Keypoint Features II

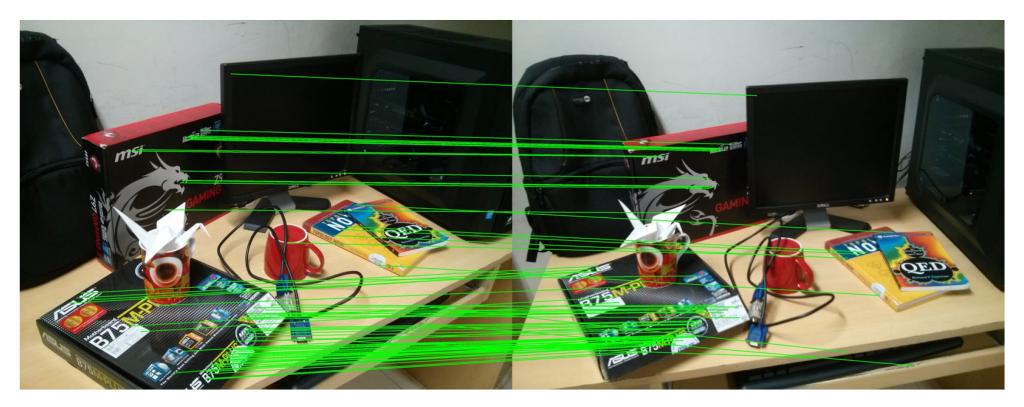
CS 6384 Computer Vision Professor Yu Xiang The University of Texas at Dallas

Some slides of this lecture are courtesy Kris Kitani

EST. 1969

UNIN

Feature Detection and Matching

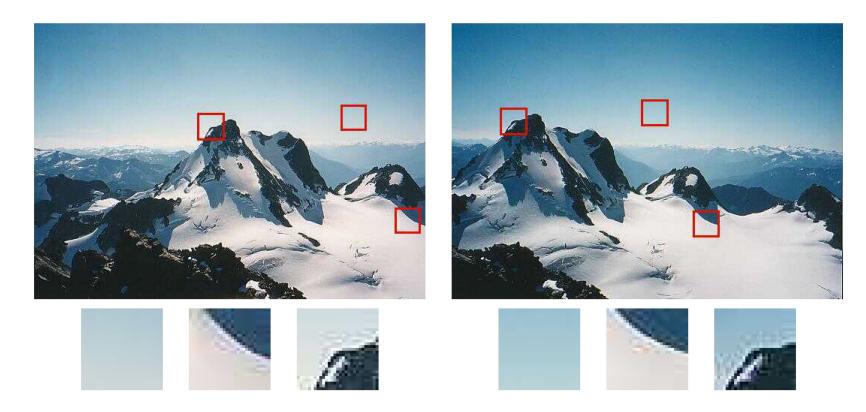


Geometry-aware Feature Matching for Structure from Motion Applications. Shah et al, WACV'15

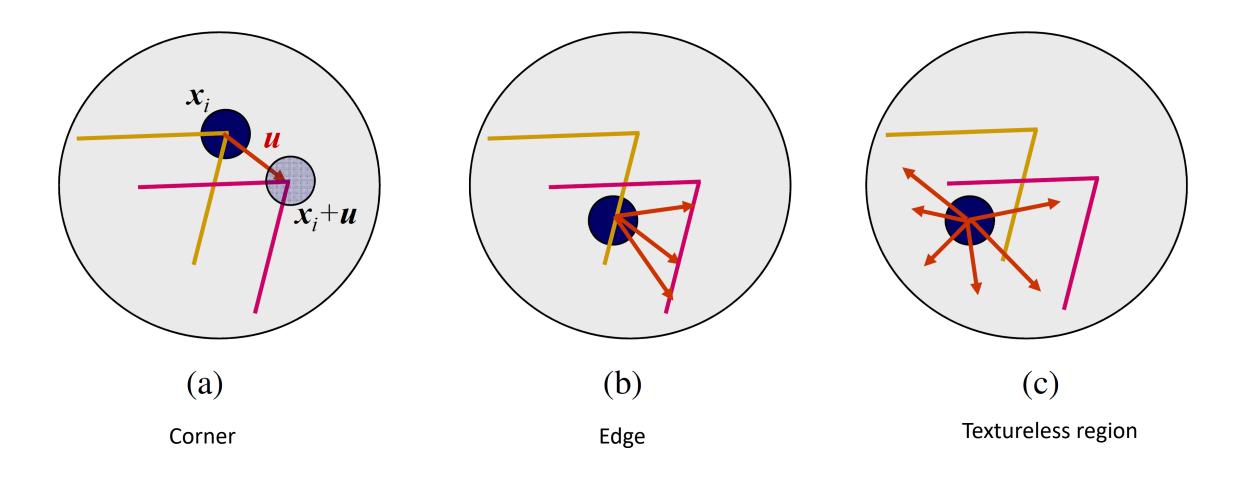
Applications: stereo matching, image stitching, 3D reconstruction, camera pose estimation, object recognition

Feature Detectors

 How to find image locations that can be reliably matched with images?



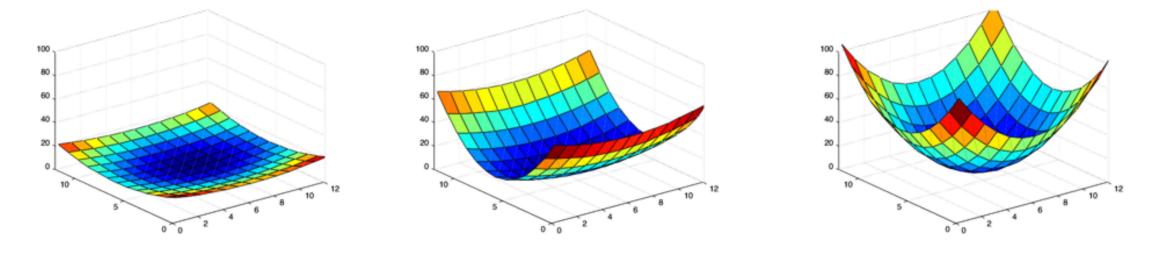
Feature Detectors



Harris Corner Detector

$$f(\Delta x, \Delta y) \approx \sum_{x,y} w(x,y) (I_x(x,y)\Delta x + I_y(x,y)\Delta y)^2$$

$$f(\Delta x, \Delta y) \approx (\Delta x \quad \Delta y) M\begin{pmatrix}\Delta x\\\Delta y\end{pmatrix} \qquad M = \sum_{x,y} w(x,y) \begin{bmatrix} I_x^2 & I_x I_y\\I_x I_y & I_y^2 \end{bmatrix} = \begin{bmatrix} \sum_{x,y} w(x,y) I_x^2 & \sum_{x,y} w(x,y) I_x I_y\\\sum_{x,y} w(x,y) I_x I_y & \sum_{x,y} w(x,y) I_y^2 \end{bmatrix}$$



Flat

2/14/2022

Edge

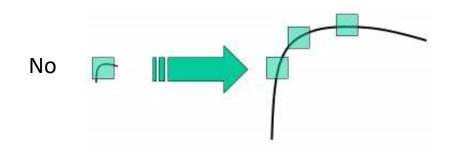
Yu Xiang

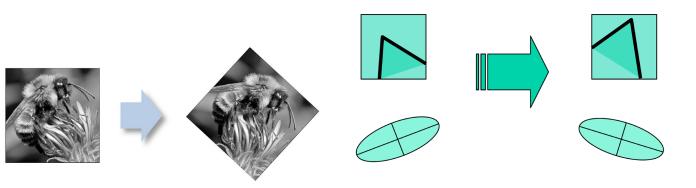
Corner

Invariance

- Can the same feature point be detected after some transformation?
 - Translation invariance Are Harris corners translation invariance?
 - 2D rotation invariance Are Harris corners rotation invariance?
 - Scale invariance

Are Harris corners scale invariance?









Scale Invariance

• Solution 1: detection features in all scales, matching features in corresponding scale (for small scale change)

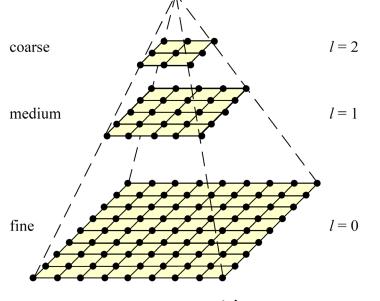
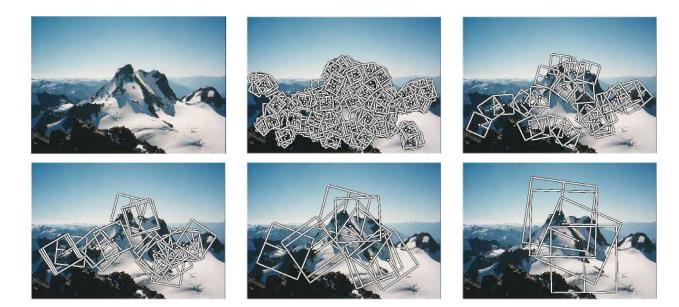


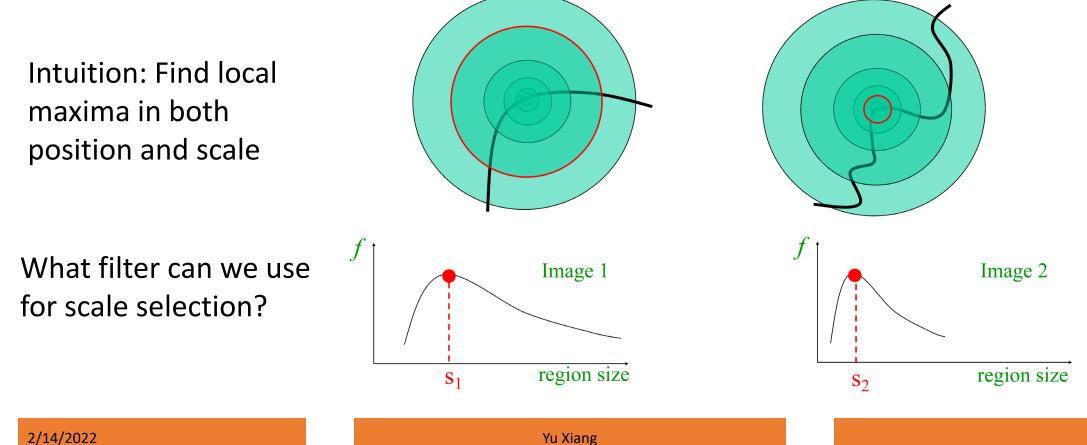
Image pyramid



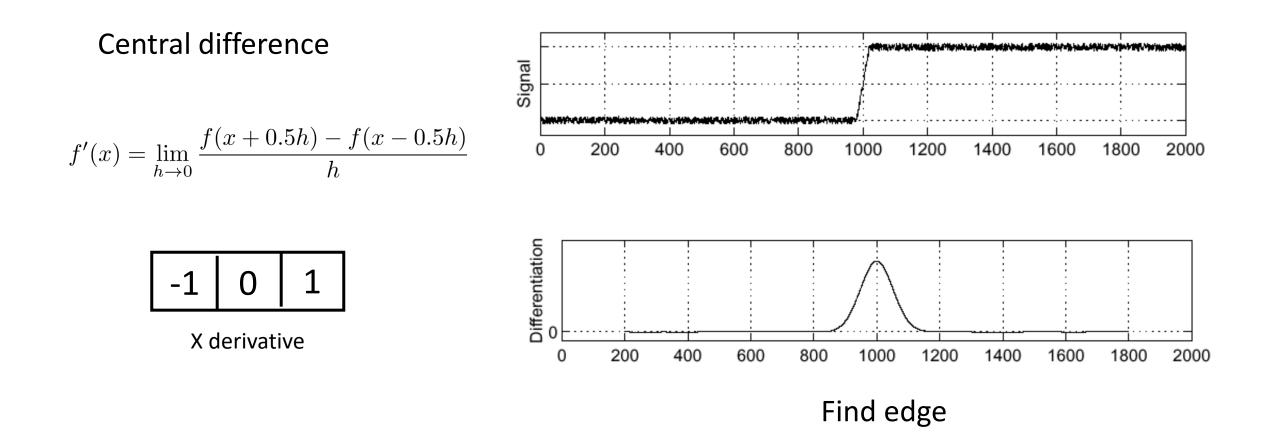
Multi-scale oriented patches (MOPS) extracted at five pyramid levels (Brown, Szeliski, and Winder 2005)

Scale Invariance

Solution 2: detect features that are stable in both location and scale

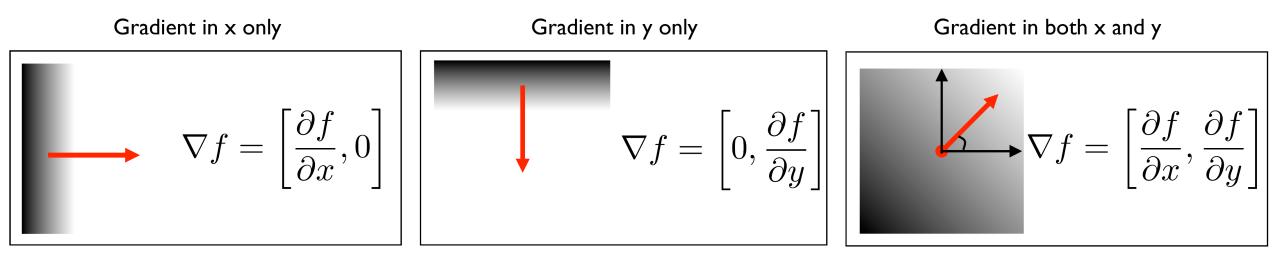


Recall Derivative Filter



2/14/2022

Image Gradient



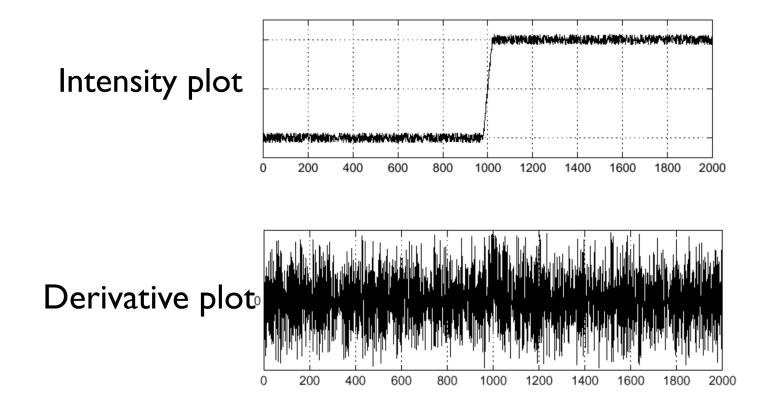
Gradient direction

$$\theta = \tan^{-1} \left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$$

Gradient magnitude
$$\nabla f || = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

Signal Noises

• Derivative filters are sensitive to noises



How to deal with noises?

Gaussian Filter

• Smoothing

$$1D \quad g(x) = \frac{1}{\sqrt{2\pi\sigma}} e^{-\frac{x^2}{2\sigma^2}}$$

$$g(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$g(x,y) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$Gaussian Filter h$$

$$g(x) = \frac{1}{2\pi\sigma^2} e^{-\frac{x^2+y^2}{2\sigma^2}}$$

$$Gaussian Filter h$$

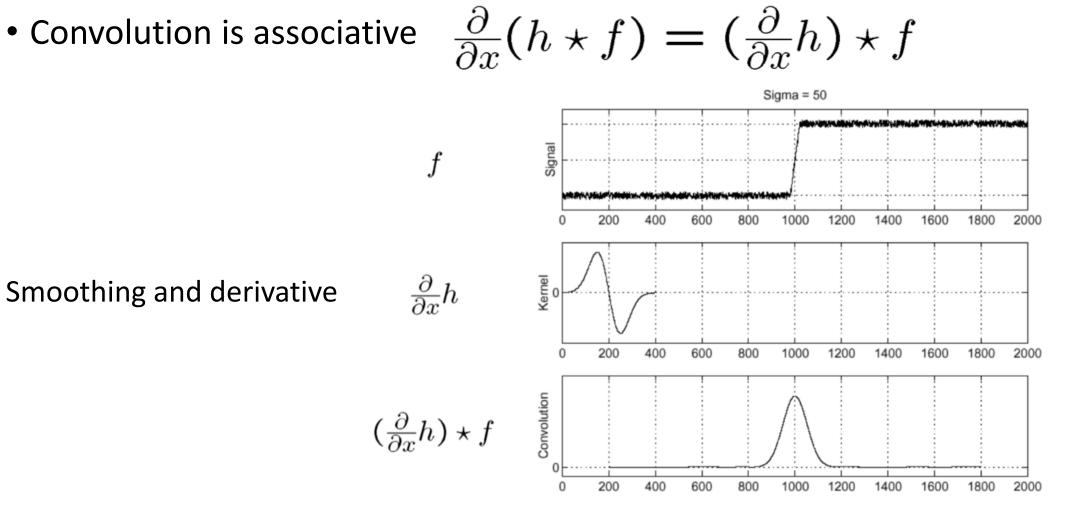
$$Gaussi$$

Sigma = 50

-2.0 0.0

2.0

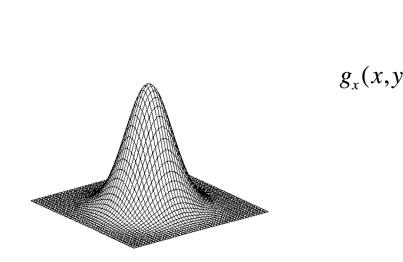
Derivative of Gaussian Filter



Smoothing and derivative

Derivative of Gaussian Filter

• Convolution is associative $\frac{\partial}{\partial x}(h \star f) = (\frac{\partial}{\partial x}h) \star f$



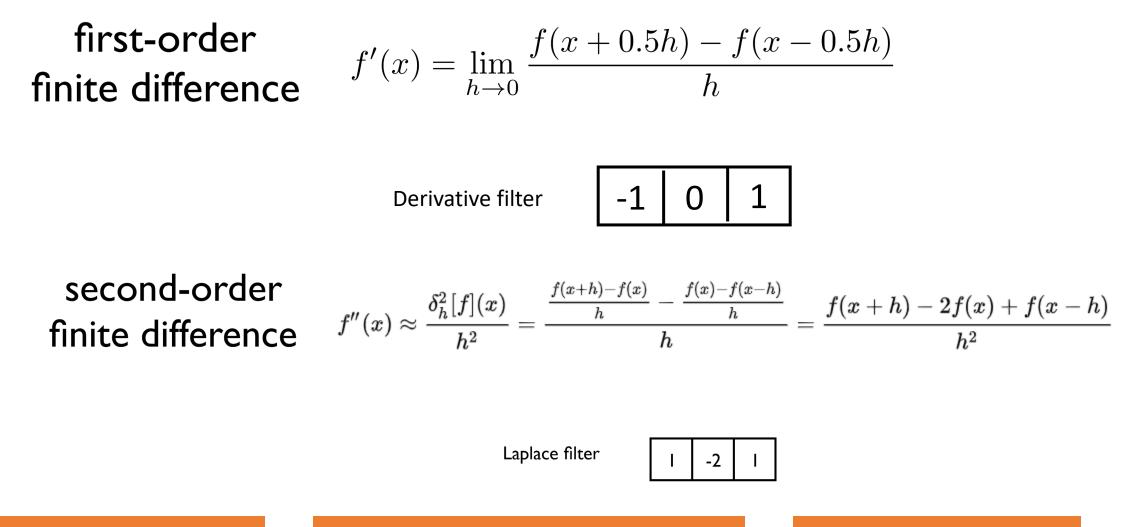
 $g_{x}(x,y) = \frac{\partial g(x,y)}{\partial x} = \frac{-x}{2\pi\sigma^{4}}e^{-\frac{x^{2}+y^{2}}{2\sigma^{2}}} \qquad g_{y}(x,y) = \frac{\partial g(x,y)}{\partial y} = \frac{-y}{2\pi\sigma^{4}}e^{-\frac{x^{2}+y^{2}}{2\sigma^{2}}}$

Gaussian

$$g(x,y) = rac{1}{2\pi\sigma^2} e^{-rac{x^2+y^2}{2\sigma^2}}$$



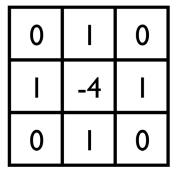
Laplace Filter



Laplace Filter

• 2D $\nabla^2 \mathbf{I} = \frac{\partial^2 \mathbf{I}}{\partial x^2} + \frac{\partial^2 \mathbf{I}}{\partial y^2}$





ID Laplace filter

2D Laplace filter

Laplacian of Gaussian Filter

$$\nabla^2 \mathbf{I} = \frac{\partial^2 \mathbf{I}}{\partial x^2} + \frac{\partial^2 \mathbf{I}}{\partial y^2}$$
$$\nabla^2 \mathbf{I} \circ g = \nabla^2 g \circ \mathbf{I}$$
$$\nabla^2 g = \frac{x^2 + y^2 - 2\sigma^2}{\sigma^4} g(x, y)$$

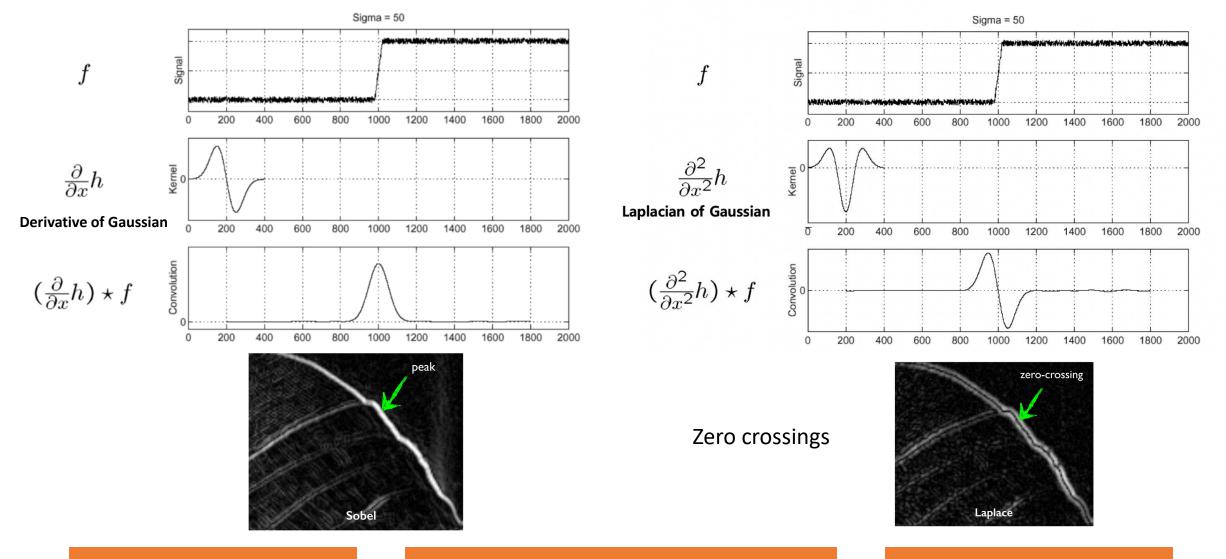
 $\nabla^2 h_\sigma(u,v)$

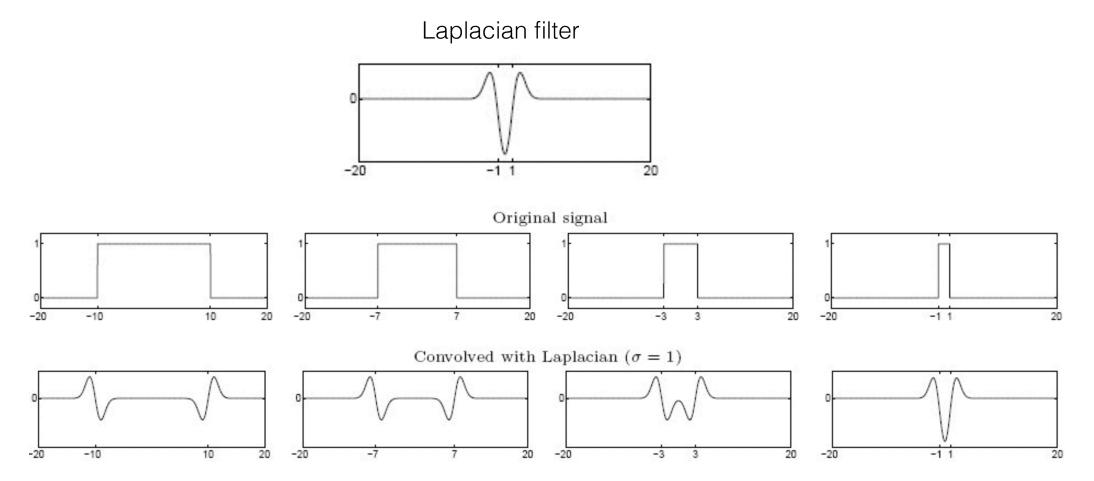


Laplacian of Gaussian

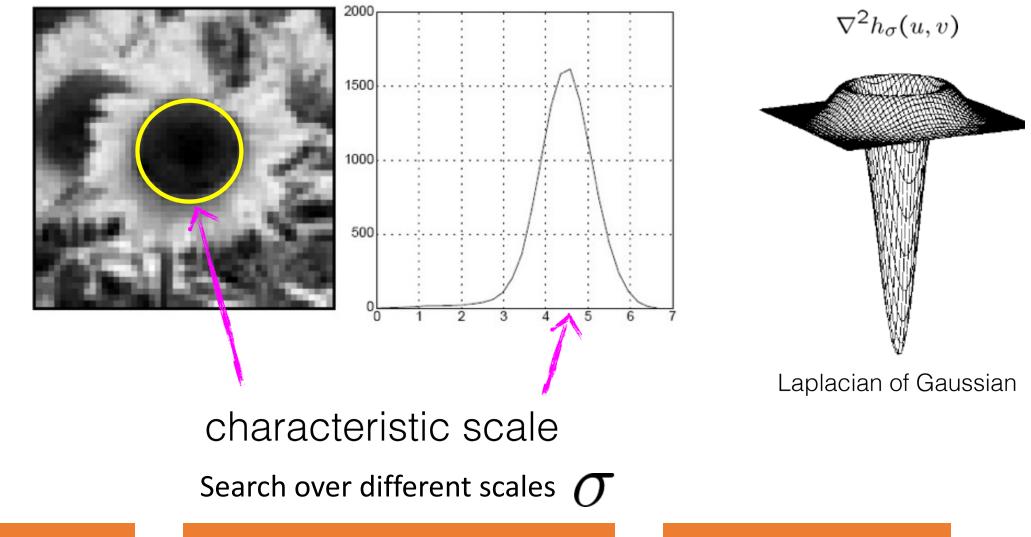
Smoothing and second derivative

Laplacian of Gaussian Filter

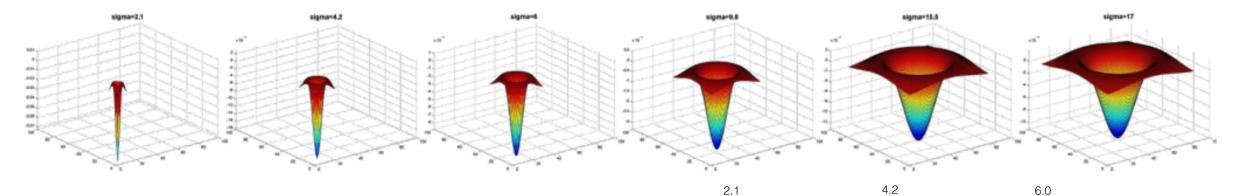




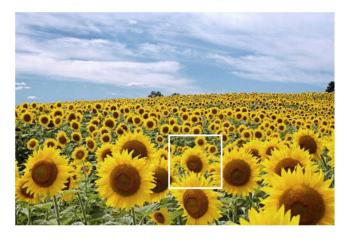
Highest response when the signal has the same **characteristic scale** as the filter

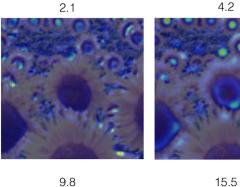


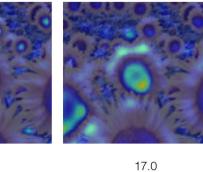
2/14/2022

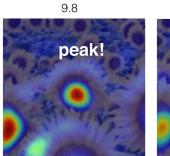


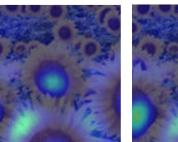
Multi-scale 2D Blob detection



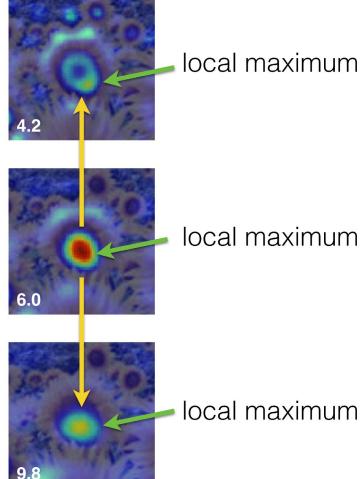










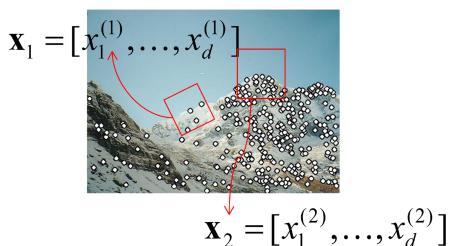


local maximum

cross-scale maximum

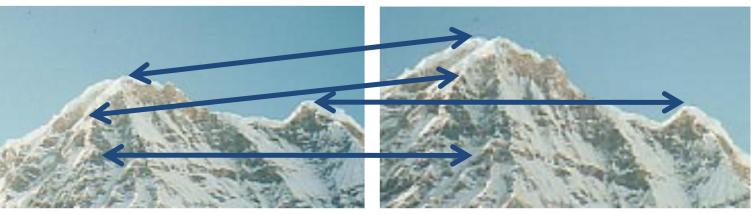
Scale Invariance Feature Transform (SIFT)

• Keypoint detection



• Compute descriptors

• Matching descriptors



David Lowe, Distinctive Image Features from Scale-Invariant Keypoints. IJCV, 2004

2/14/2022

SIFT: Scale-space Extrema Detection

• Difference of Gaussian (DoG)

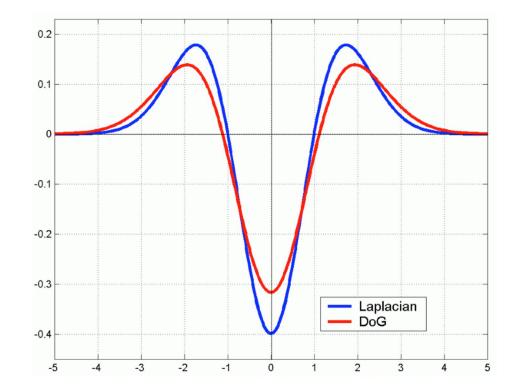
$$G(x, y, \sigma) = \frac{1}{2\pi\sigma^2} e^{-(x^2 + y^2)/2\sigma^2}$$

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$

$$D(x, y, \sigma) = (G(x, y, k\sigma) - G(x, y, \sigma)) * I(x, y)$$

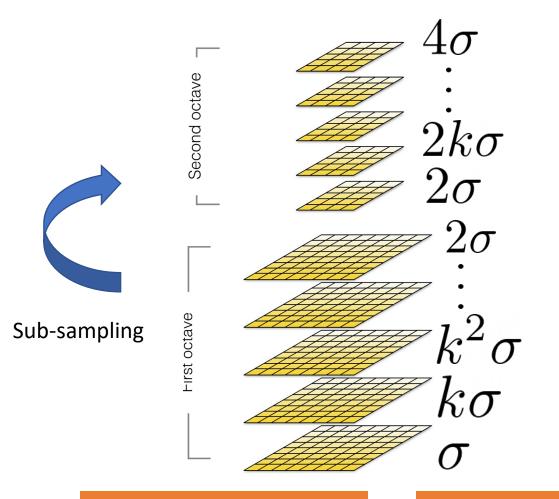
= $L(x, y, k\sigma) - L(x, y, \sigma).$

Approximate of Laplacian of Gaussian (efficient to compute)



SIFT: Scale-space Extrema Detection

• Gaussian pyramid



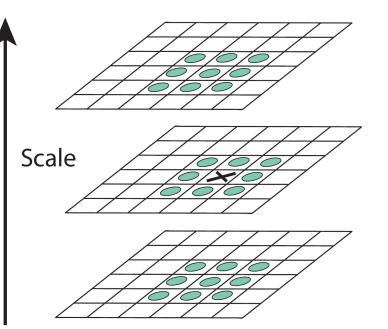
• Gaussian filters

$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$
$$G_{\sigma_1} * G_{\sigma_2} = G_{\sigma} \quad \sigma^2 = \sigma_1^2 + \sigma_2^2$$

- Sub-sampling by a factor of 2
 - Multiple the Gaussian kernel deviation by 2

SIFT: Scale-space Extrema Detection

Scale (next octave) Scale (first octave) Difference of Gaussian (DOG) Gaussian



Maxima and minima of DoG images

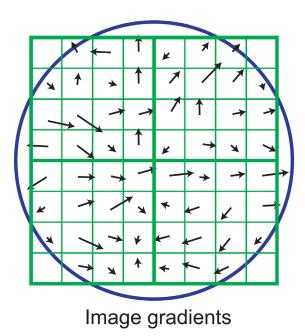
$$\begin{split} L(x,y,\sigma) &= G(x,y,\sigma) * I(x,y) \\ G(x,y,\sigma) &= \frac{1}{2\pi\sigma^2} e^{-(x^2+y^2)/2\sigma^2} \end{split} \quad D(x,y,\sigma) = (G(x,y,k\sigma) - G(x,y,\sigma)) * I(x,y) \\ &= L(x,y,k\sigma) - L(x,y,\sigma). \end{split}$$

. . .

SIFT Descriptor

• Image gradient magnitude and orientation

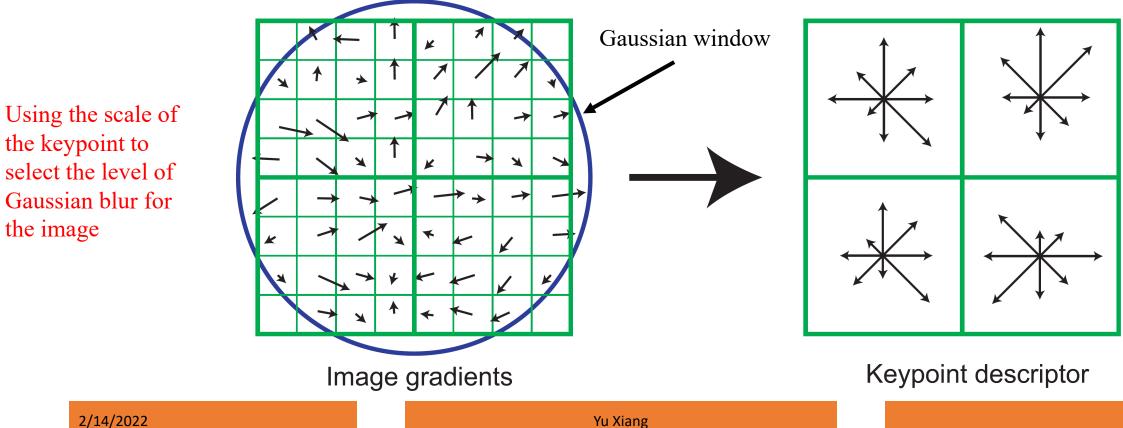
$$L(x, y, \sigma) = G(x, y, \sigma) * I(x, y)$$



SIFT Descriptor

the image

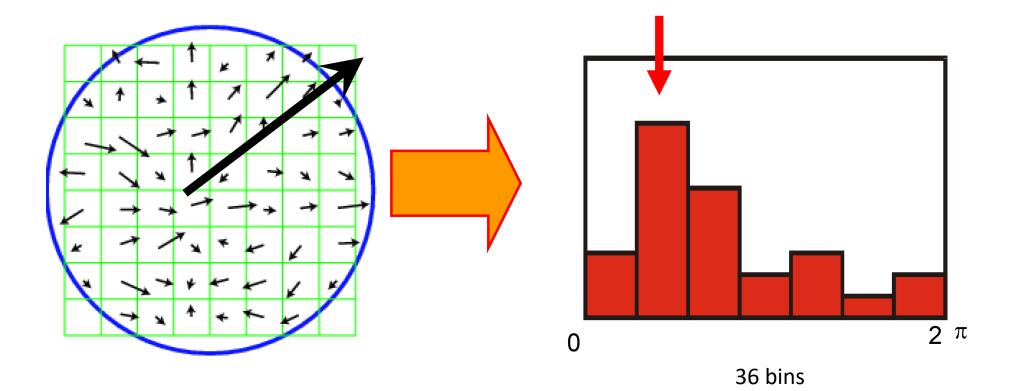
- Divide the 16x16 window into a 4x4 grid of cells (2x2 case shown below) •
- Compute an orientation histogram for each cell •
- 16 cells * 8 orientations = 128 dimensional descriptor



28

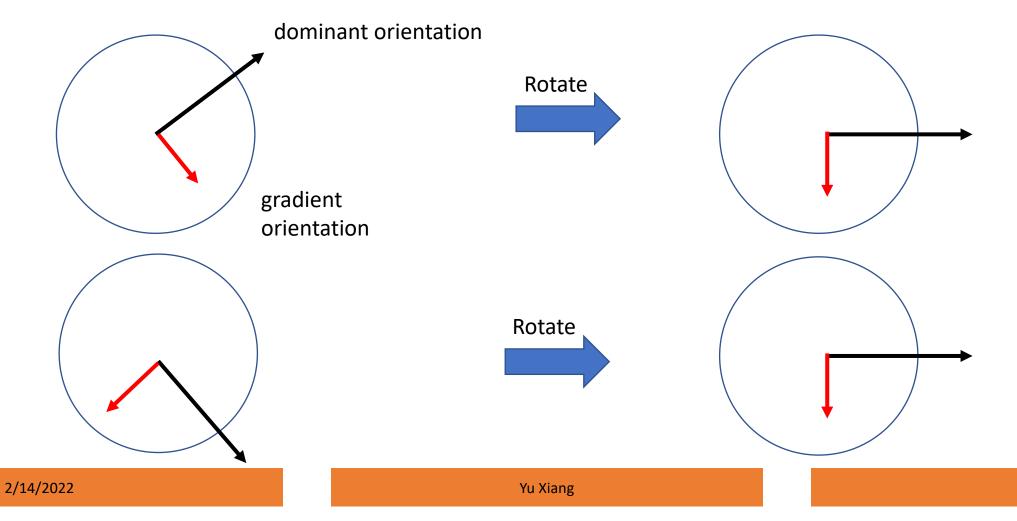
SIFT: Rotation Invariance

• Rotate all orientations by the dominant orientation



SIFT: Rotation Invariance

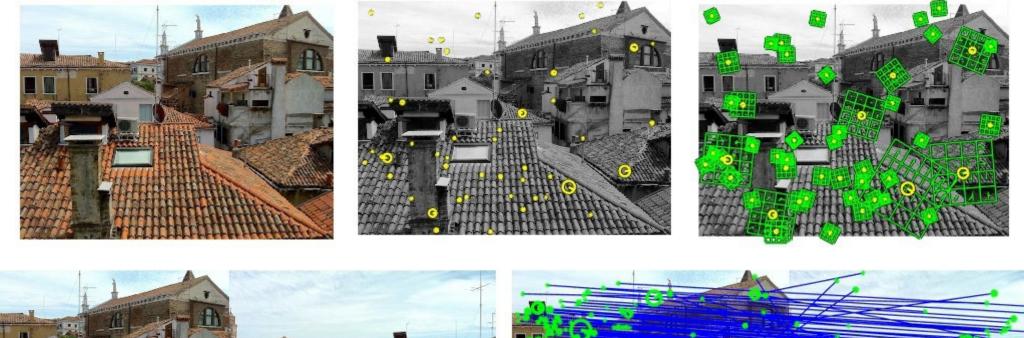
• Rotate all orientations by the dominant orientation



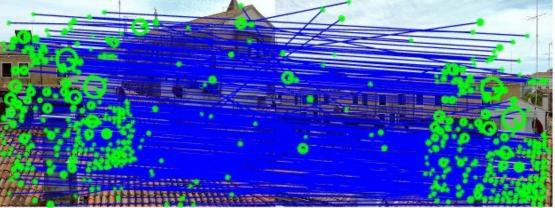
SIFT Properties

- Can handle change in viewpoint (up to about 60 degree out of plane rotation)
- Can handle significant change in illumination
- Relatively fast < 1s for moderate image sizes
- Lots of code available
 - E.g., <u>https://www.vlfeat.org/overview/sift.html</u>

SIFT Matching Example

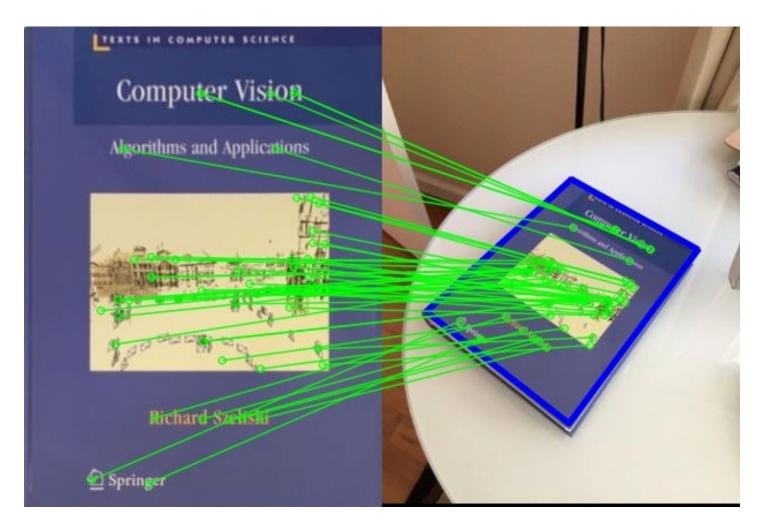






https://www.vlfeat.org/overview/sift.html

SIFT Matching Example



2/14/2022

Further Reading

- Section 7.1, Computer Vision, Richard Szeliski
- David Lowe, Distinctive Image Features from Scale-Invariant Keypoints. IJCV, 2004
- ORB: An efficient alternative to SIFT or SURF. Rublee et al., ICCV, 2011