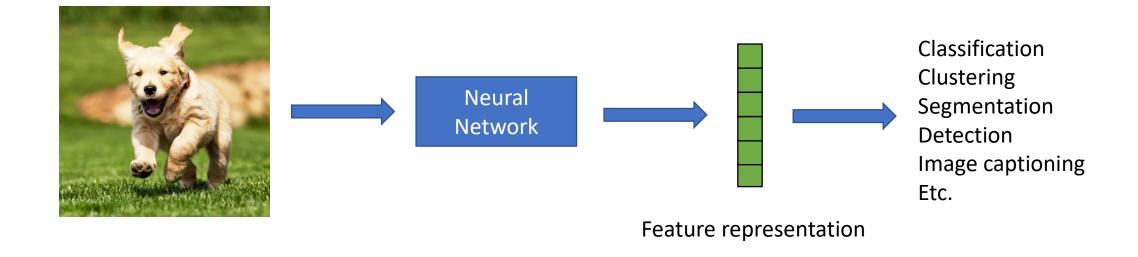


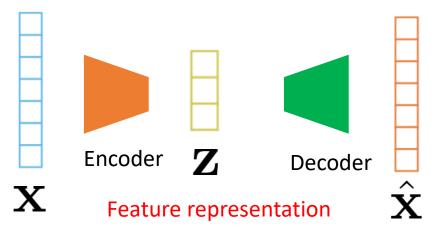
CS 6384 Computer Vision
Professor Yu Xiang
The University of Texas at Dallas

# Learning Visual Representations

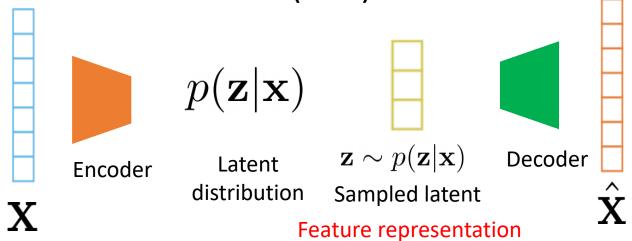


#### Generative Models

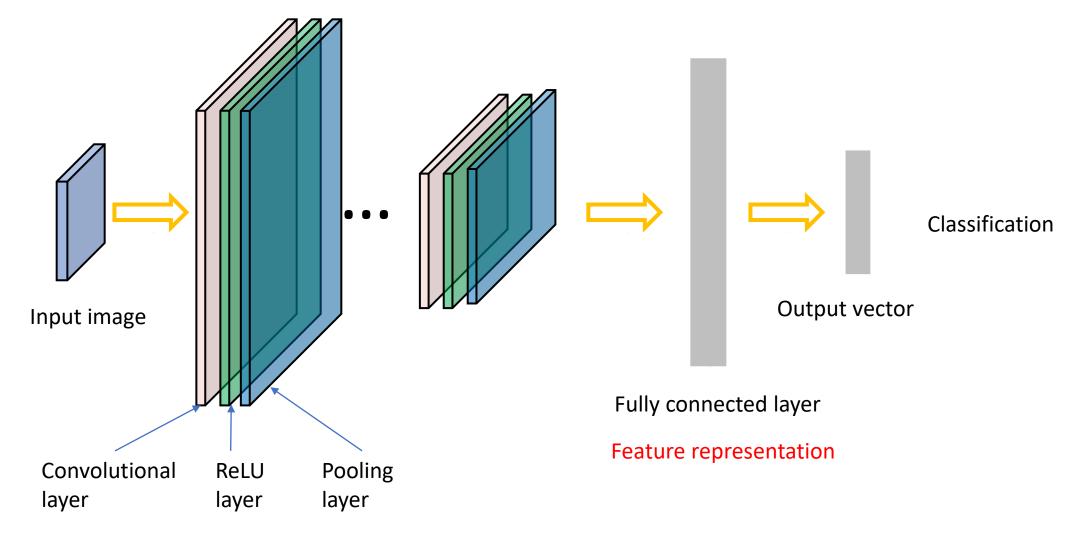
Autoencoder



Variational Autoencoder (VAE)



# Discriminative Models (Supervised Learning)

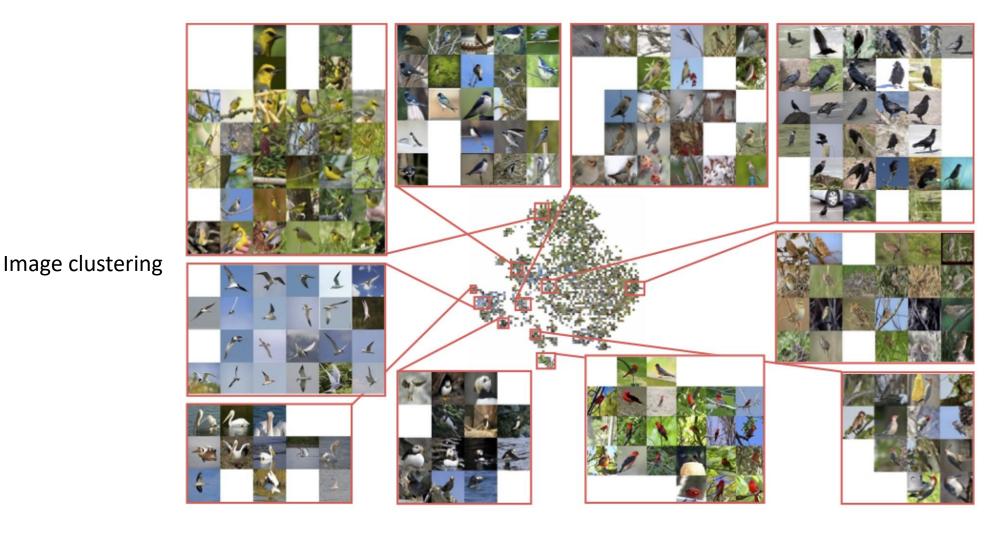


- Train neural networks for image classification
- Use internal features in the network as feature representations
- Applications



Image retrieval

Deep Metric Learning via Lifted Structured Feature Embedding. Song et al., CVPR, 2016.



t-Distributed Stochastic Neighbor Embedding (t-SNE)

L.J.P. van der Maaten and G.E. Hinton. **Visualizing High-Dimensional Data Using t-SNE**. *Journal of Machine Learning Research* 9(Nov):2579-2605, 2008.

Deep Metric Learning via Lifted Structured Feature Embedding. Song et al., CVPR, 2016.

- Training with classification loss functions
  - E.g., cross-entropy loss

Can we have better loss functions for representation learning?

- Deep metric learning
  - Learning distance metrics with neural networks

### Distance metrics

• L1 distance

$$D(\mathbf{x}, \mathbf{y}) = \sum_{i=1}^{N} |x_i - y_i|$$

• L2 distance

$$D(\mathbf{x}, \mathbf{y}) = \sqrt{\sum_{i=1}^{N} (x_i - y_i)^2}$$

Cosine distance

$$D(\mathbf{x}, \mathbf{y}) = 1 - \frac{\mathbf{x} \cdot \mathbf{y}}{\|\mathbf{x}\| \|\mathbf{y}\|}$$
Cosine similarity

## Deep Metric Learning



Feature representation

$$D(\mathbf{x}_1, \mathbf{x}_2) = D(f(\mathbf{x}_1), f(\mathbf{x}_2))$$

L2 distance 
$$D(\mathbf{x}_1,\mathbf{x}_2) = \|f(\mathbf{x}_1) - f(\mathbf{x}_2)\|_2$$

Learning the distance metric is equivalent to learning the feature representation

#### Contrastive Loss

Use positive pairs and negative pairs





Positive pair  $f(\mathbf{x}_1)$   $f(\mathbf{x}_2)$  should be close

$$D(\mathbf{x}_1,\mathbf{x}_2)$$
 small

Negative pair  $f(\mathbf{x}_1)$   $f(\mathbf{x}_2)$  should be far

$$D(\mathbf{x}_1,\mathbf{x}_2)$$
 large

Learning a Similarity Metric Discriminatively, with Application to Face Verification. Chopra et al., CVPR, 2005.

### Contrastive Loss

• Training data  $\{(\mathbf{x}_i, \mathbf{x}_j, y_{ij})\}$   $y_{ij} = \begin{cases} 1 & \text{if positive pair} \\ 0 & \text{if negative pair} \end{cases}$ 

(a) Contrastive embedding

$$J = \frac{1}{m} \sum_{(i,j)}^{m/2} y_{i,j} D_{i,j}^2 + (1-y_{i,j}) \left[\alpha - D_{i,j}\right]_+^2$$
 
$$[x]_+ = \max(0,x)$$
 m: number of images in a batch

m: number of images in a batch

Learning a Similarity Metric Discriminatively, with Application to Face Verification. Chopra et al., CVPR, 2005.

#### Contrastive Loss

• Compute Gradient 
$$J=rac{1}{m}\sum_{(i,j)}^{m/2}y_{i,j}D_{i,j}^2+\left(1-y_{i,j}
ight)\left[lpha-D_{i,j}
ight]_+^2$$

$$\frac{\partial J}{\partial D_{i,j}} = \frac{2}{m} (y_{i,j} D_{i,j} - (1 - y_{i,j}) [\alpha - D_{i,j}]_{+})$$

$$D_{i,j} = \|f(\mathbf{x}_i) - f(\mathbf{x}_j)\|_2 \qquad \frac{\partial D_{i,j}}{\partial f(\mathbf{x}_i)} = \frac{f(\mathbf{x}_i) - f(\mathbf{x}_j)}{\|f(\mathbf{x}_i) - f(\mathbf{x}_j)\|}$$

$$\mathbf{x}_i \longrightarrow \frac{\text{Neural Network}}{\text{Network}} \longrightarrow f(\mathbf{x}_i)$$

Gradients
$$\frac{\partial J}{\partial f(\mathbf{x}_i)}$$

## Triplet Loss

Use a triplet (anchor, positive, negative)



(b) Triplet embedding

$$J = \frac{3}{2m} \sum_{i}^{m/3} \left[ D_{ia,ip}^2 - D_{ia,in}^2 + \alpha \right]_{+}$$

$$D_{ia,ip} = ||f(\mathbf{x}_i^a) - f(\mathbf{x}_i^p)||$$
  $D_{ia,in} = ||f(\mathbf{x}_i^a) - f(\mathbf{x}_i^n)||$ 

FaceNet: A Unified Embedding for Face Recognition and Clustering. Schroff et al., CVPR, 2015.

## Lifted Structured Loss

Consider all positive pairs and negative pairs in a mini-batch

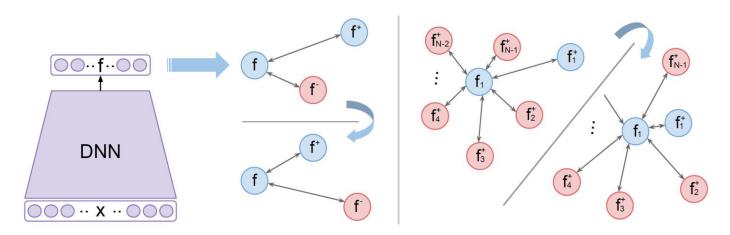
$$J = \frac{1}{2|\widehat{\mathcal{P}}|} \sum_{(i,j) \in \widehat{\mathcal{P}}} \max \left(0,\ J_{i,j}\right)^2$$
 
$$J_{i,j} = \max \left(\max_{(i,k) \in \widehat{\mathcal{N}}} \alpha - D_{i,k}, \max_{(j,l) \in \widehat{\mathcal{N}}} \alpha - D_{j,l}\right) + D_{i,j}$$
 
$$\max_{\mathbf{x}_1} \alpha - D_{i,k}, \max_{\mathbf{x}_2} \alpha - D_{j,l}\right) + D_{i,j}$$
 
$$\max_{(c) \text{ Lifted structured embedding}} \mathbf{x}_{i}$$
 
$$\max_{\mathbf{x}_2 \in \mathbf{x}_3 \in \mathbf{x}_4 \in \mathbf{x}_5} \mathbf{x}_{i}$$
 
$$\max_{(c) \text{ Lifted structured embedding}} \mathbf{x}_{i}$$
 Relaxed loss 
$$\tilde{J}_{i,j} = \log \left(\sum_{(i,k) \in \mathcal{N}} \exp\{\alpha - D_{i,k}\} + \sum_{(j,l) \in \mathcal{N}} \exp\{\alpha - D_{j,l}\}\right) + D_{i,j}$$

Deep Metric Learning via Lifted Structured Feature Embedding. Song et al., CVPR, 2016.

# Multi-class N-pair Loss

• Use a positive pair and N-1 negative ones and  $\{\mathbf{x},\mathbf{x}^+,\mathbf{x}_1^-,\ldots,\mathbf{x}_{N-1}^-\}$ 

$$\begin{split} \mathcal{L}_{\text{N-pair}}(\mathbf{x}, \mathbf{x}^+, \{\mathbf{x}_i^-\}_{i=1}^{N-1}) &= \log \left(1 + \sum_{i=1}^{N-1} \exp(f(\mathbf{x})^\top f(\mathbf{x}_i^-) - f(\mathbf{x})^\top f(\mathbf{x}^+))\right) \\ &= -\log \frac{\exp(f(\mathbf{x})^\top f(\mathbf{x}^+))}{\exp(f(\mathbf{x})^\top f(\mathbf{x}^+)) + \sum_{i=1}^{N-1} \exp(f(\mathbf{x})^\top f(\mathbf{x}_i^-))} \quad & \text{Softmax for multi-class classification} \end{split}$$



Improved Deep Metric Learning with Multi-class N-pair Loss Objective. Kihyuk Sohn, NeurIPS, 2016

# InfoNCE (Noise Contrastive Estimation) Loss

• Similar to multi-class N-pair Loss

$$\mathcal{L}_q = -\log \frac{\exp(q \cdot k_+ / \tau)}{\sum_{i=0}^K \exp(q \cdot k_i / \tau)}$$

Query q

Positive k+

(K+1)-way softmax classification

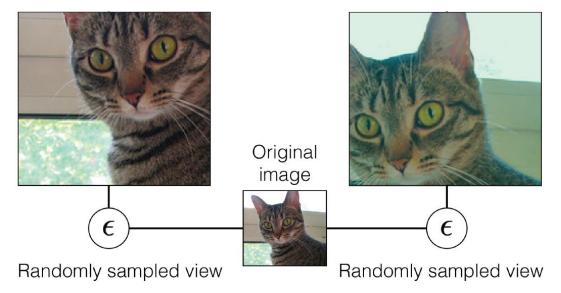
Negatives ki

Motivated from identifying targets from noisy data

Use class labels to specify positive pairs and negative pairs

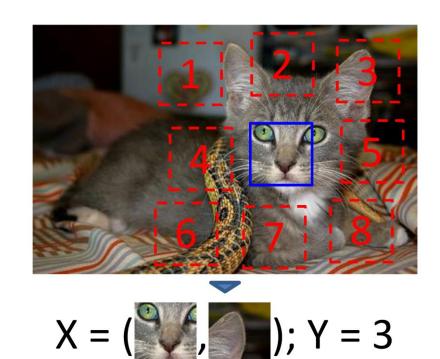
- Loss functions
  - Contrastive loss
  - Triplet loss
  - Lifted structured loss
  - N-pair loss
  - InfoNCE
- Consider more relationships in a mini-batch is better

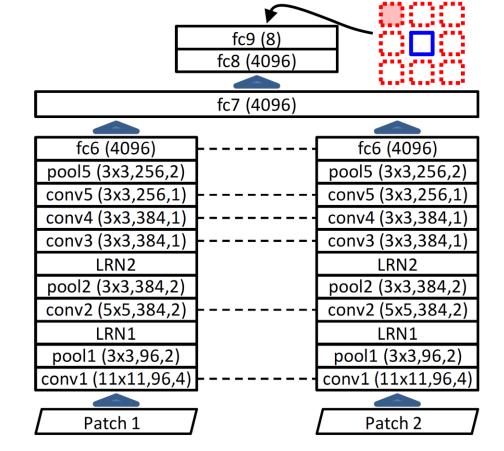
- Pretext tasks
  - Tasks designed for feature learning
  - Not the final tasks
- Positive pairs from different views of the same image



Learning Representations by Maximizing Mutual Information Across Views. Bachman et al., NeurIPS, 2019

Pretext task: context prediction

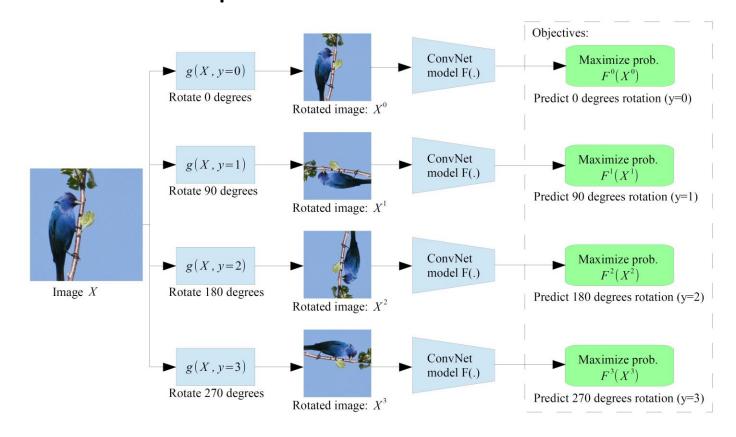




Feature representation

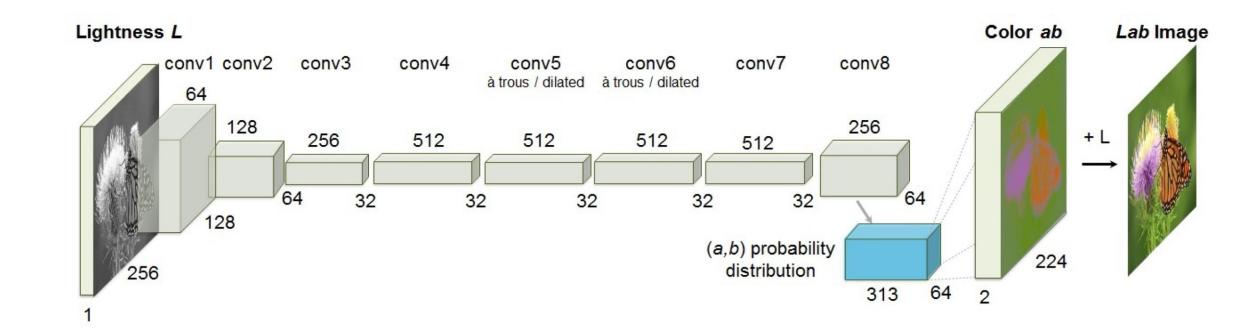
Unsupervised Visual Representation Learning by Context Prediction. Doersch, et al., ICCV, 2015

Pretext task: rotation prediction



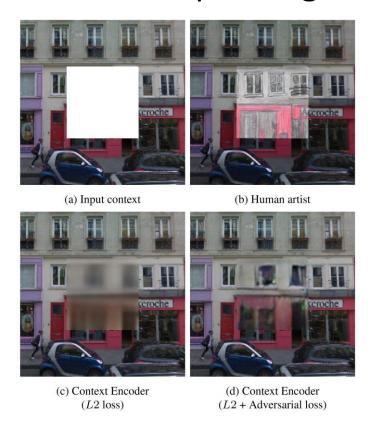
Unsupervised Representation Learning by Predicting Image Rotations. Gidaris, et al., ICLR, 2018

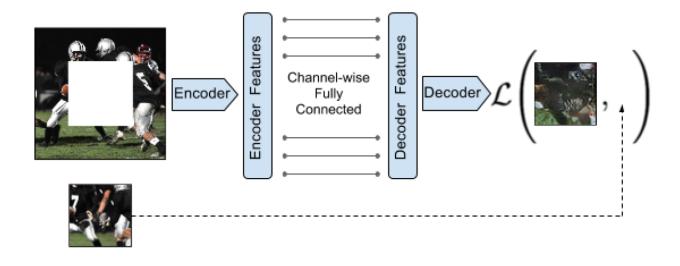
Pretext task: colorization



Colorful Image Colorization. Zhang, et al., ECCV, 2016

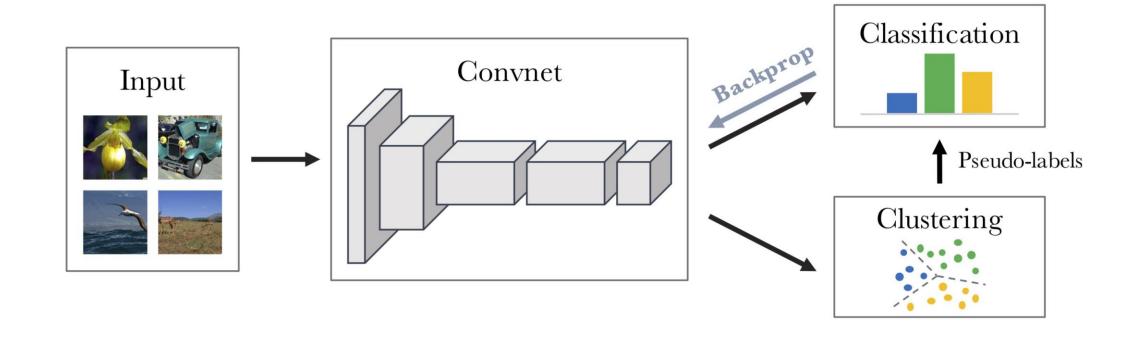
Pretext task: inpainting





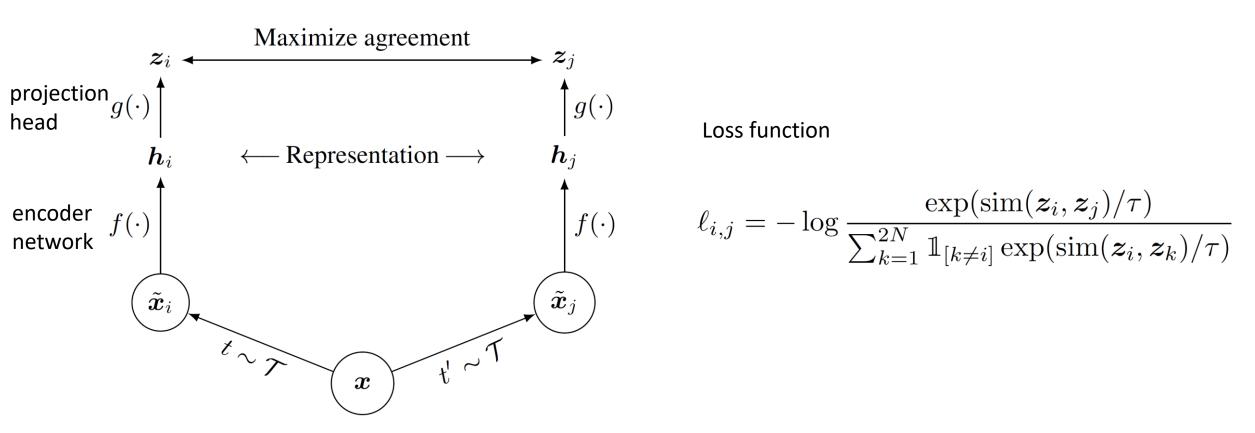
Context Encoders: Feature Learning by Inpainting. Pathak, et al., CVPR, 2016

Pretext task: clustering



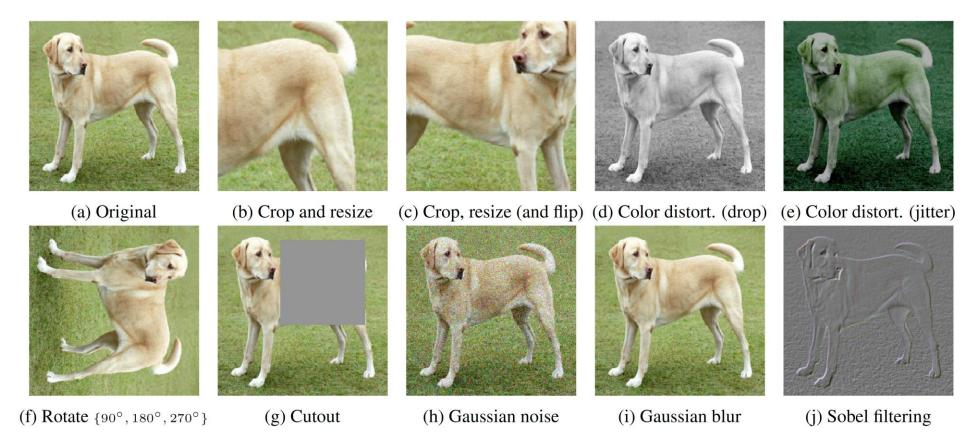
Deep Clustering for Unsupervised Learning of Visual Features. Caron et al., ECCV, 2018

• A simple framework for contrastive learning of visual representations



A Simple Framework for Contrastive Learning of Visual Representations. Chen et al., ICML, 2020

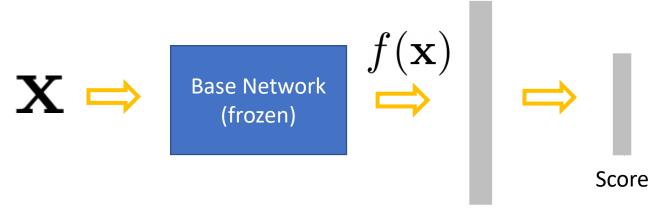
#### Transformations



A Simple Framework for Contrastive Learning of Visual Representations. Chen et al., ICML, 2020

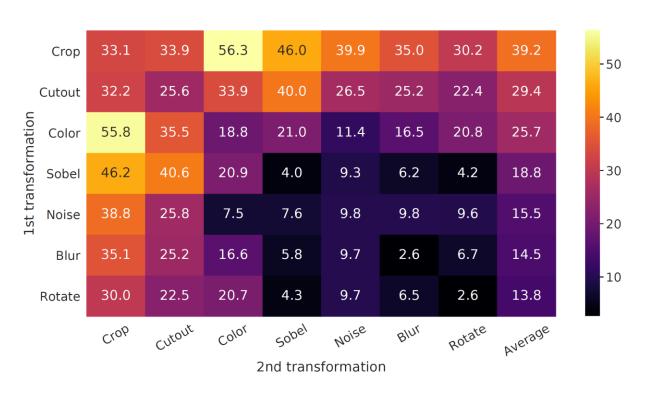
• After training, keep the encoder network  $h_i = f(\tilde{x}_i) = \text{ResNet}(\tilde{x}_i)$ 

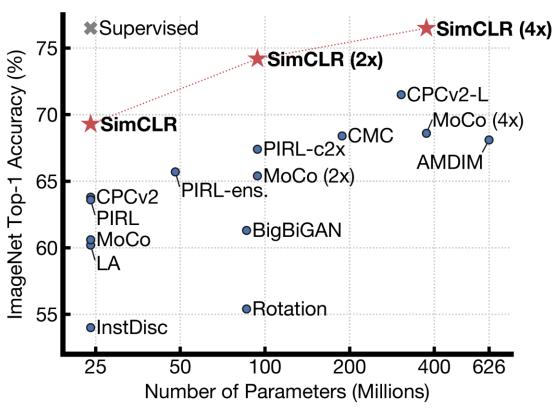
- Linear evaluation protocol for classification
  - A linear classifier is trained on top of the frozen base network



Fully connected layer

A Simple Framework for Contrastive Learning of Visual Representations. Chen et al., ICML, 2020





ImageNet top-1 accuracy

2x, 4x: more channels in ResNet

A Simple Framework for Contrastive Learning of Visual Representations. Chen et al., ICML, 2020

4/7/2023

https://github.com/google-research/simclr

# Summary: Visual Representation Learning

- Generative models
  - Autoencoder
  - VAE
- Discriminative models
  - Supervised learning
    - Training with image classification
    - Deep metric learning
  - Unsupervised/self-supervised learning
    - Use pretext tasks
    - Metric learning loss functions

## Further Reading

- Learning a Similarity Metric Discriminatively, with Application to Face Verification, 2005 <a href="http://yann.lecun.com/exdb/publis/pdf/chopra-05.pdf">http://yann.lecun.com/exdb/publis/pdf/chopra-05.pdf</a>
- FaceNet: A Unified Embedding for Face Recognition and Clustering, 2015 https://arxiv.org/abs/1503.03832
- Deep Metric Learning via Lifted Structured Feature Embedding, 2016 https://arxiv.org/abs/1511.06452
- Improved Deep Metric Learning with Multi-class N-pair Loss Objective, 2016 <a href="https://papers.nips.cc/paper/2016/file/6b180037abbebea991d8b1232f8a8ca9-Paper.pdf">https://papers.nips.cc/paper/2016/file/6b180037abbebea991d8b1232f8a8ca9-Paper.pdf</a>
- Learning Representations by Maximizing Mutual Information Across Views, 2019 <a href="https://arxiv.org/pdf/1906.00910.pdf">https://arxiv.org/pdf/1906.00910.pdf</a>
- A Simple Framework for Contrastive Learning of Visual Representations, 2020 <a href="https://arxiv.org/abs/2002.05709">https://arxiv.org/abs/2002.05709</a>