

Pose Tracking I

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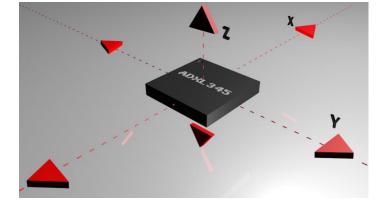
Tracking in VR

- Tracking the user's sense organs
 - E.g., Head and eye
 - Render stimulus accordingly
- Tracking user's other body parts
 - E.g., human body and hands
 - Locomotion and manipulation
- Tracking the rest of the environment
 - Augmented reality
 - Obstacle avoidance in the real world



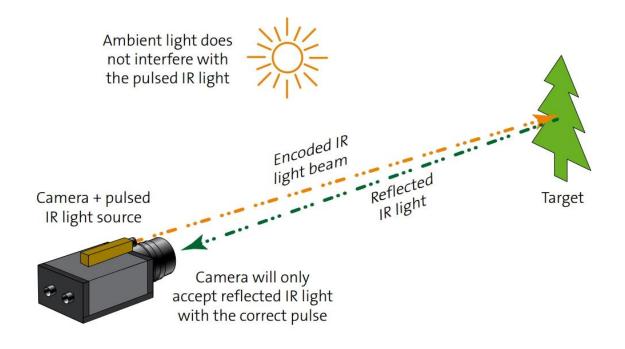
Tracking 3D Orientation and 3D Position

- Why not just integrate the accelerometer?
 - Drift error, quadratically growing with calibration error (difference between true value and the measured value)
 - The true body acceleration cannot be accurately extracted, especially when the body quickly rotates
 - IMU itself cannot help
 - Cannot distinguish motions at constant velocity



Wave-based Tracking

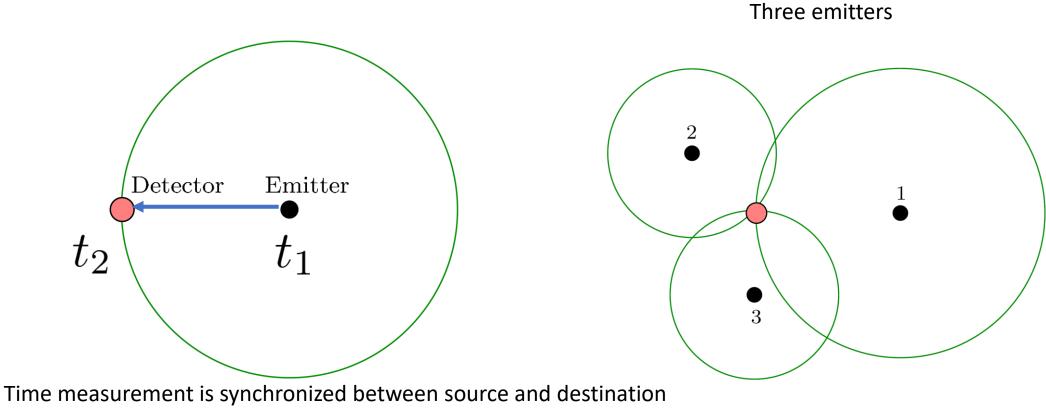
- Active tracking systems
 - Infrared, ultrasound, and electromagnetic fields
- Emitter-detector pair
 - Speaker-microphone
 - Time of flight to estimate distance



https://www.stemmer-imaging.com/en-ie/knowledge-base/cameras-3d-time-of-flight-cameras/

Wave-based Tracking

• Trilateration



Use time of arrival (time of flight) to compute distance

• 330 m/s for ultrasound

10/6/2021

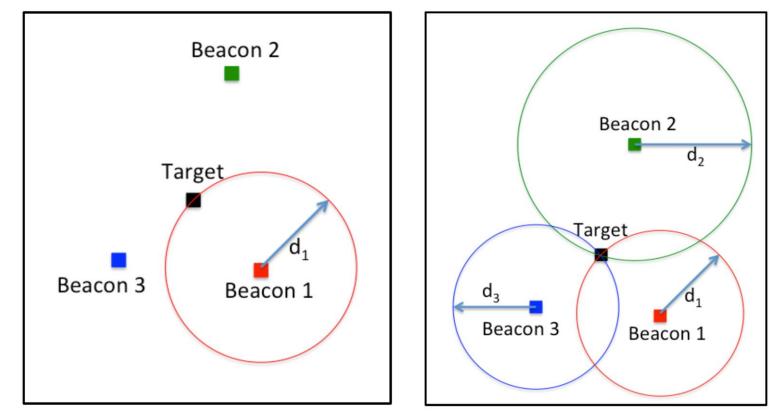
Time of Arrival (ToA)

• Signals sent from a beacon to the target

• Known sending time and arrival time

$$d = c * (t_{arrival} - t_{sent})$$

 $d = \sqrt{(x_{ref} - x)^{2} + (y_{ref} - y)^{2}}$



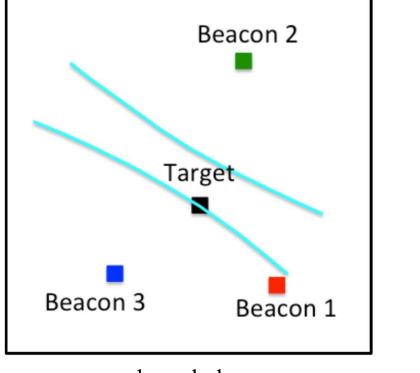
https://sites.tufts.edu/eeseniordesignhandbook/files/2017/05/FireBrick_OKeefe_F1.pdf

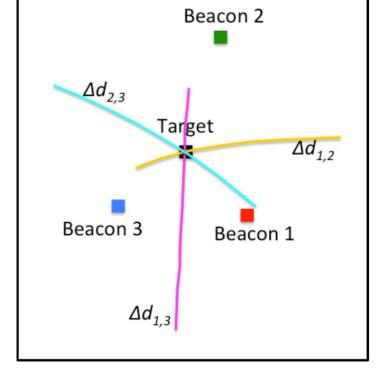
Time Difference of Arrival (TDoA)

- Do not know sending time
- Signals sent from the target to beacons

 $\Delta d = c * (\Delta t)$

$$\Delta d = \sqrt{(x_2 - x)^2 - (y_2 - y)^2} - \sqrt{(x_1 - x)^2 - (y_1 - y)^2}$$





hyperbola

https://sites.tufts.edu/eeseniordesignhandbook/files/2017/05/FireBrick_OKeefe_F1.pdf

Yu Xiang

Wave-based Tracking

- Magnetic fields
 - The field should vary greatly across different locations
 - Drawback: the field may become unpredictably warped in each environment, causing straight-line motions to be estimated as curved

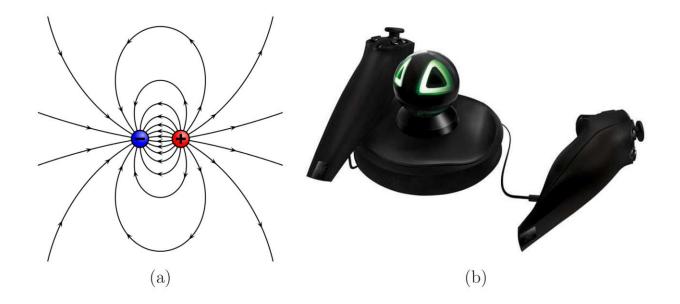
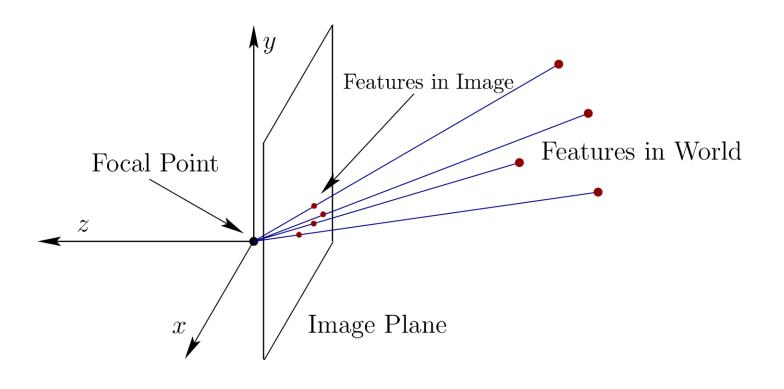


Figure 9.10: (a) A magnetic dipole offers a field that varies its magnitude and direction as the position changes (figure by Wikipedia user Geek3). (b) The Razer Hydra, a game controller system that generates a weak magnetic field using a base station, enabling it to track the controller positions (figure by http://www.GamingShogun.com/).

Feature-based Tracking

• Using visibility of features in the real world



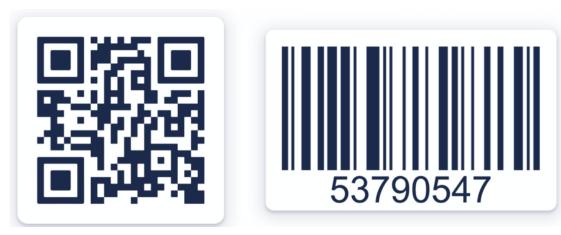
- Natural Features
 - No setup cost
 - A difficult computer vision problem
- Artificial features
 - Print a special tag



QR code

QR Code (Quick Response Code)

• QR codes contains more information than barcodes



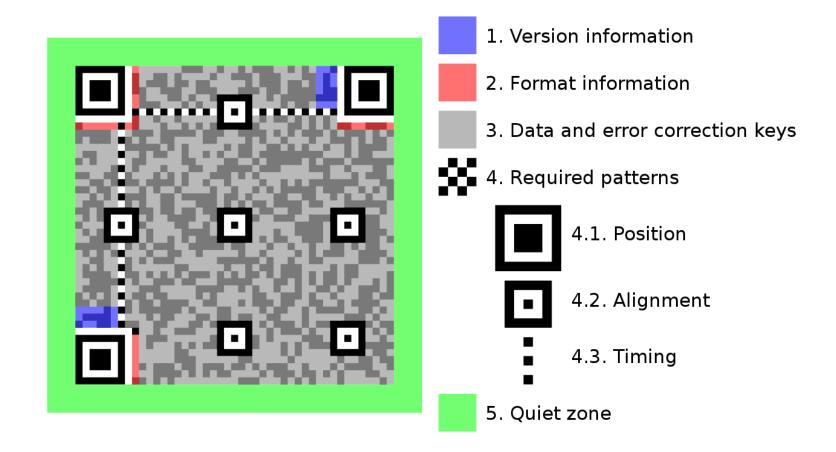
7,089 numeric characters or 2,953 alphanumeric characters

20 to 100 characters



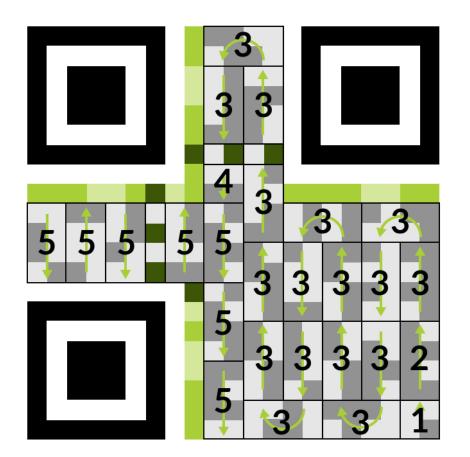
Photo of QR Code inventor Masahiro Hara. Source: <u>qrcode.com</u> DENSO WAVE

QR Code



Structure of a QR code (version 7), highlighting functional elements (Wikipedia)

QR Code



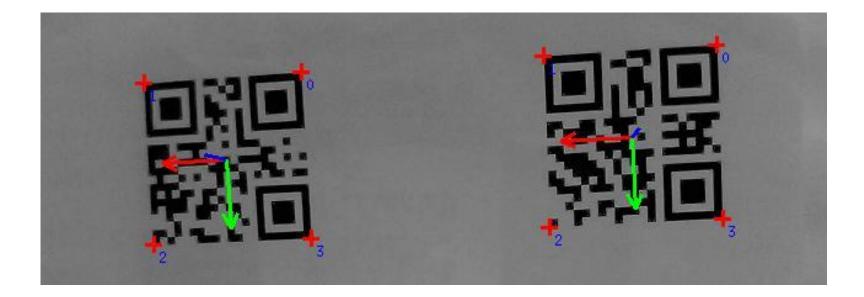
1 Mode indicator
2 Character count indicator
3 Standard data modules
4 Stop indicator
5 Error correction modules
Fixed patterns
Format information

Mode type: numeric, alphanumeric, byte, or kanji (Japanese)

Data is stored in bitse.g., 01011011

QR Code for Pose Estimation

• Using the 4 corners of a QR code as features

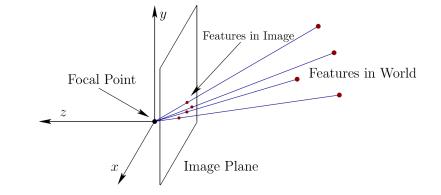


https://visp-doc.inria.fr/doxygen/visp-daily/tutorial-pose-estimation-qrcode.html

The Perspective-n-Point (PnP) Problem

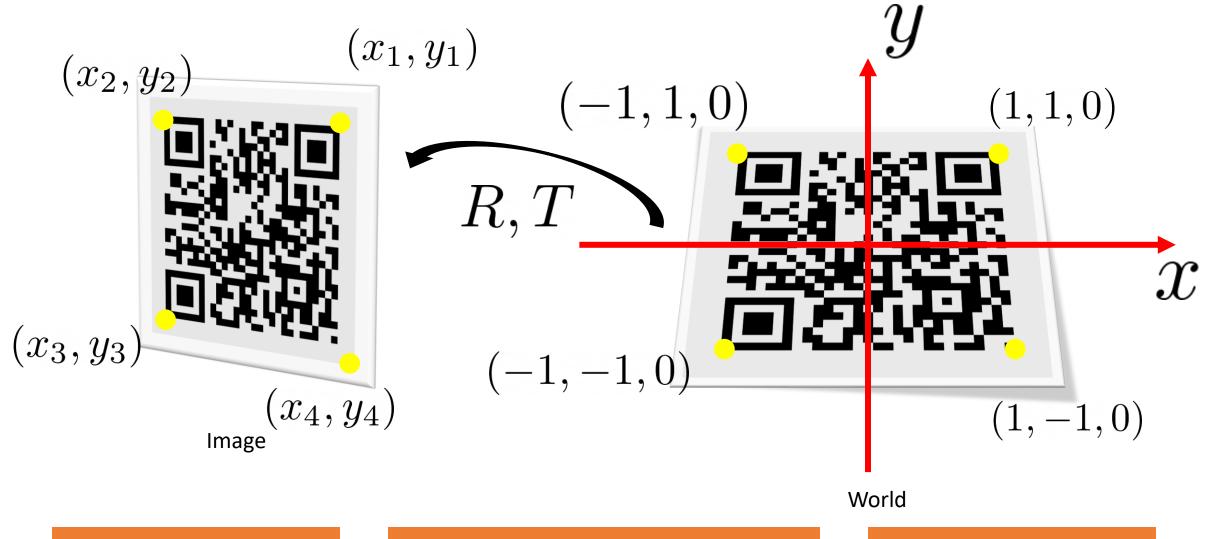
- Given/known variables
 - A set of n 3D points in the world coordinates p_w
 - Their projections (2D coordinates) on an image p_c
 - Camera intrinsics K
- Unknown variables
 - 3D rotation of the camera with respective to the world coordinates R
 - 3D translation of the camera T

$$s \, p_c = K \left[\, R \, | \, T \,
ight] \, p_w$$
 $s egin{bmatrix} u \ v \ 1 \end{bmatrix} = egin{bmatrix} f_x & \gamma & u_0 \ 0 & f_y & v_0 \ 0 & 0 & 1 \end{bmatrix} egin{bmatrix} r_{11} & r_{12} & r_{13} & t_1 \ r_{21} & r_{22} & r_{23} & t_2 \ r_{31} & r_{32} & r_{33} & t_3 \end{bmatrix} egin{bmatrix} x \ y \ z \ 1 \end{bmatrix}$



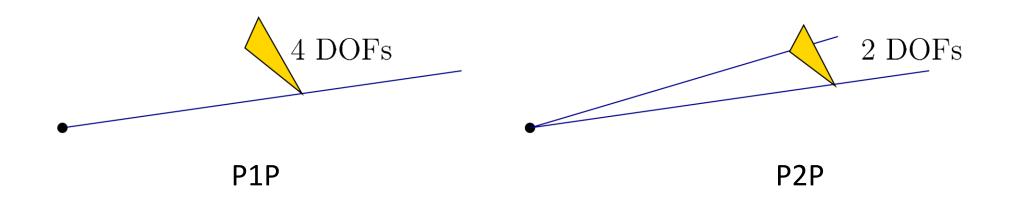
F

The PnP Problem with QR Code

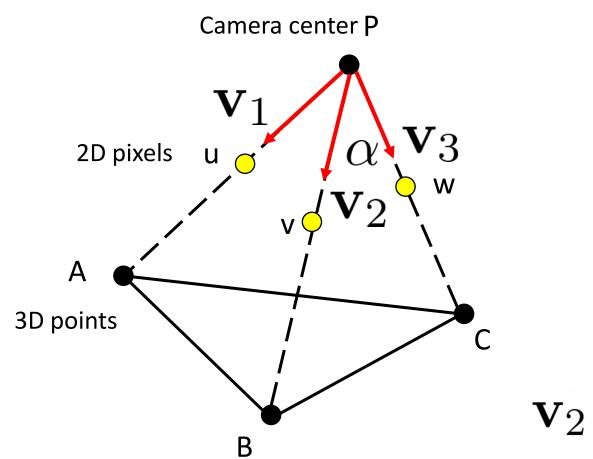


The Perspective-n-Point (PnP) Problem

- 6 degrees of freedom (DOFs)
 - 3 DOF rotation, 3 DOF translation
- Each feature that is visible eliminates 2 DOFs



P3P

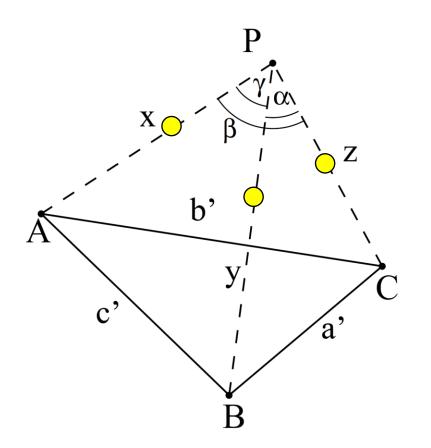


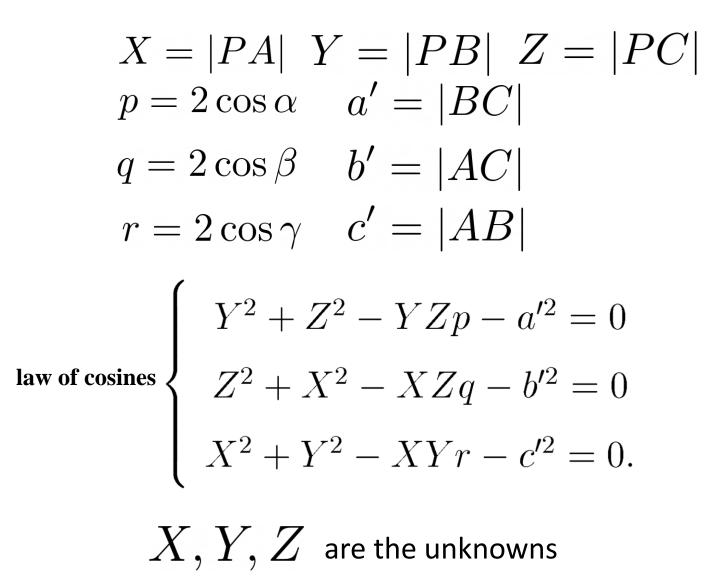
$$\mathbf{v}_1 = K^{-1}\mathbf{u}$$
$$\mathbf{v}_2 = K^{-1}\mathbf{v}$$
$$K^{-1}\mathbf{v}$$

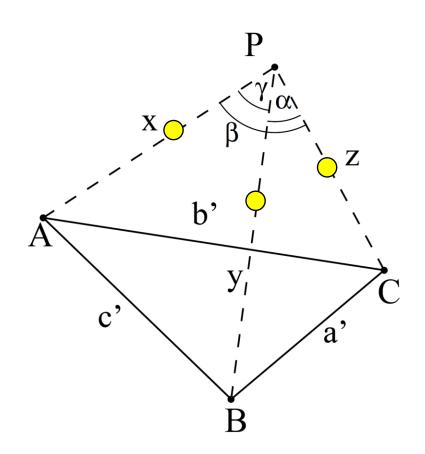
$$\mathbf{v}_3 = K^{-1}\mathbf{w}$$

$\mathbf{v}_2 \cdot \mathbf{v}_3 = \|\mathbf{v}_2\| \|\mathbf{v}_3\| \cos \alpha$

P3P







- Find the solutions for X, Y, Z (depth of the 3 pixels)
- Obtain the coordinates of A, B, C in camera frame
- Compute R and T using the coordinates of A, B, C in camera frame and in world frame

6D Pose Between Two Sets of 3D Points

- A well-studied problem
- Least-squares Estimation

$$\Sigma^{2} = \sum_{i=1}^{N} \| p_{i}' - (Rp_{i} + T) \|^{2}.$$

K.S. Arun, T.S. Huang, and S.D. Blostein. Least-Squares Fitting of Two 3-D Points Sets. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 9(5):698–700, 1987.

S. Umeyama. Least-squares estimation of transformation parameters between two point patterns. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 13(4), April 1991

Further Reading

• Section 9.3, Virtual Reality, Steven LaValle