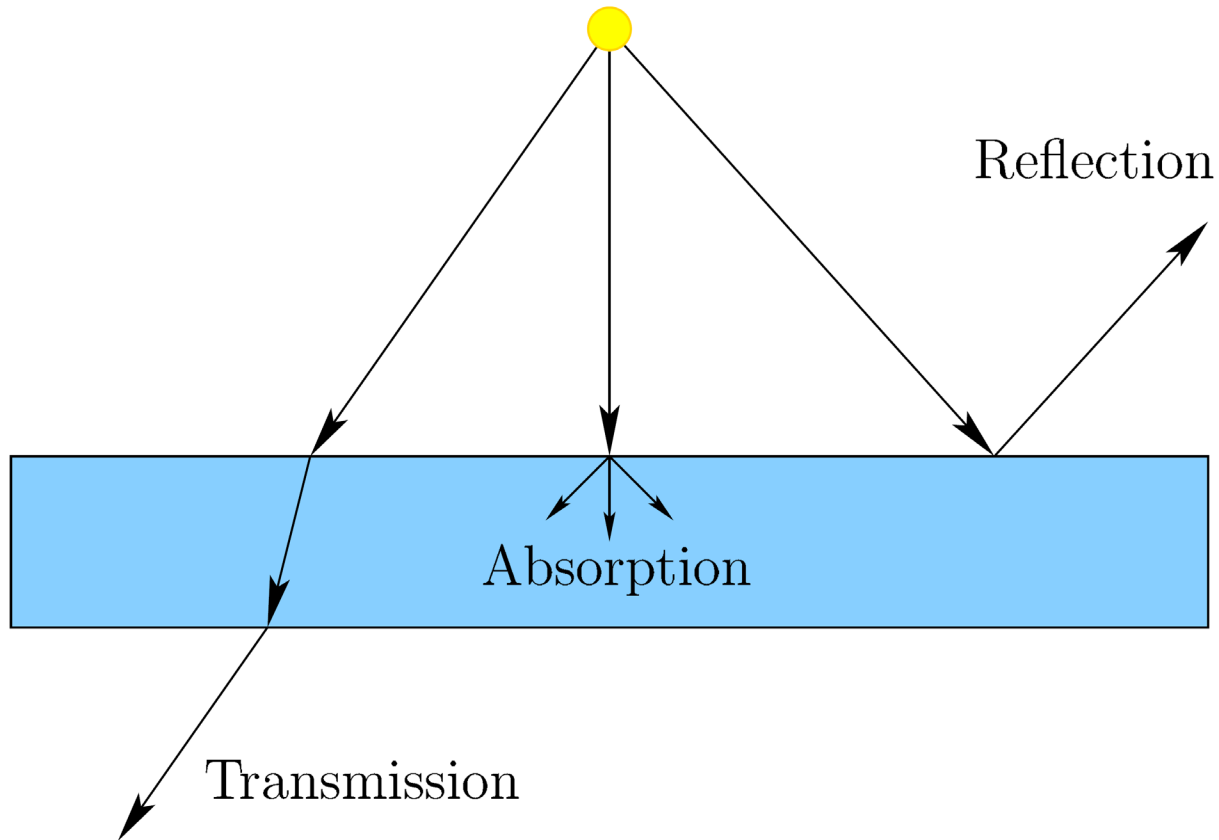
Rasterization: determine which fragments are inside the triangles

Basic Behavior of Light

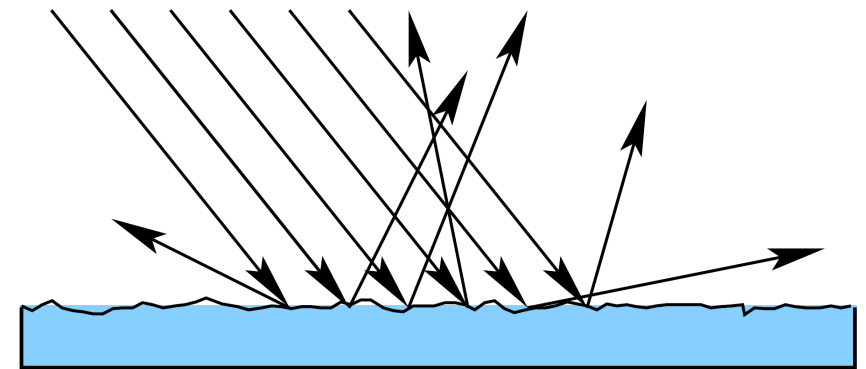
- Light can be described in three ways
 - Photons: tiny particles of energy moving through space at high speed
 - Waves: ripples through space
 - Rays: a ray traces the motion of a single hypothetical photon



Interactions with Materials

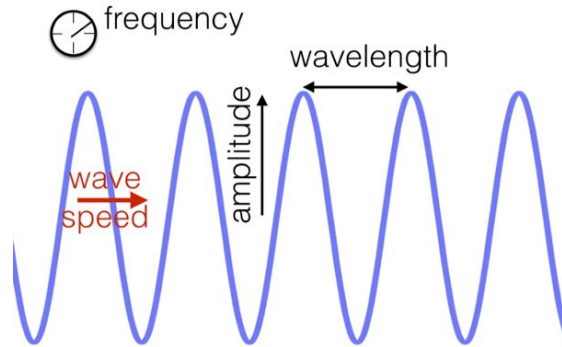


Specular



Diffuse

Wavelengths and Colors

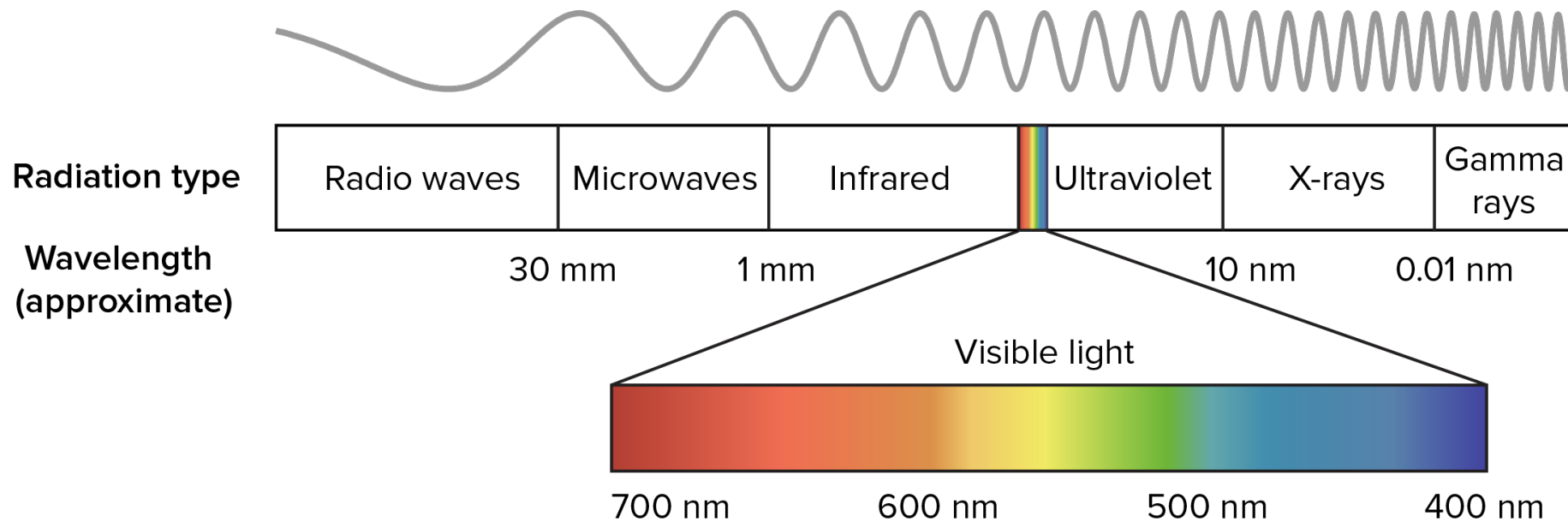


Wavelength $\lambda = \frac{v}{f}$

Speed: meters per second

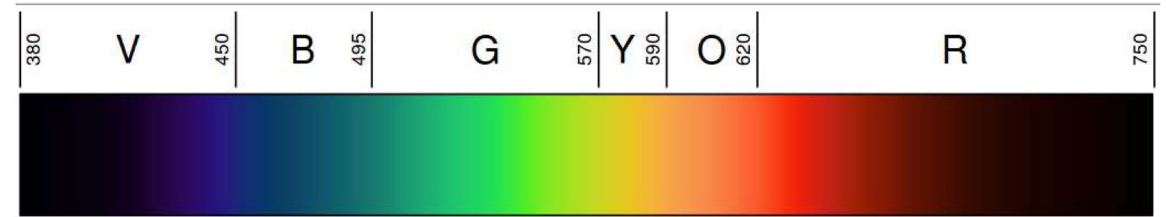
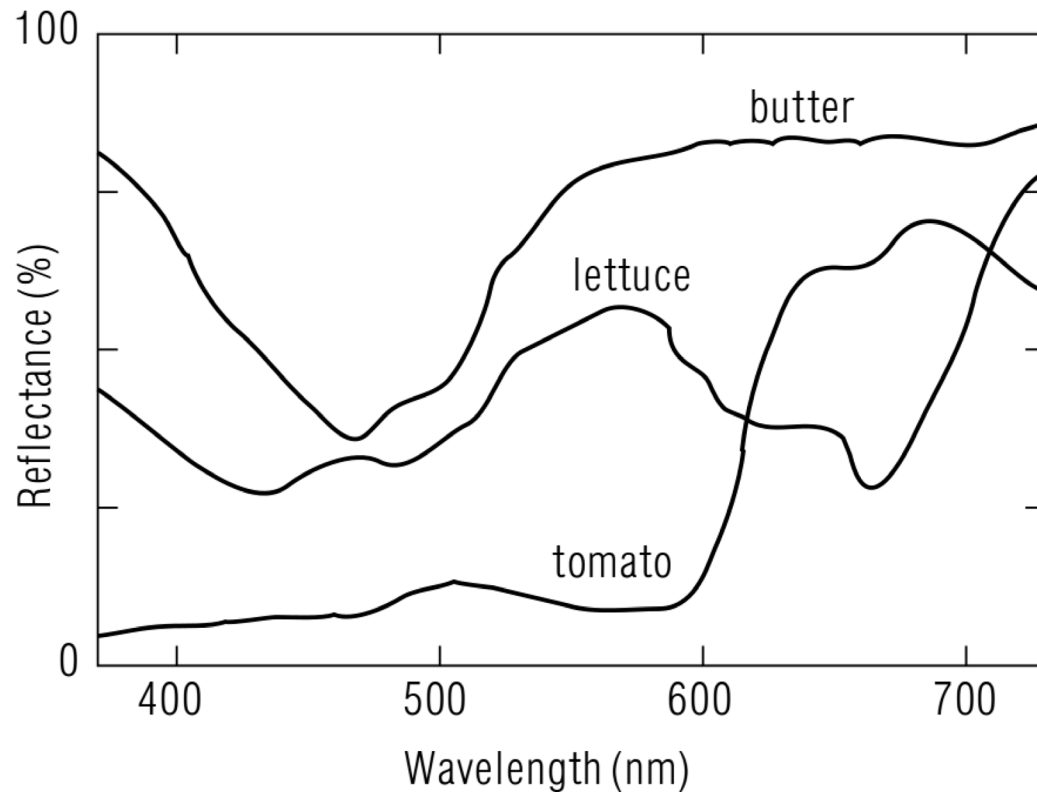
Frequency: how many cycles per second

Electromagnetic spectrum



Reflection of Materials

- We see objects with different colors because the materials reflect specific colors differently



Lambertian Lighting

Diffuse reflection

$$R = d_R I_R \max(0, n \cdot \ell)$$

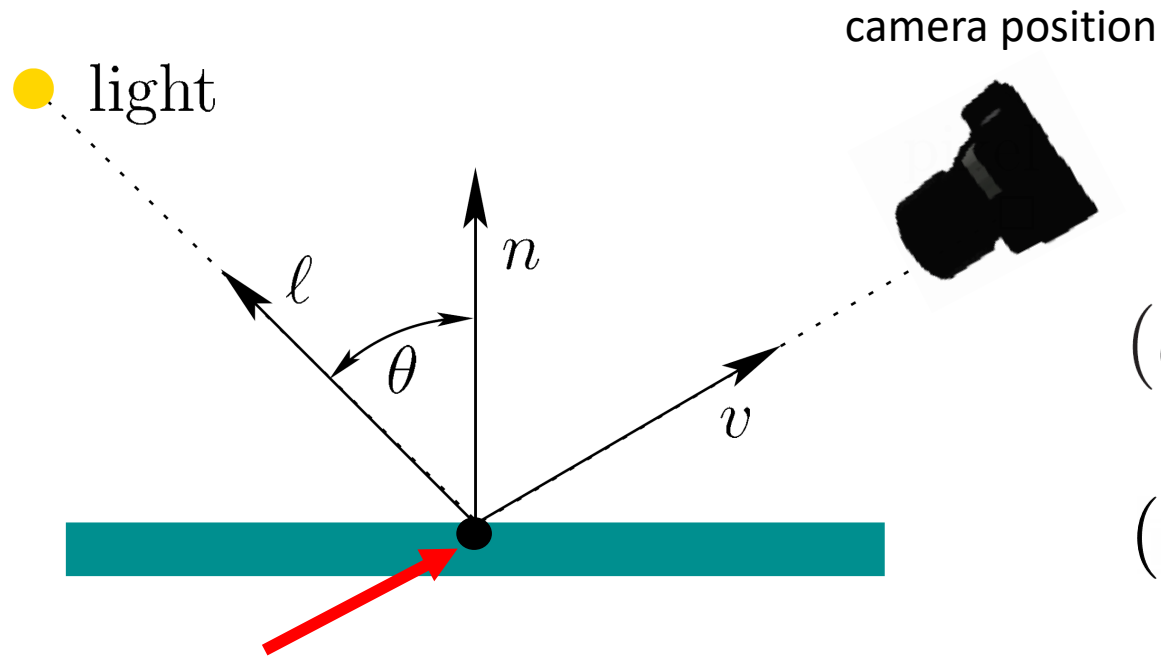
$$G = d_G I_G \max(0, n \cdot \ell)$$

$$B = d_B I_B \max(0, n \cdot \ell)$$

$$n \cdot \ell = \cos \theta$$

(d_R, d_G, d_B) Reflectance property of the material (triangle)

(I_R, I_G, I_B) Spectral power distribution of the light source

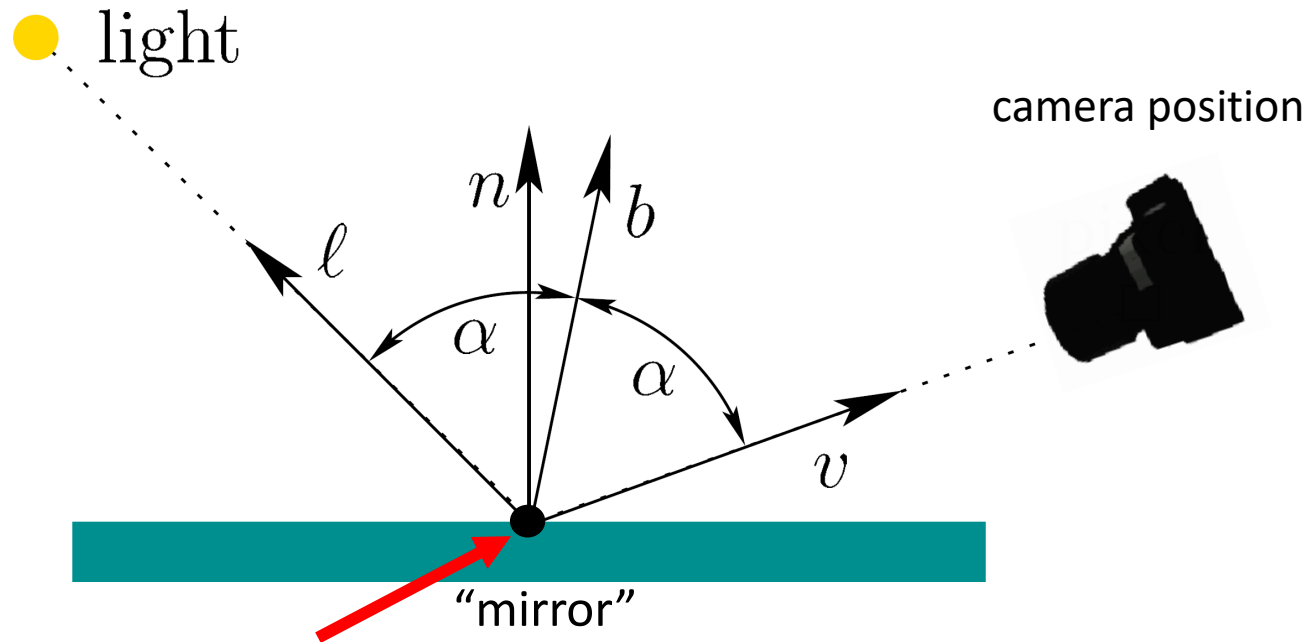


Think about this point as a vertex of a 3D mesh. We want to compute its color on the image

$$L = dI \max(0, n \cdot \ell) \quad n \cdot \ell < 0$$

Light behind triangle

Blinn-Phong Lighting



Think about this point as
a vertex of a 3D mesh.
We want to compute its
color on the image

Related to specular reflection

$$b = \frac{l + v}{\|l + v\|}$$

x Material property that expresses
the amount of surface shininess
 $x=100$, mild amount of shininess
 $x=10000$, almost like a mirror

s Specular reflectance
property of the material

$$L = dI \max(0, n \cdot l) + sI \max(0, n \cdot b)^x$$

Ambient Lighting

- Independent of light/surface position, viewer, normal
- Adding some background color

$$L = dI \max(0, n \cdot \ell) + sI \max(0, n \cdot b)^x + L_a$$

Ambient light



Multiple Light Sources and Attenuation

- N light sources

$$L = L_a + \sum_{i=1}^N dI_i \max(0, n \cdot l_i) + sI_i \max(0, n \cdot b_i)^x$$

- Attenuation: the greater the distance, the low the intensity

$$L = L_a + \sum_{i=1}^N \frac{1}{k_c + k_l c + k_q c^2} \left(dI_i \max(0, n \cdot l_i) + sI_i \max(0, n \cdot b_i)^x \right)$$

constant linear quadratic attenuation

c Light source distance to surface

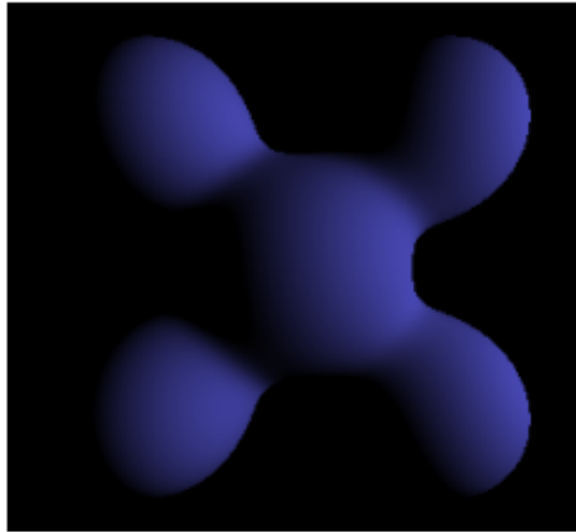
Used by OpenGL for ~25 years

Phong Reflection Model



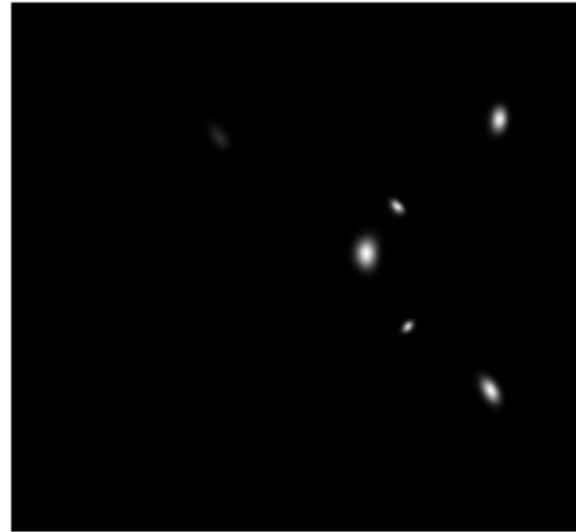
Ambient

+



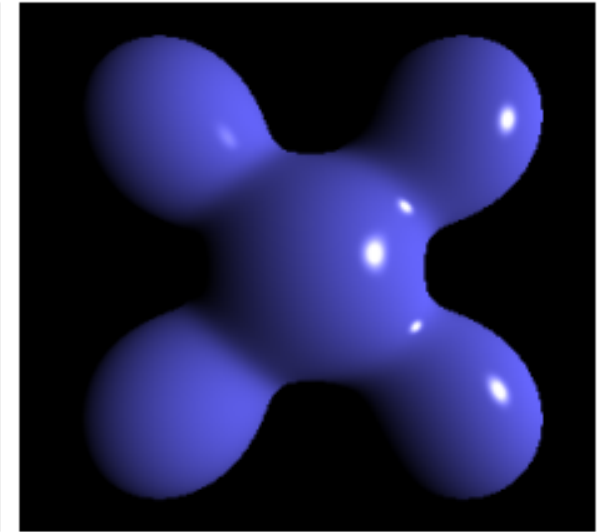
Diffuse

+



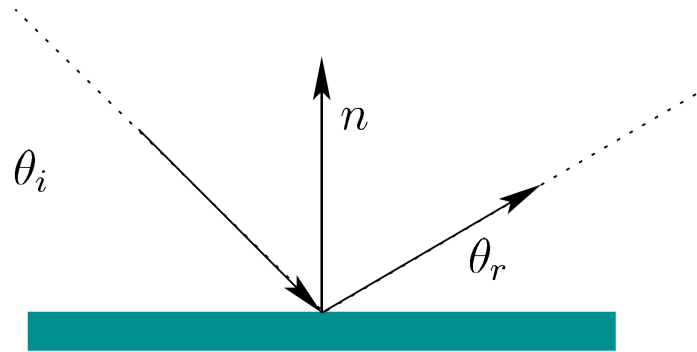
Specular

=

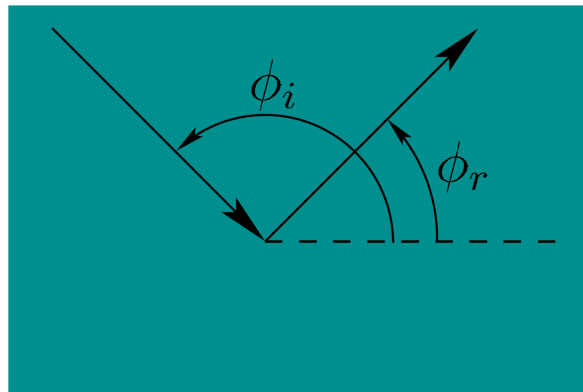


Phong Reflection

Bidirectional Reflectance Distribution Function (BRDF)



Side view



Top view

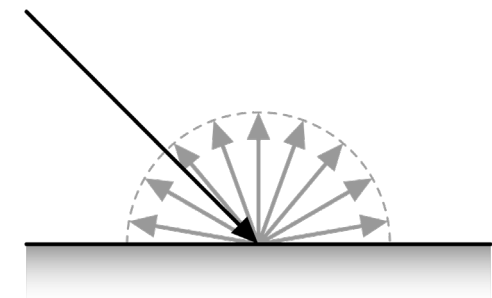
Shading in a more precise and general way

$$f(\theta_i, \phi_i, \theta_r, \phi_r) = \frac{\text{radiance}}{\text{irradiance}}$$

- Radiance: light energy reflected from the surface
- Irradiance: light energy arriving at the surface

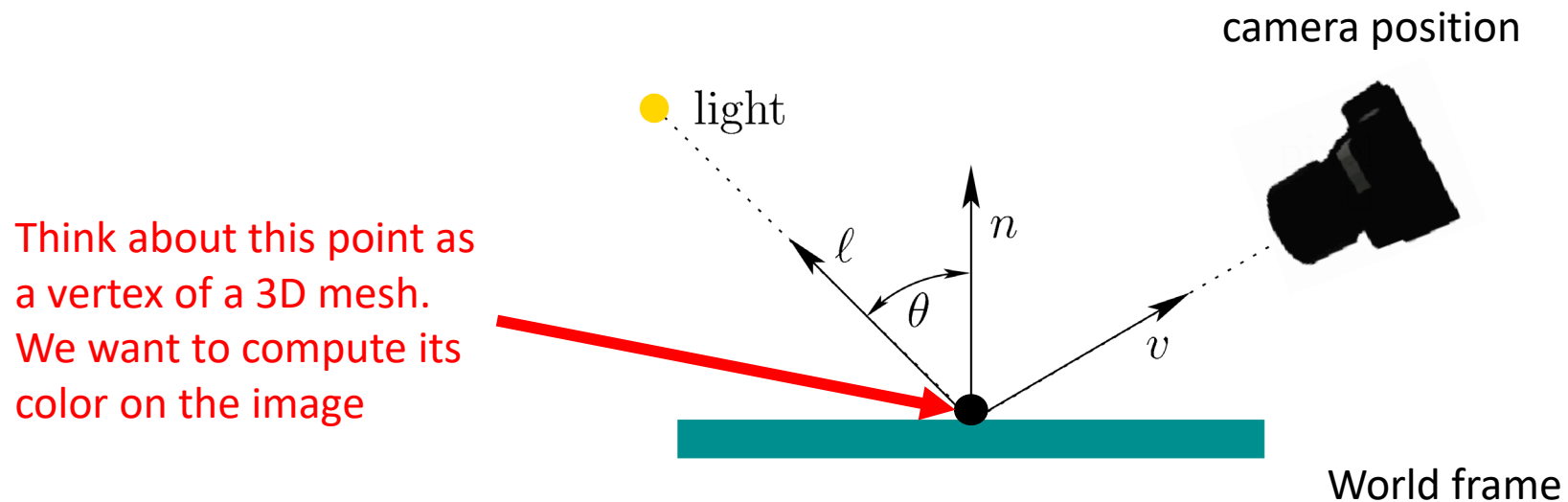
For Lambertian shading,
BRDF is a constant

- The surface reflects equally in all directions



Lighting Calculations

- All lighting calculations can happen in world space
 - Transform vertices and normal into world space
- Calculate lighting, i.e., compute vertex color given material properties, light source color and position, vertex position, normal position, view position

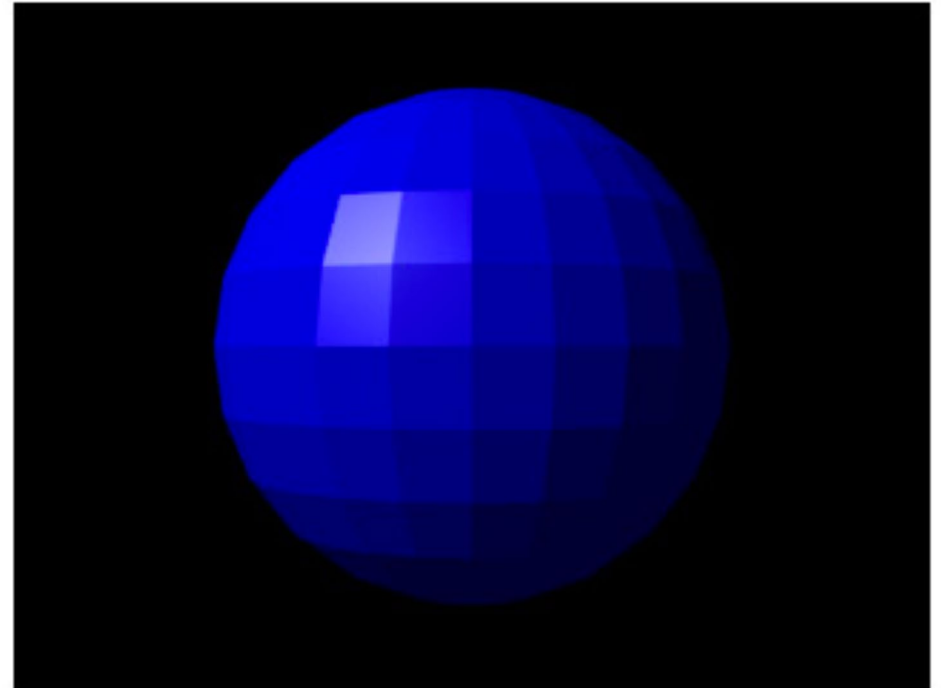


Lighting vs. Shading

- Lighting: interaction between light and surface
 - Different mathematic models exist, e.g., Phong lighting model
 - What formula is being used to calculate intensity/color
- Shading: how to compute color for each fragment
 - What attributes to interpolate
 - Where to do lighting calculation

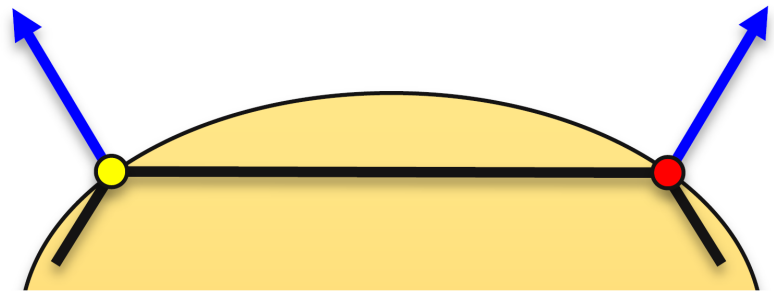
Flat Shading

- Compute color only once per triangle (i.e., with Phong lighting)
 - Compute color for the first vertex or the centroid
- Pro: fast to compute
- Con: create a flat, unrealistic appearance



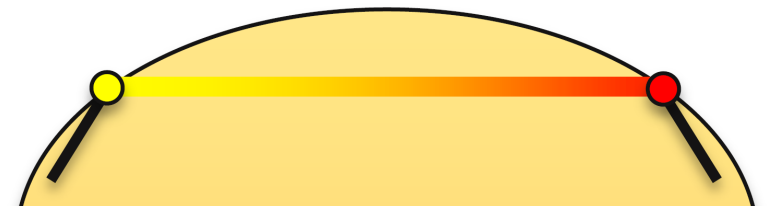
Gouraud or Per-vertex Shading

- Compute color only once per vertex (i.e., with Phong lighting)
- Interpolate per-vertex color to all fragments within the triangle
- Pro: fast to compute
- Con: flat, unrealistic specular highlights



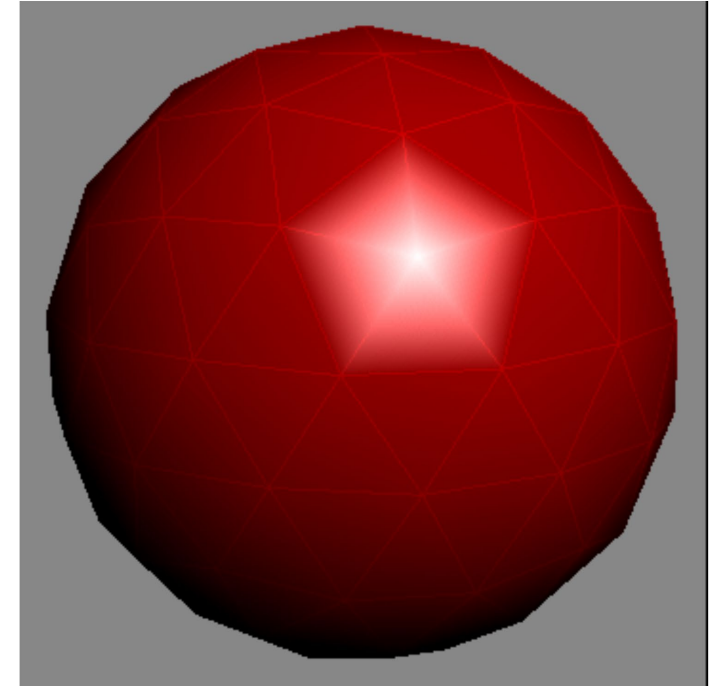
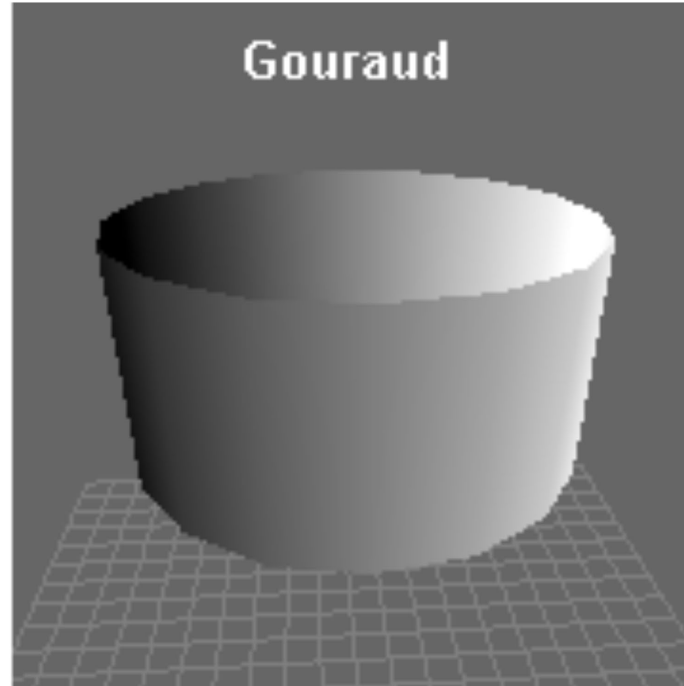
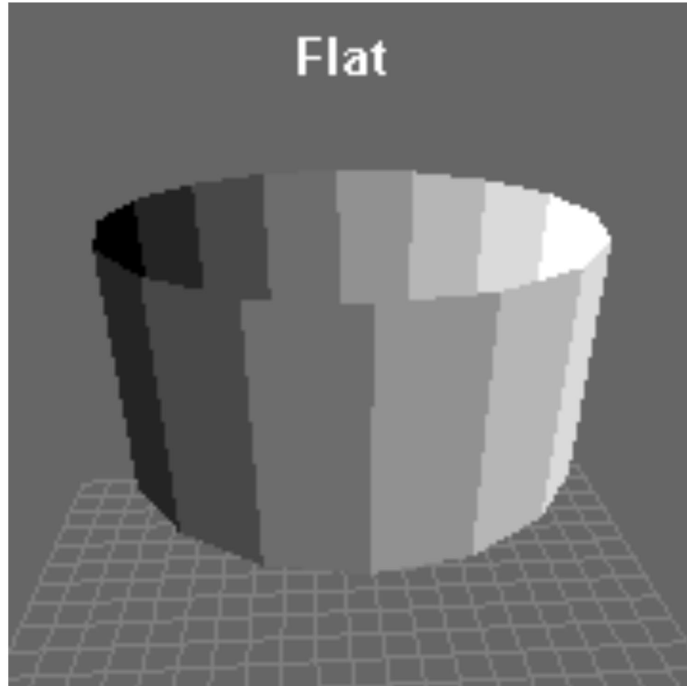
per-vertex lighting

interpolate colors



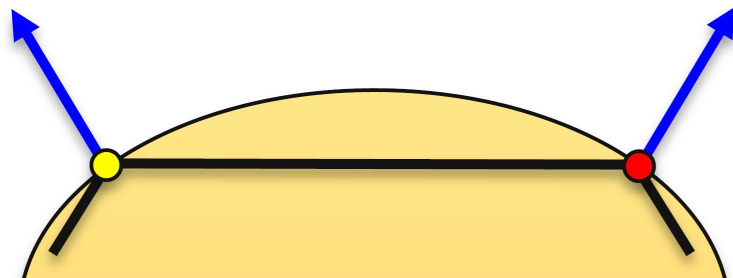
shaded surface

Gouraud or Per-vertex Shading

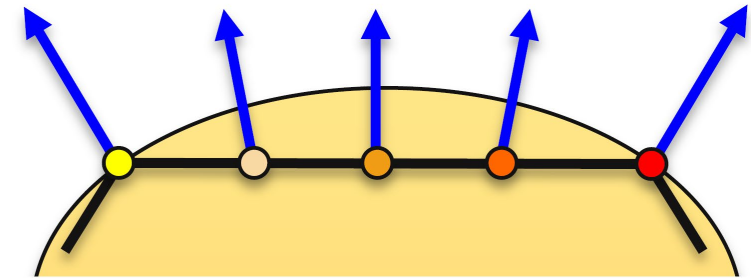


Phong Shading or Per-fragment Shading

- Compute color only once per fragment (i.e., with Phong lighting)
- Need to interpolate per-vertex normal to all fragments to do the lighting calculation
- Pro: better appearance of specular highlights
- Con: slower to compute



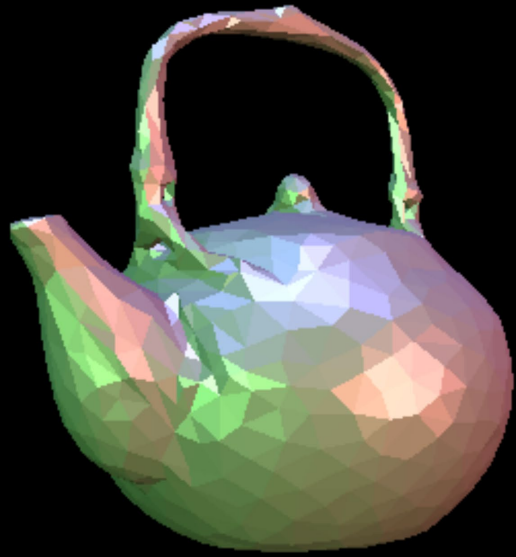
interpolate normals



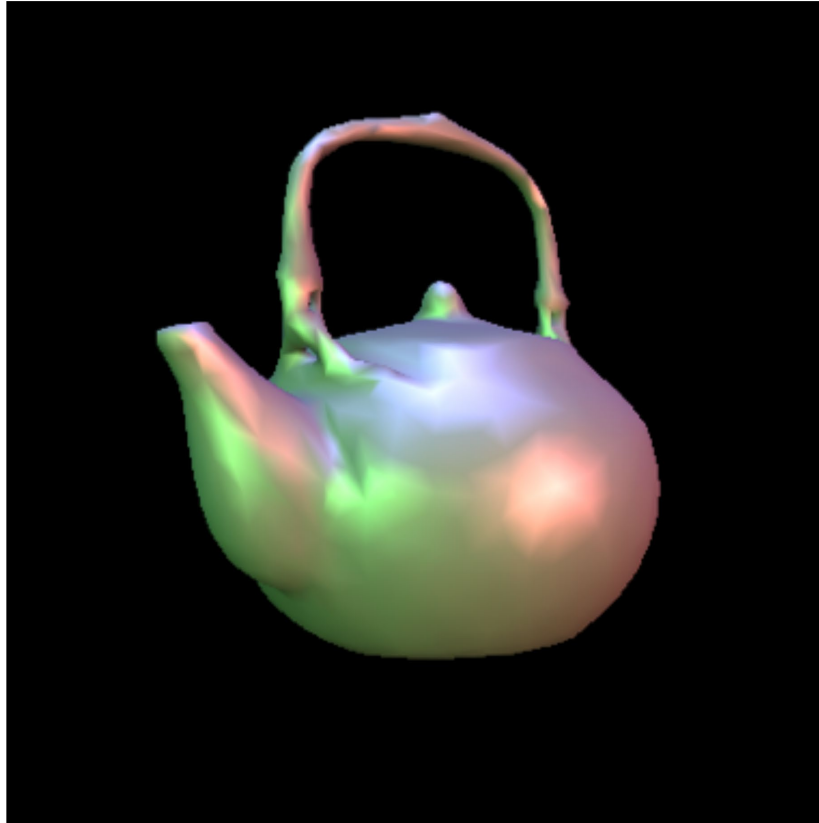
per-fragment lighting

Shading

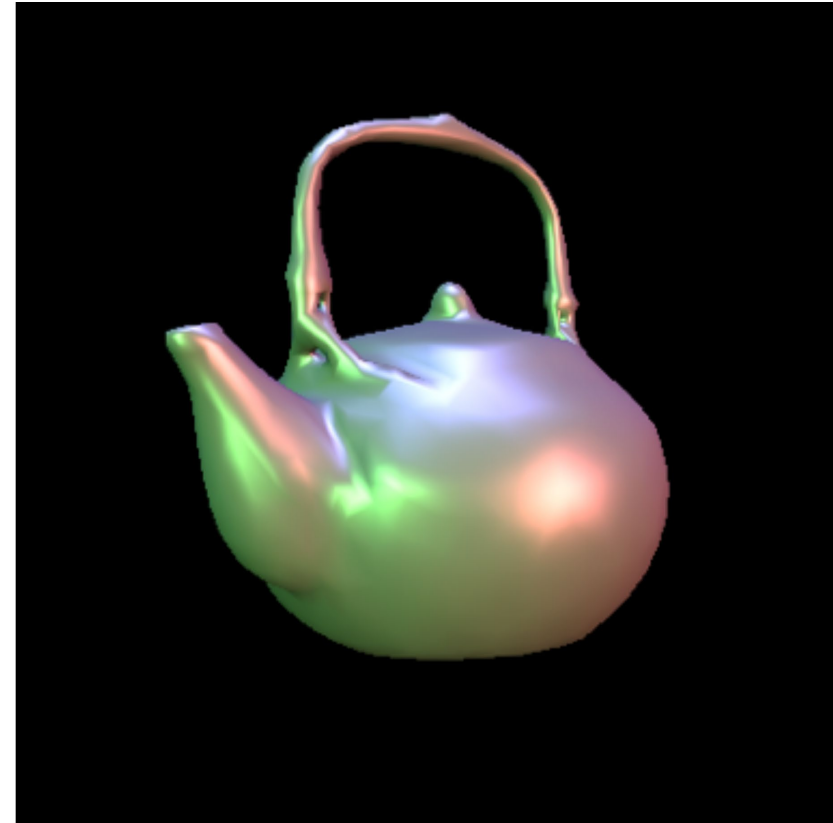
Flat Shading



Gouraud Shading

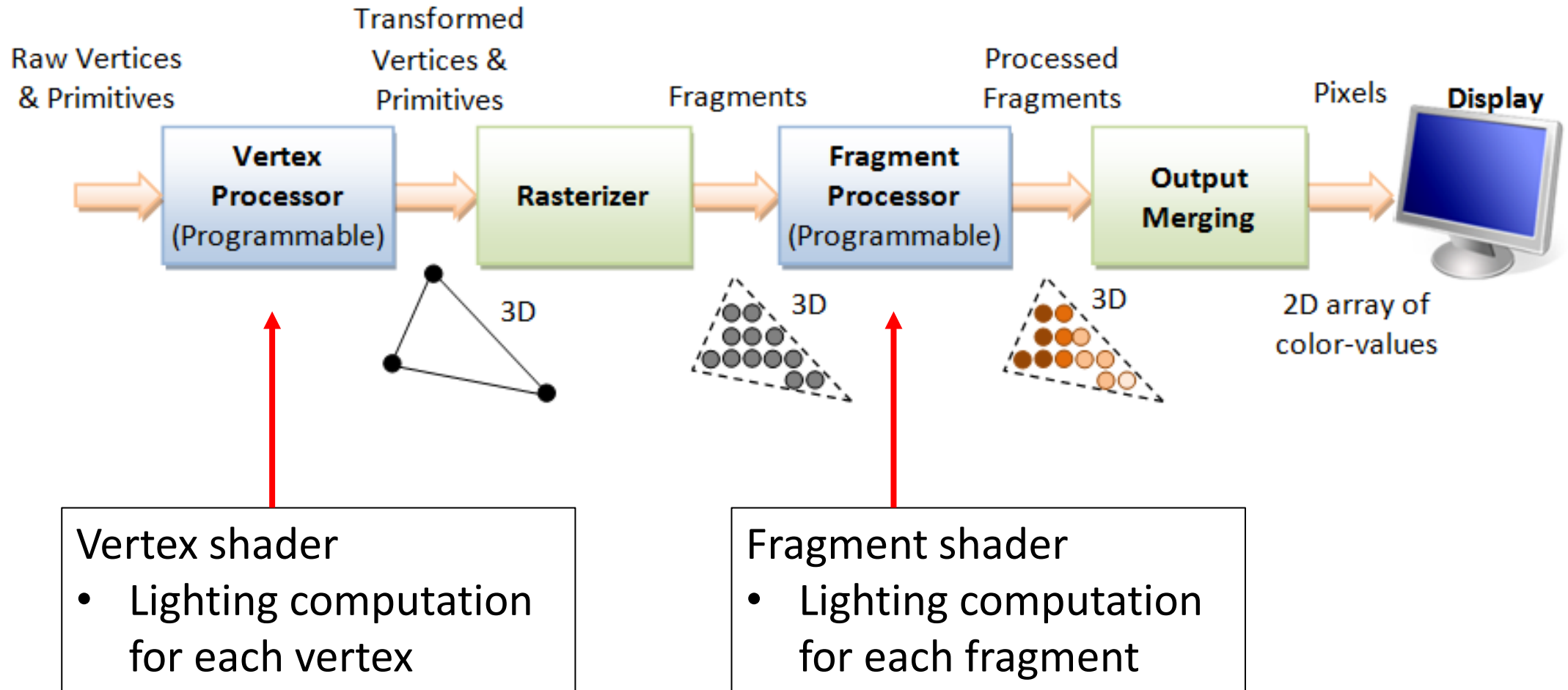


Phong Shading



<http://www.decew.net/OSS/timeline.php>

Shader

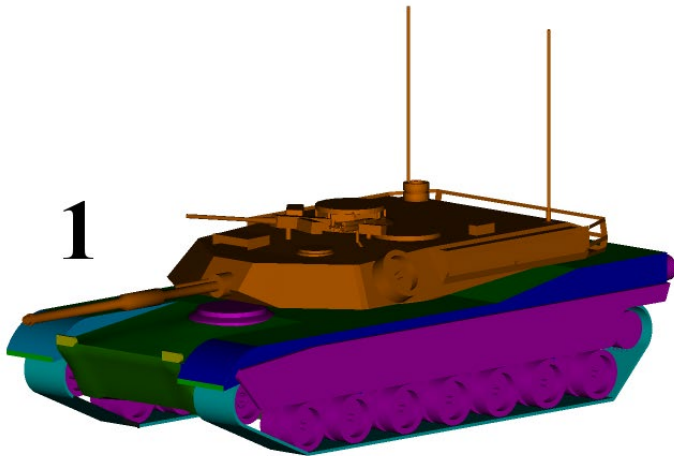


Shader

- Shaders are small programs that are executed in parallel on GPUs for each vertex (vertex shader) or each fragment (fragment shader)
- Vertex shader (before rasterization)
 - Modelview projection transform of vertex and normal
 - If per-vertex lighting, compute lighting for each vertex
- Fragment shader (after rasterization)
 - If per-vertex lighting, assign color to each fragment
 - If per-fragment lighting, compute lighting for each fragment

Texture Mapping

- Map textures (2D images) to 3D models



Without texture

- Need to specify vertex colors

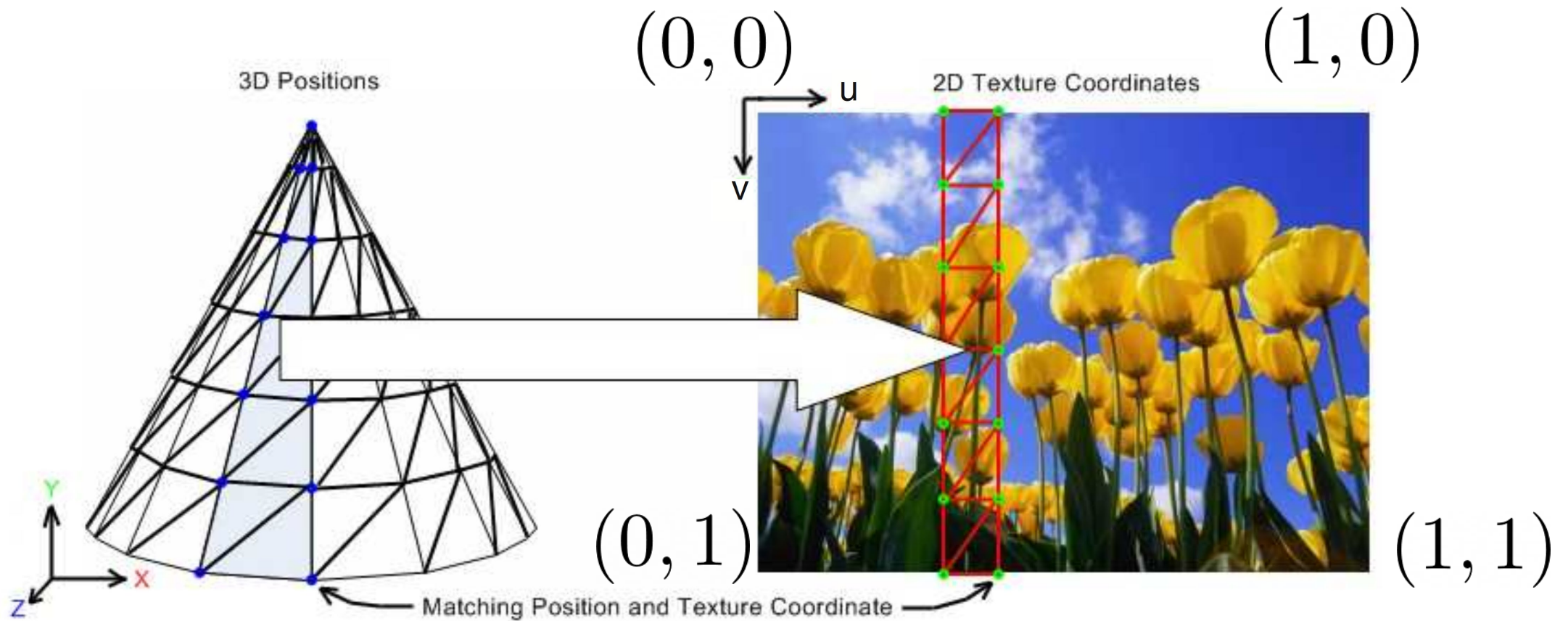


With texture

- Vertex colors from texture

Texture Mapping

- UV coordinates (normalized)

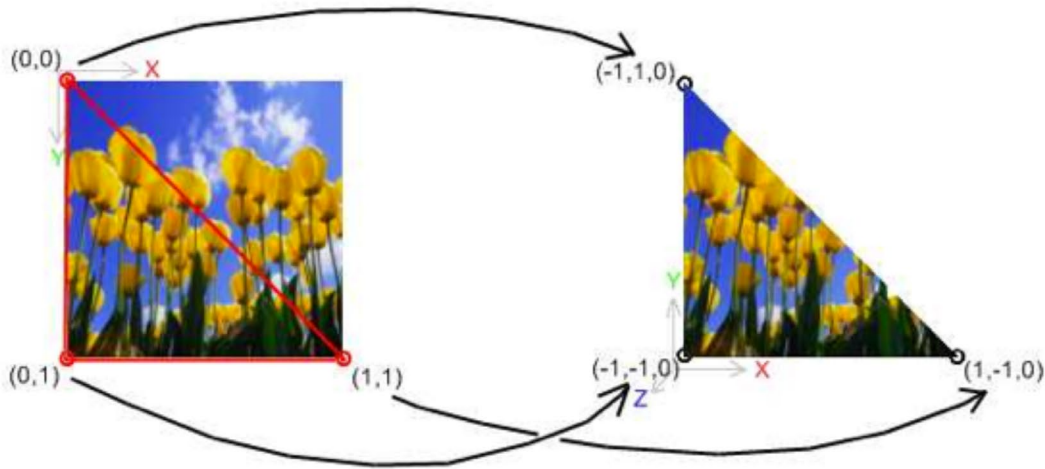


Texture Mapping

- Same texture, different UV coordinates for mapping

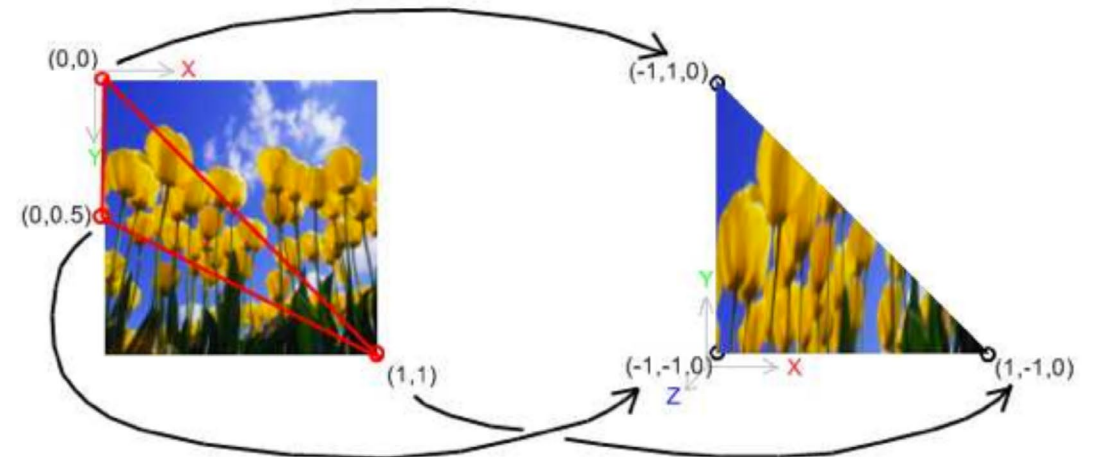
Texture Coordinates

Rendered Triangle



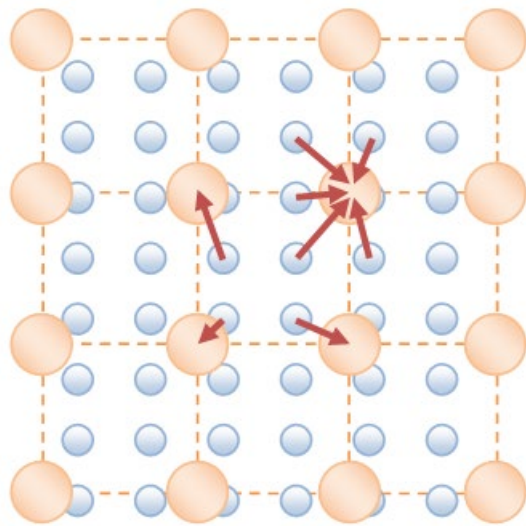
Texture Coordinates

Rendered Triangle

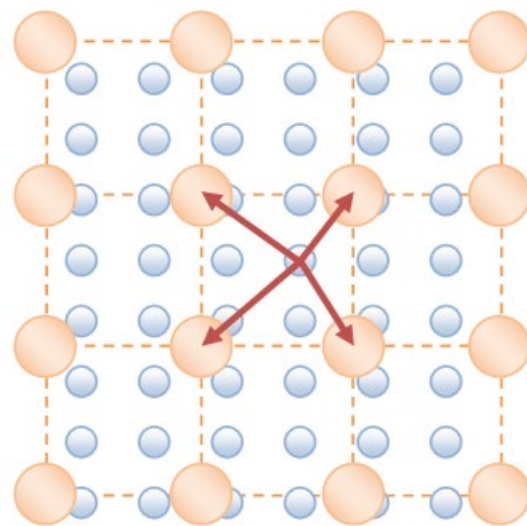


Texture Mapping

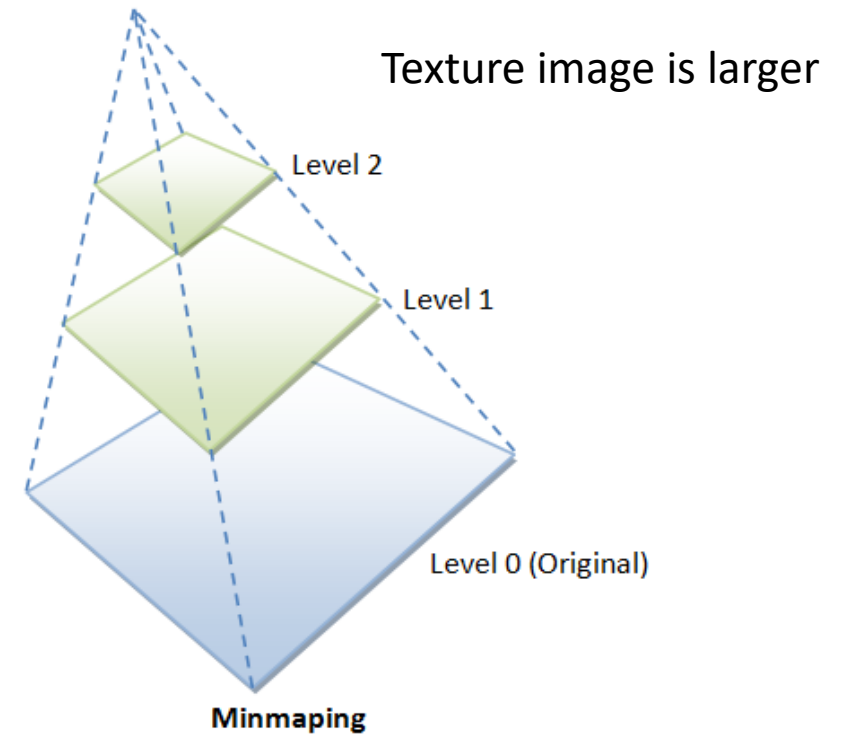
- Texture filtering: the resolution of the texture image is different from the displayed fragment
 - Magnification
 - Minification



Magnification – Nearest Point Sampling



Magnification – Bilinear Interpolation

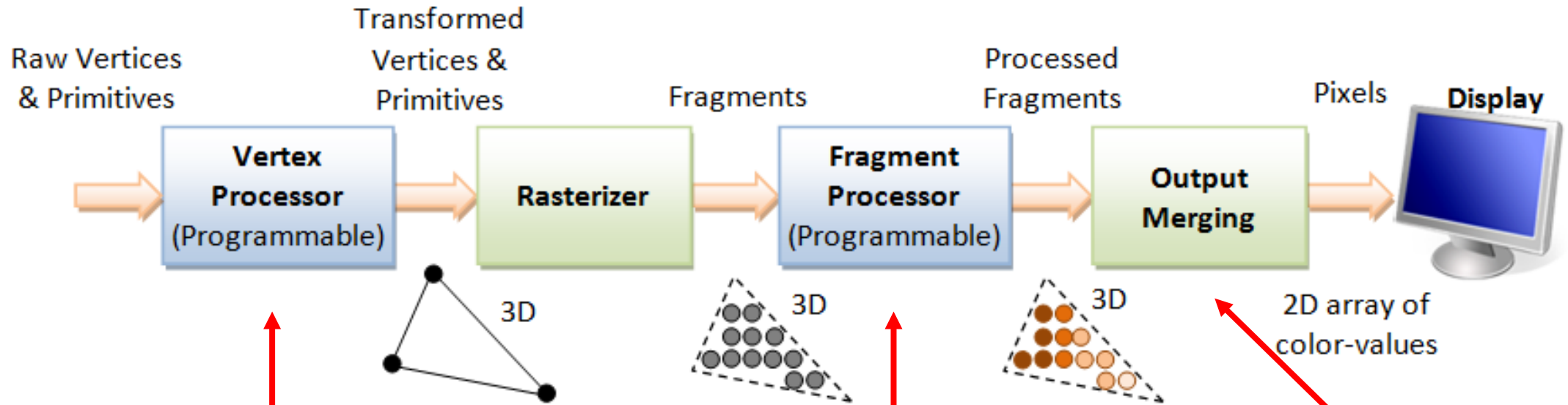


Minmapping

Texture Mapping



Review of the Graphics Pipeline



Vertex shader

- Vertex transforms
- Per-vertex lighting

Fragment shader

- Texturing
- Per-fragment lighting

Combine the fragments of all primitives into 2D color-pixel for display

Further Reading

- 3D graphics with OpenGL, Basic Theory
https://www3.ntu.edu.sg/home/ehchua/programming/opengl/CG_BasicsTheory.html
- Textbook: Shirley and Marschner “Fundamentals of Computer Graphics”, AK Peters, 2009