# Keypoint Features II

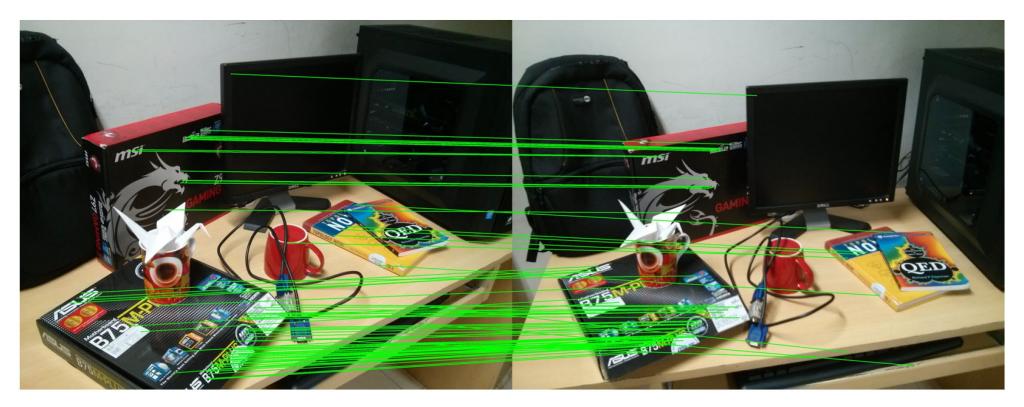
CS 6384 Computer Vision Professor Yu Xiang The University of Texas at Dallas

Some slides of this lecture are courtesy Kris Kitani

EST. 1969

UNIN

# Feature Detection and Matching

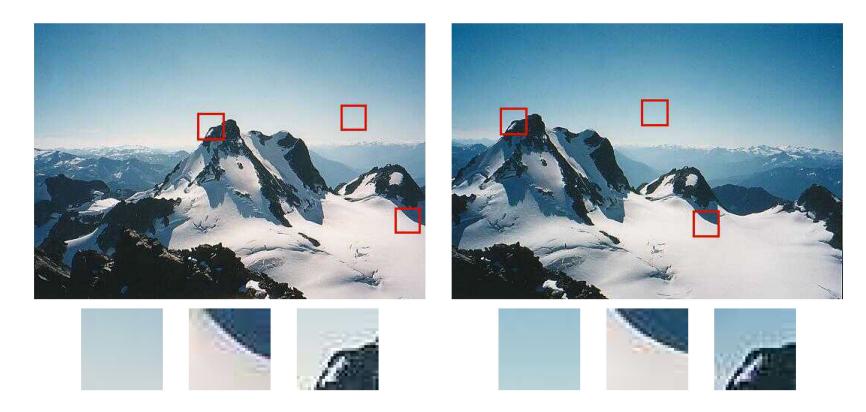


Geometry-aware Feature Matching for Structure from Motion Applications. Shah et al, WACV'15

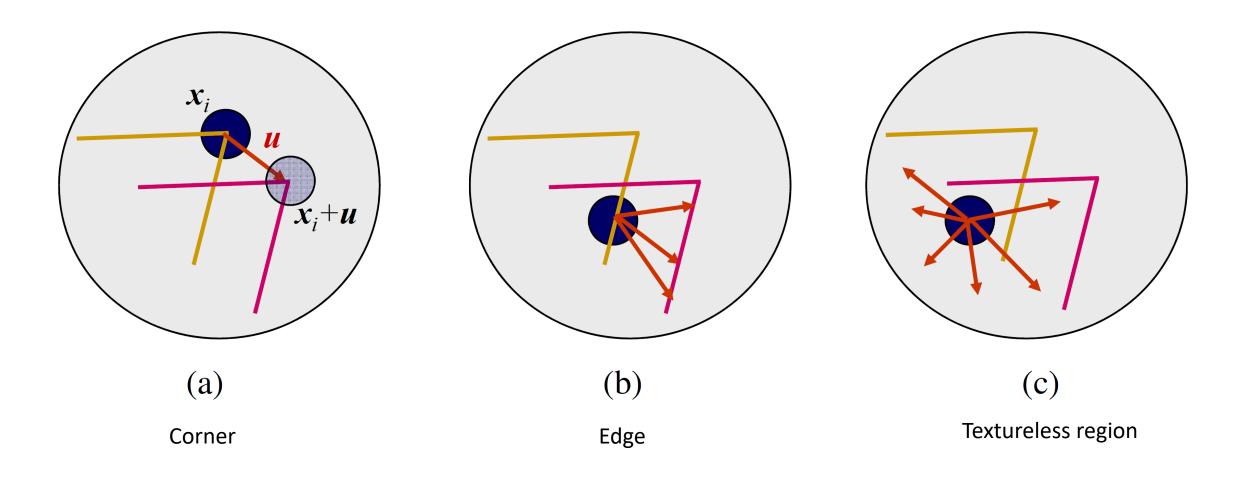
Applications: stereo matching, image stitching, 3D reconstruction, camera pose estimation, object recognition

#### Feature Detectors

 How to find image locations that can be reliably matched with images?



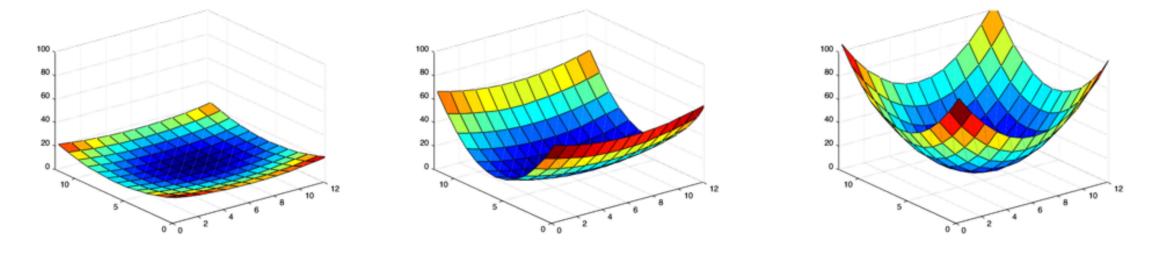
#### Feature Detectors



#### Harris Corner Detector

$$f(\Delta x, \Delta y) \approx \sum_{x,y} w(x,y) (I_x(x,y)\Delta x + I_y(x,y)\Delta y)^2$$

$$f(\Delta x, \Delta y) \approx (\Delta x \quad \Delta y) M\begin{pmatrix}\Delta x\\\Delta y\end{pmatrix} \qquad M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y\\I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} \sum_{x,y} w(x,y) I_x^2 & \sum_{x,y} w(x,y) I_x I_y\\\sum_{x,y} w(x,y) I_x I_y & \sum_{x,y} w(x,y) I_y^2 \end{bmatrix}$$



Flat

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Edge

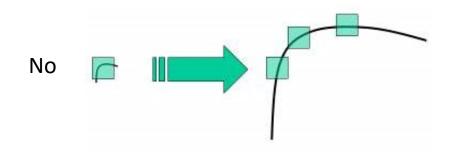
Yu Xiang

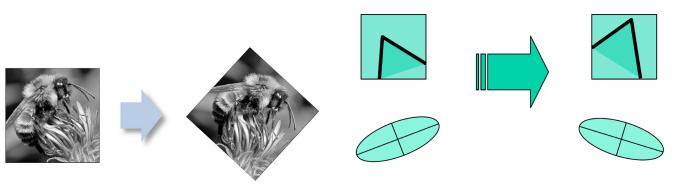
Corner

#### Invariance

- Can the same feature point be detected after some transformation?
  - Translation invariance Are Harris corners translation invariance?
  - 2D rotation invariance Are Harris corners rotation invariance?
  - Scale invariance

Are Harris corners scale invariance?









# Scale Invariance

• Solution 1: detection features in all scales, matching features in corresponding scale (for small scale change)

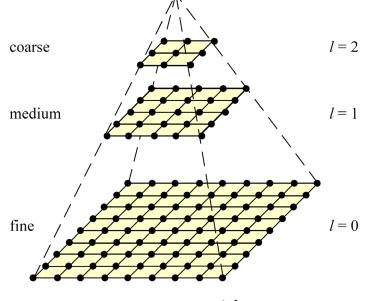
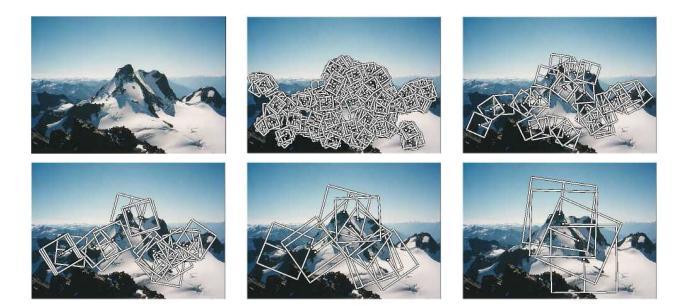


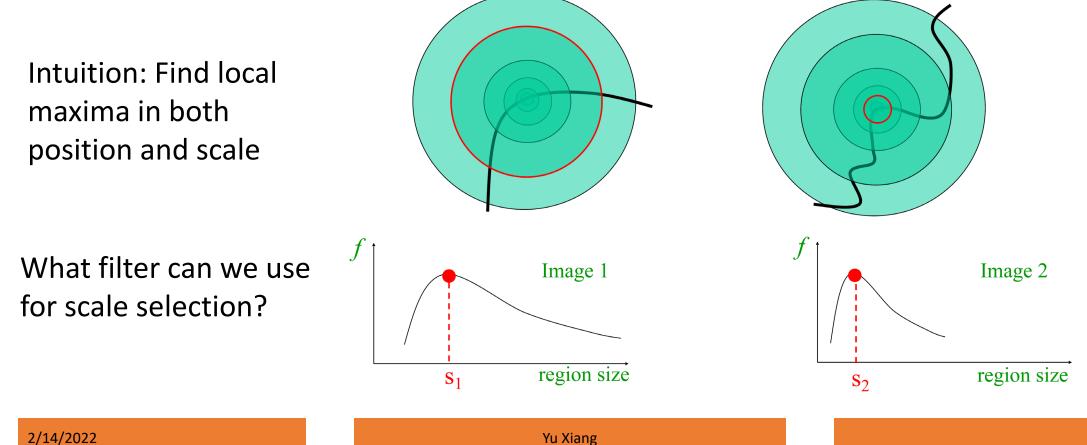
Image pyramid



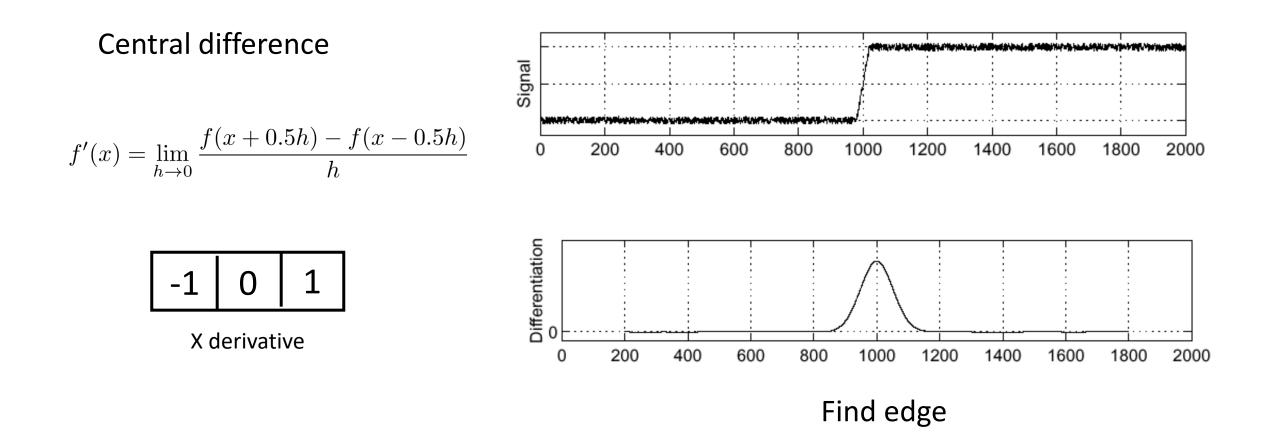
Multi-scale oriented patches (MOPS) extracted at five pyramid levels (Brown, Szeliski, and Winder 2005)

# Scale Invariance

Solution 2: detect features that are stable in both location and scale

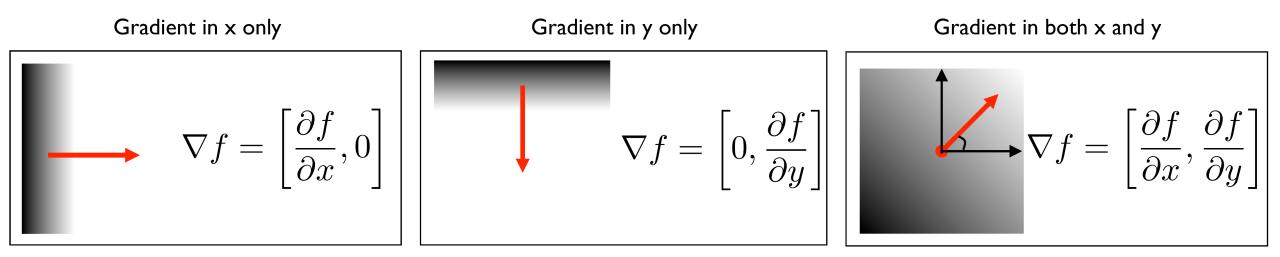


#### **Recall Derivative Filter**



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#### Image Gradient



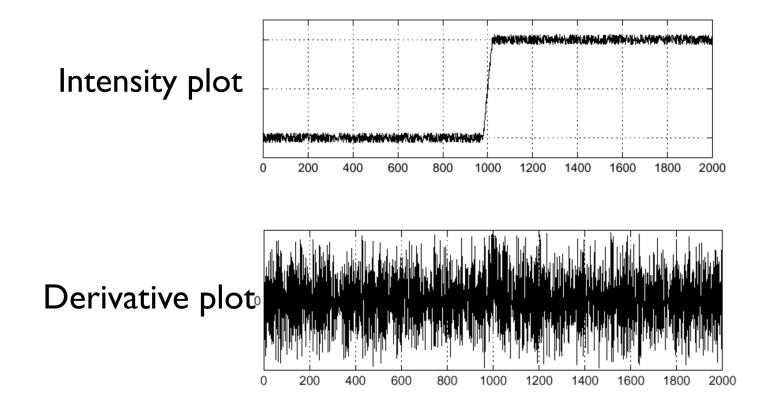
Gradient direction

$$\theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$$

**Gradient magnitude**  
$$\nabla f || = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

# Signal Noises

• Derivative filters are sensitive to noises



How to deal with noises?

#### Gaussian Filter

• Smoothing

$$1D \quad g(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2}{2\sigma^2}}$$

$$g(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$g(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$Gaussian Filter h$$

$$g(x) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$Gaussian Filter h$$

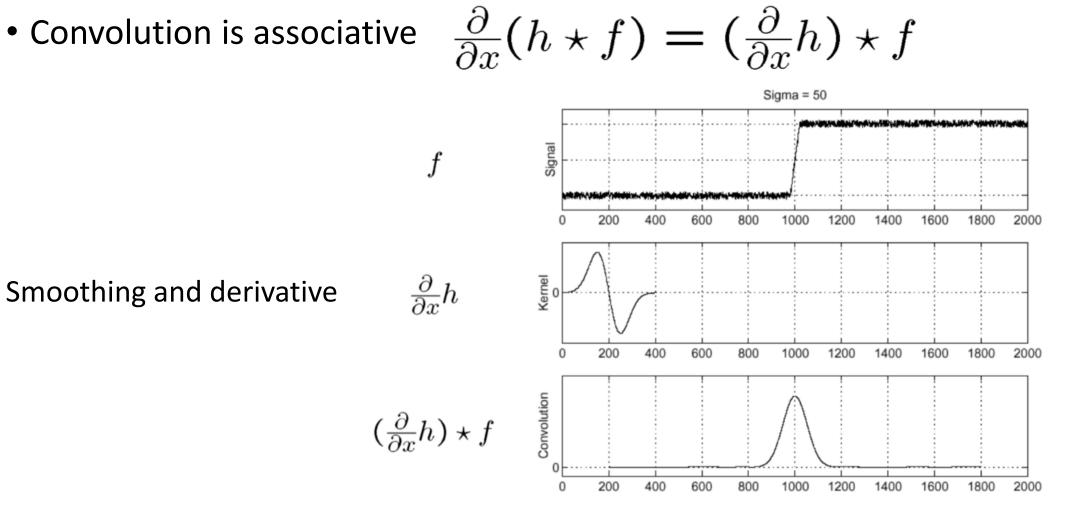
$$Gaussi$$

Sigma = 50

-2.0 0.0

2.0

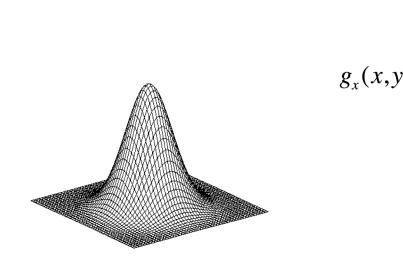
#### Derivative of Gaussian Filter



Smoothing and derivative

#### Derivative of Gaussian Filter

• Convolution is associative  $\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$ 



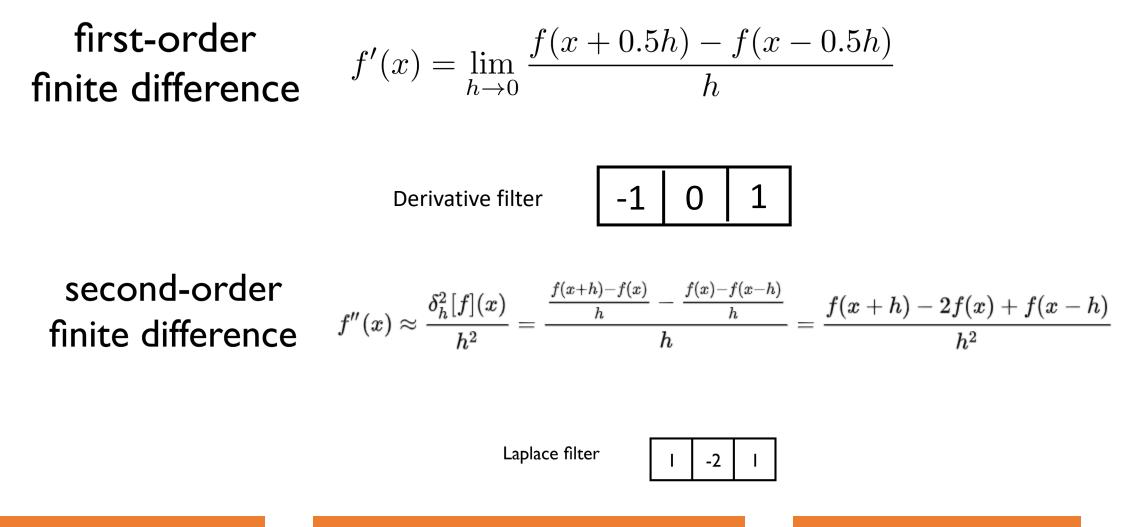
 $g_{x}(x,y) = \frac{\partial g(x,y)}{\partial x} = \frac{-x}{2\pi\sigma^{4}}e^{-\frac{x^{2}+y^{2}}{2\sigma^{2}}} \qquad g_{y}(x,y) = \frac{\partial g(x,y)}{\partial y} = \frac{-y}{2\pi\sigma^{4}}e^{-\frac{x^{2}+y^{2}}{2\sigma^{2}}}$ 

Gaussian

$$g(x,y) = rac{1}{2\pi\sigma^2} e^{-rac{x^2+y^2}{2\sigma^2}}$$



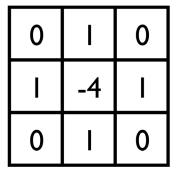
#### Laplace Filter



#### Laplace Filter

• 2D  $\nabla^2 \mathbf{I} = \frac{\partial^2 \mathbf{I}}{\partial x^2} + \frac{\partial^2 \mathbf{I}}{\partial y^2}$ 





ID Laplace filter

2D Laplace filter

# Laplacian of Gaussian Filter

$$\nabla^2 \mathbf{I} = \frac{\partial^2 \mathbf{I}}{\partial x^2} + \frac{\partial^2 \mathbf{I}}{\partial y^2}$$
$$\nabla^2 \mathbf{I} \circ g = \nabla^2 g \circ \mathbf{I}$$
$$\nabla^2 g = \frac{x^2 + y^2 - 2\sigma^2}{\sigma^4} g(x, y)$$

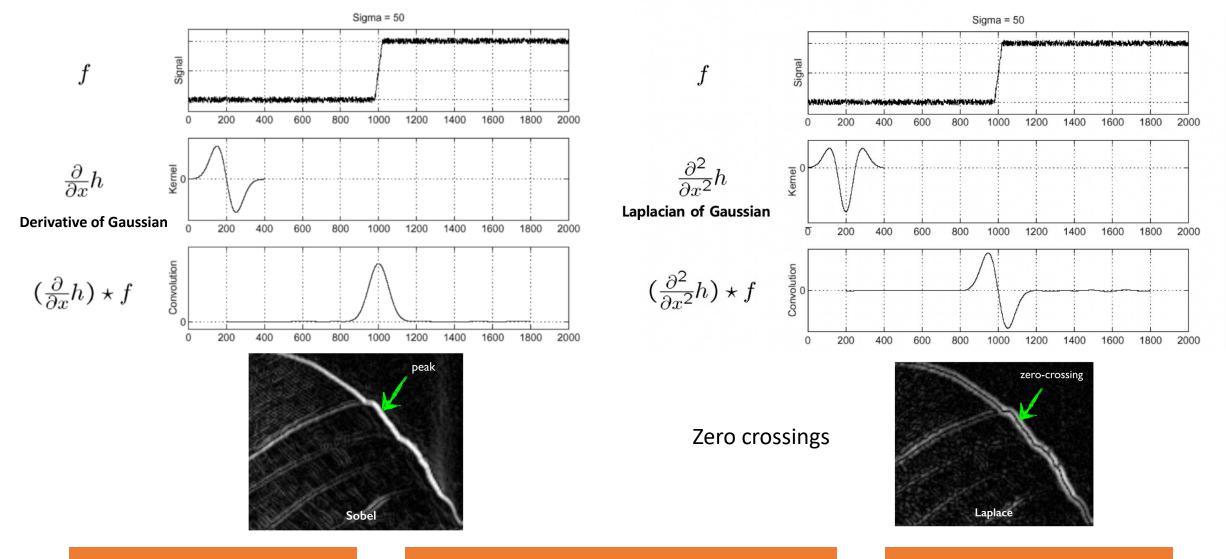
 $\nabla^2 h_\sigma(u,v)$ 

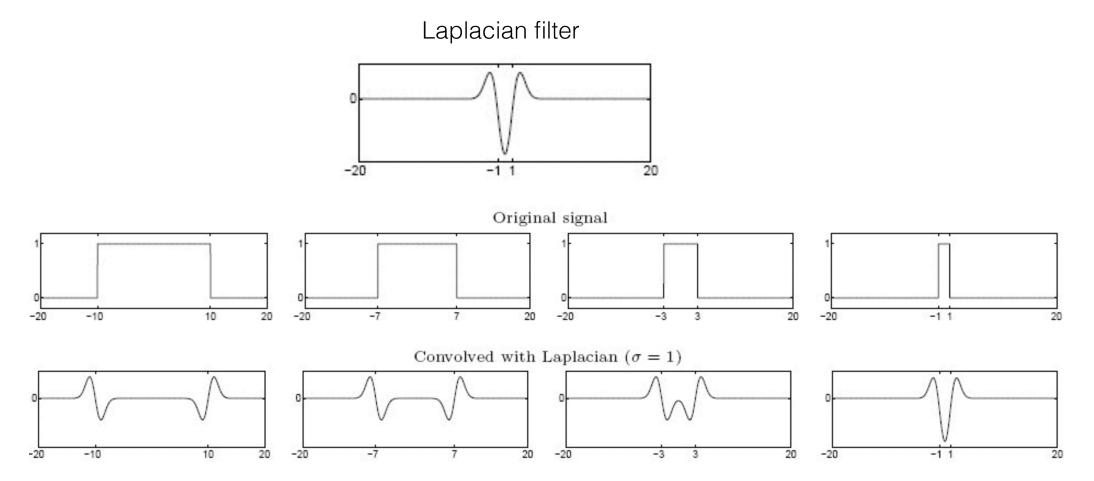


Laplacian of Gaussian

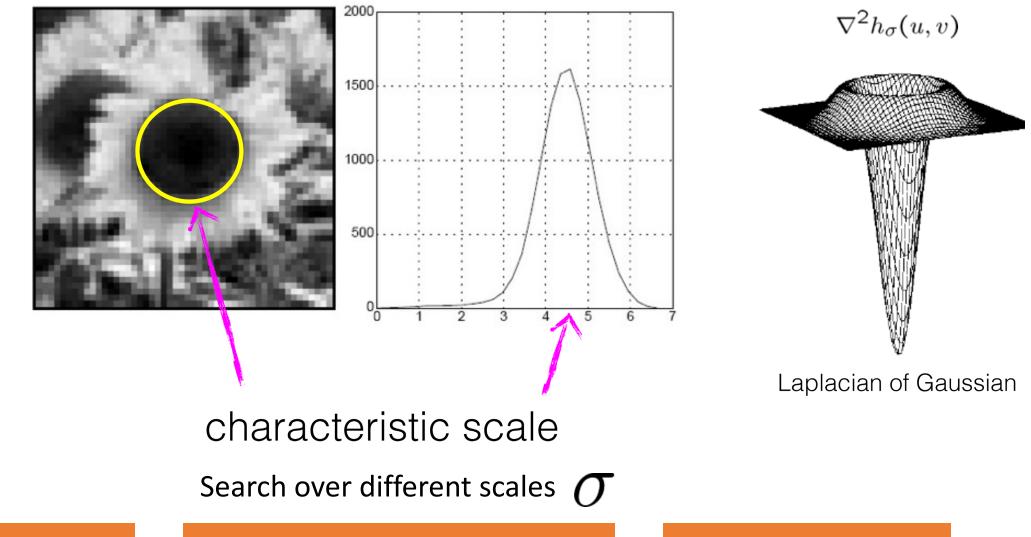
Smoothing and second derivative

#### Laplacian of Gaussian Filter

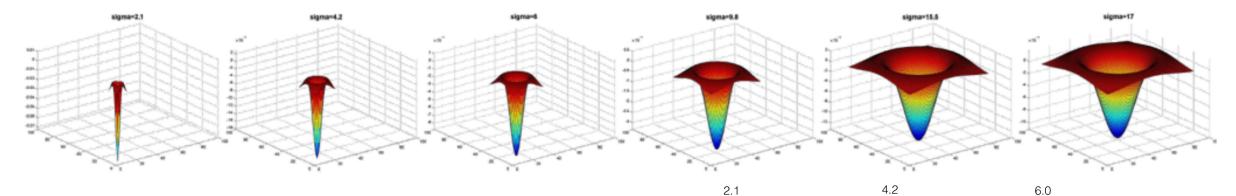




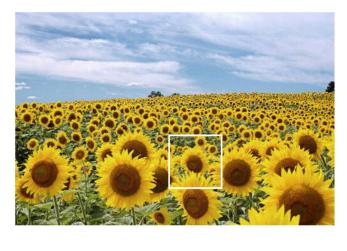
Highest response when the signal has the same **characteristic scale** as the filter

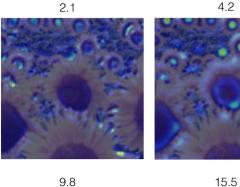


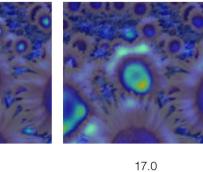
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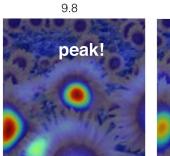


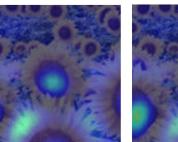
Multi-scale 2D Blob detection



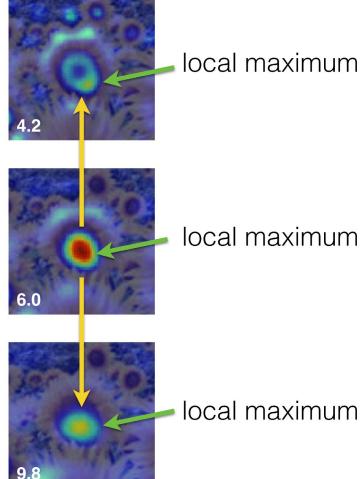










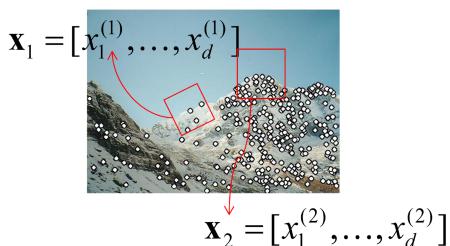


local maximum

cross-scale maximum

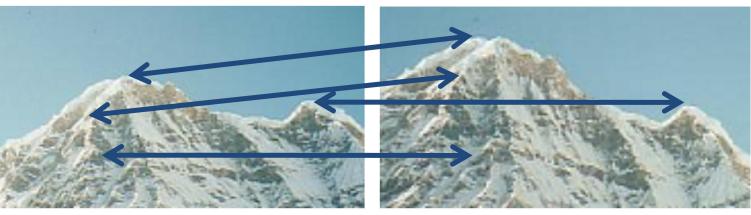
# Scale Invariance Feature Transform (SIFT)

• Keypoint detection



• Compute descriptors

• Matching descriptors



David Lowe, Distinctive Image Features from Scale-Invariant Keypoints. IJCV, 2004

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#### SIFT: Scale-space Extrema Detection

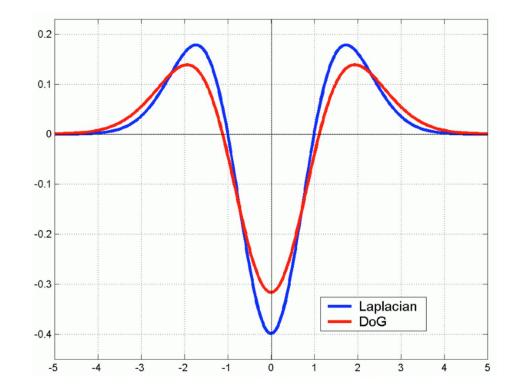
• Difference of Gaussian (DoG)

$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2 + y^2)/2\sigma^2}$$

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

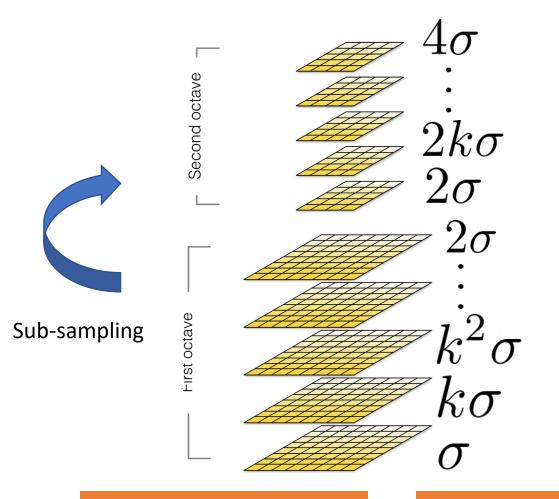
$$D(x, y, \sigma) = (G(x, y, k\sigma) - G(x, y, \sigma)) * I(x, y)$$
  
=  $L(x, y, k\sigma) - L(x, y, \sigma).$ 

Approximate of Laplacian of Gaussian (efficient to compute)



# SIFT: Scale-space Extrema Detection

• Gaussian pyramid



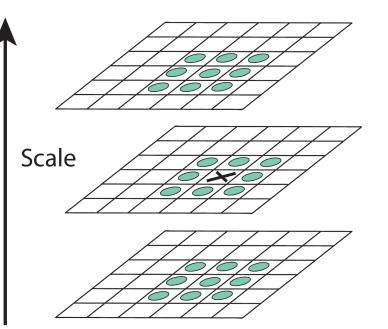
• Gaussian filters

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$
$$G_{\sigma_1} * G_{\sigma_2} = G_{\sigma} \quad \sigma^2 = \sigma_1^2 + \sigma_2^2$$

- Sub-sampling by a factor of 2
  - Multiple the Gaussian kernel deviation by 2

#### SIFT: Scale-space Extrema Detection

Scale (next octave) Scale (first octave) Difference of Gaussian (DOG) Gaussian



#### Maxima and minima of DoG images

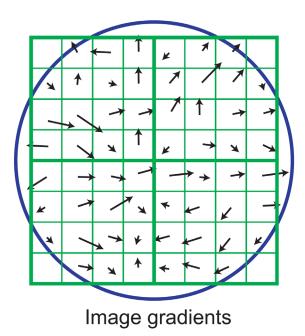
$$\begin{split} L(x,y,\sigma) &= G(x,y,\sigma) * I(x,y) \\ G(x,y,\sigma) &= \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2} \end{split} \quad D(x,y,\sigma) = (G(x,y,k\sigma) - G(x,y,\sigma)) * I(x,y) \\ &= L(x,y,k\sigma) - L(x,y,\sigma). \end{split}$$

. . .

# SIFT Descriptor

• Image gradient magnitude and orientation

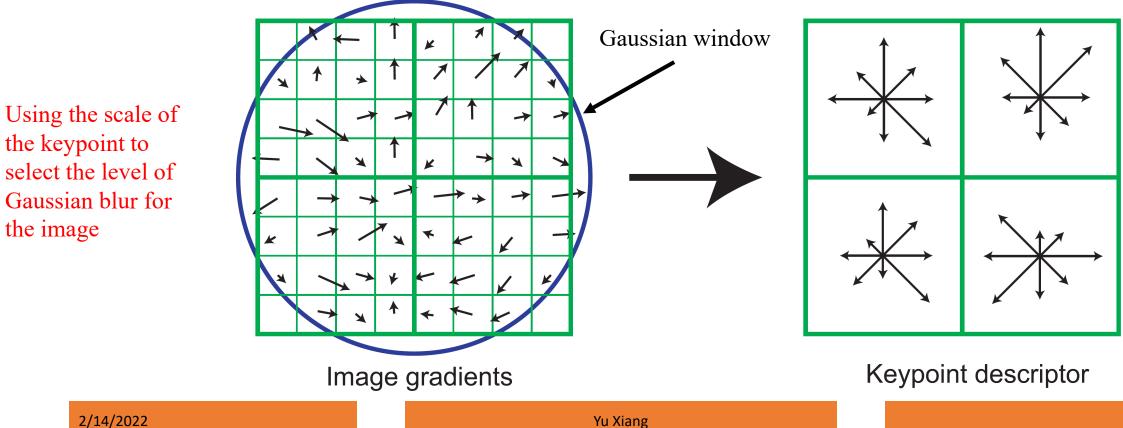
$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$



# SIFT Descriptor

the image

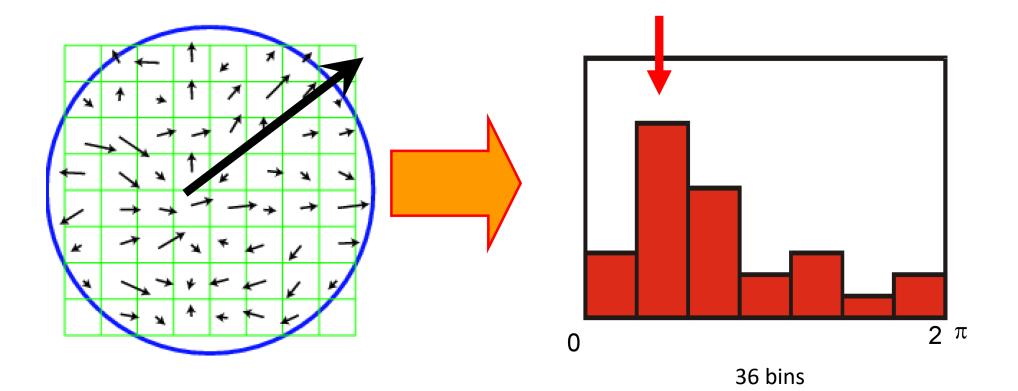
- Divide the 16x16 window into a 4x4 grid of cells (2x2 case shown below) •
- Compute an orientation histogram for each cell •
- 16 cells \* 8 orientations = 128 dimensional descriptor



28

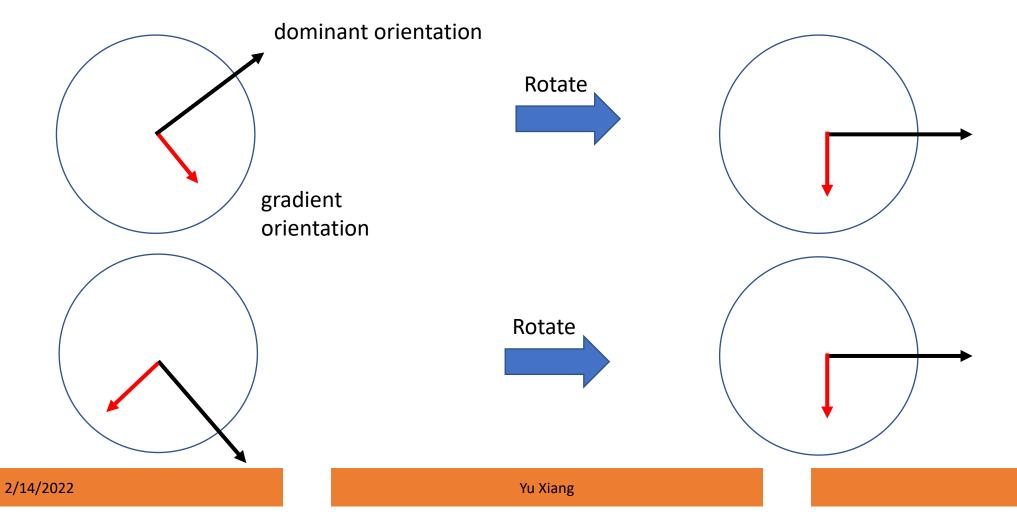
# SIFT: Rotation Invariance

• Rotate all orientations by the dominant orientation



# SIFT: Rotation Invariance

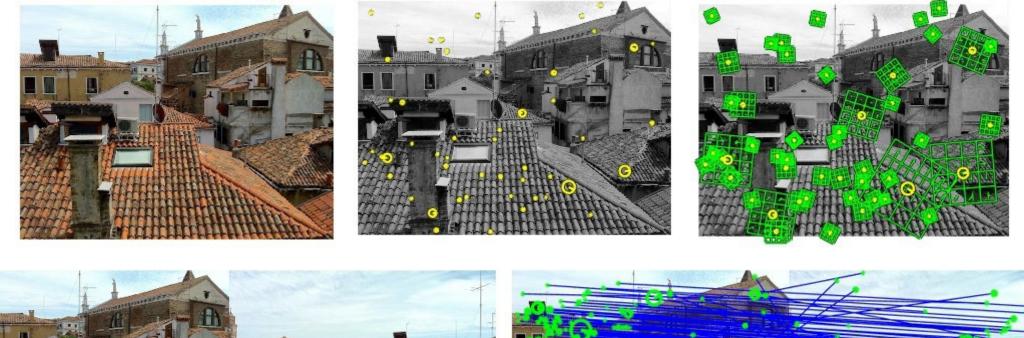
• Rotate all orientations by the dominant orientation



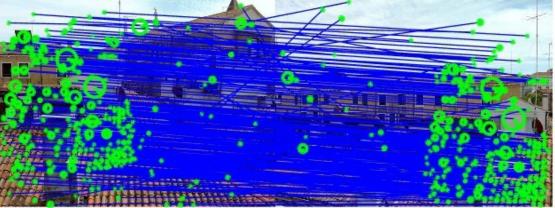
# **SIFT** Properties

- Can handle change in viewpoint (up to about 60 degree out of plane rotation)
- Can handle significant change in illumination
- Relatively fast < 1s for moderate image sizes
- Lots of code available
  - E.g., <u>https://www.vlfeat.org/overview/sift.html</u>

# SIFT Matching Example

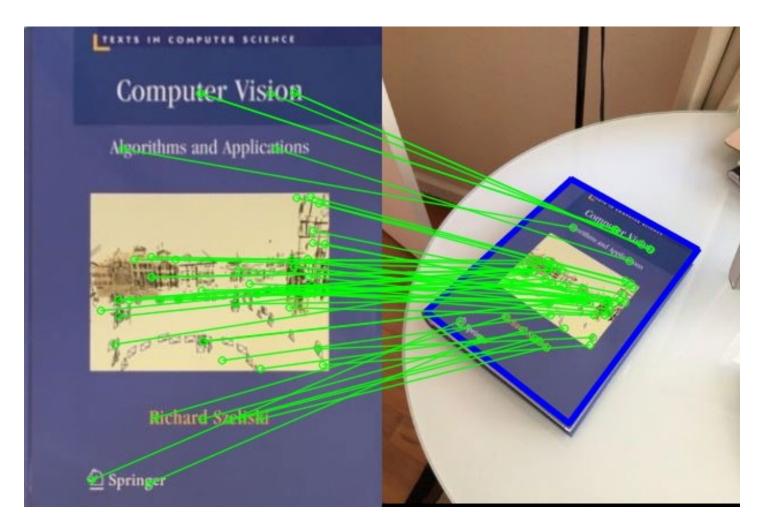






https://www.vlfeat.org/overview/sift.html

# SIFT Matching Example



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# Further Reading

- Section 7.1, Computer Vision, Richard Szeliski
- David Lowe, Distinctive Image Features from Scale-Invariant Keypoints. IJCV, 2004
- ORB: An efficient alternative to SIFT or SURF. Rublee et al., ICCV, 2011